

A and F stars as probes of outer Galactic disc kinematics

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ABSTRACT

Previous studies of the rotation law in the outer Galactic disc have mainly used gas tracers or clump giants. Here, we explore A and F stars as alternatives: these provide a much denser sampling in the outer disc than gas tracers and have experienced significantly less velocity scattering than older clump giants. This first investigation confirms the suitability of A stars in this role. Our work is based on spectroscopy of ~ 1300 photometrically selected stars in the red calcium-triplet region, chosen to mitigate against the effects of interstellar extinction. The stars are located in two low Galactic latitude sightlines, at longitudes $\ell = 118^\circ$, sampling strong Galactic rotation shear, and $\ell = 178^\circ$, near the anticentre. With the use of Markov Chain Monte Carlo parameter fitting, stellar parameters and radial velocities are measured, and distances computed. The obtained trend of radial velocity with distance is inconsistent with existing flat or slowly rising rotation laws from gas tracers (Brand & Blitz 1993; Reid et al. 2014). Instead, our results fit in with those obtained by Huang et al. (2016) from disc clump giants that favoured rising circular speeds. An alternative interpretation in terms of spiral arm perturbation is not straight forward. We assess the role that undetected binaries in the sample and distance error may have in introducing bias, and show that the former is a minor factor. The random errors in our trend of circular velocity are within $\pm 5 \text{ km s}^{-1}$.

Key words: methods: observational – techniques: radial velocities – Galaxy: disc – Galaxy: kinematics and dynamics.

1 INTRODUCTION

The kinematics of stars outside the Solar Circle is relatively poorly known. In addition to setting a constraint on the Galactic potential, secure knowledge of the motions of stars at all radii and longitudes in the Galactic disc facilitates studies of non-axisymmetric motion, such as streaming motions due to spiral density waves or transient winding arms. Understanding the kinematics of the disc in full, including the rotation law, will help us map out its structure, and set constraints on its formation and evolution.

Within the disc of the Milky Way, the rotational motion is the dominant component. The IAU recommended standard of the circular velocity at the Sun is 220 km s^{-1} (Kerr & Lynden-Bell 1986). This result is based mainly on the analysis of tracers of the gaseous interstellar medium (ISM), including CO, H I 21 cm, and H II radio recombination line observations. In recent decades, the work

of Brand & Blitz (1993) has been particularly influential. How the rotation varies outward from the Solar Circle is more challenging to measure than within because of the greater reliance on the uncertain distances to the ISM tracers.

It has been common practice to associate CO and H II radio recombination lines with star-forming regions whose distances are specified by spectroscopic parallax. More recent studies have made use of masers in star-forming regions with much better defined distances, and these have begun to favour a higher rotation speed. Honma et al. (2012) used a sample of 52 masers associated with pre-main-sequence stars to find the rotational velocity of the local standard of rest (LSR) to be between 223 and 248 km s^{-1} , with a flat rotation curve. Reid et al. (2014) took a similar approach, using an expanded sample of over 100 masers to refine the circular rotation speed at the Sun to $240 \pm 8 \text{ km s}^{-1}$. Bobylev, Bajkova & Shirokova (2016) support a raised circular speed ($236 \pm 6 \text{ km s}^{-1}$) and a nearly flat rotation curve, based on a large sample of open clusters.

A feature of the studies to date is a drop in sensitivity with increasing Galactocentric radius, R_G , as the number or quality of available

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measurements declines. In the case of maser measurements, just a handful are available beyond $R_G \sim 12$ kpc. Similarly, the number of star clusters catalogued at $R_G \geq 10$ kpc is limited to a few tens. This is an unavoidable consequence of the inherent low spatial frequency of these object classes outside the Solar Circle. Hence, Galactic rotation of the outer disc remains highly uncertain.

The frequency of stars at increasingly large Galactocentric radii becomes much higher than either masers or H II regions and work has been undertaken exploiting helium-burning clump giants that can serve as a form of standard candle (Castellani, Chieffi & Straniero 1992). Examples of this, emphasizing measurement of the outer disc, are the works by López-Corredoira (2014), using proper motions from PPMXL¹ and by Huang et al. (2016) using LSS-GAC² and APOGEE³ radial velocities. As older objects with ages exceeding 1 Gyr, clump giants will be subject to significant kinematic scatter, including asymmetric drift.

In this study, we examine another class of stellar tracer that can also provide a much denser sampling of the outer disc than is available from ISM tracers. We turn to A/F-type stars. These stars offer the following advantages: they are intrinsically relatively luminous, with absolute magnitudes in the i band of ~ 0 to 3; as younger objects (~ 100 Myr), they have experienced significantly less scattering within the Galactic disc (Dehnen & Binney 1998); and, as we shall show, the A stars especially are efficiently selected from photometric H α surveys. We are able to detect them at useful densities out to $R_G \sim 14$ kpc. Furthermore, the numbers of A-type stars most likely exceed the numbers of clump giants in the outer disc, given that the outer disc is younger than the inner disc (Bergemann et al. 2014). Our own investigations of photometry from the INT⁴ Photometric H α Survey of the Northern Galactic Plane (IPHAS; Drew et al. 2005), used here for target selection, supports this expectation.

We explore radial velocity (RV) measurements of near-main-sequence A/F stars as kinematic tracers in two outer-disc pencil beams, with a view to future fuller exploitation via spectroscopy on forthcoming massively multiplexed wide-field spectrographs (e.g. WEAVE,⁵ in construction for the William Herschel Telescope). To greatly reduce the impact of extinction on the reach of our samples, our observations target the calcium-triplet (CaT) region, in the far red part of the spectrum. Now is a good time to embark on this investigation in view of the imminent release of *Gaia* astrometry, which will include complementary proper motions of disc stars and support improved distance estimates.

We present a method of RV measurement in the CaT part of the spectrum and apply it to a data set of ~ 1300 spectra of A- and F-type field stars, in order to confirm their viability as tracers of Galactic disc kinematics and to pave the way for more comprehensive use of them in future. This first data set is made up of stars in two pencil beams at Galactic longitudes $\ell = 118^\circ$ and $\ell = 178^\circ$. Our data were obtained at MMT using the multi-object spectrograph HectoSpec. Section 2 describes the observations obtained and how they were

prepared for analysis. In Section 3, we detail the method used to obtain the RVs and stellar parameters and determine distances. The derived parameter distributions and error budgets are presented. The results obtained close to the anticentre at $\ell = 178^\circ$, our control direction, demonstrate the validity of the analysis, while the results at $\ell = 118^\circ$ indicate a strong departure from a flat or slowly rising Galactic rotation law (Section 4). In Section 5, we review possible bias, make comparisons with earlier results, and consider whether structure due to spiral arm perturbations may have been detected. Our results turn out to be consistent with the rising section of the rotation law presented by Huang et al. (2016) based on disc clump giants over the Galactocentric radius range 11–15 kpc. A summary of our conclusions is given in Section 6.

2 OBSERVATIONS AND DATA

2.1 Sightline and selection of targets for observation

We chose to study two pencil-beam sightlines located at Galactic co-ordinates $\ell = 178^\circ$, $b = 1^\circ$ and $\ell = 118^\circ$, $b = 2^\circ$. These were chosen for the following reasons:

(i) In principle, RVs measured at $\ell = 118^\circ$ should sample strong shear in Galactic rotation and hence provide stronger insight into how the rotation changes with Galactocentric radius outside the Solar Circle. This particular sightline is also one that presents relatively low total extinction (Sale et al. 2014) and limited CO emission (Dame, Hartmann & Thaddeus 2001), thereby promising access to greater distances. It is consistent with these properties that there is a raised stellar density visible at this location of up to twice the average for the region (see Farnhill et al. 2016). This pencil beam most likely misses the main Perseus spiral arm, since the main belt of extinction and CO emission lies at higher latitudes than our chosen pointing by one to two degrees. It is worth noting that the necessarily sparse H II region data used by Brand & Blitz (1993) to measure the outer-disc rotation curve revealed little change in apparent RV with distance in this location: all values cluster around an LSR value of -50 km s⁻¹. Russeil (2003) reported a departure of -21 ± 10.3 km s⁻¹ from mean circular speed associated with the Perseus Arm.

(ii) Sightlines near the Galactic anticentre intersect the direction of dominant circular motion essentially at right angles, leading to the expectation of measured RVs close to 0 (in the LSR frame) exhibiting negligible change with increasing distance. We chose to observe an anticentre sightline so that it serves as a control directly revealing e.g. RV measurement bias and the magnitude of kinematic scatter. Again, the particular choice made is of a pencil beam that is subject to relatively light extinction. At $\ell = 178^\circ$, higher extinction is found a degree away, on and below the Galactic equator.

The targets we observed have magnitudes spanning the range, $14.2 \leq i \leq 18.5$, which are expected to populate a heliocentric distance range of approximately 2–10 kpc.

The sample was selected using the IPHAS $r - i$, $r - H\alpha$ colour-colour diagram, as shown in Fig. 1. Drew et al. (2008) described how this colour-colour diagram can be used to effectively select samples of near-main-sequence early-A stars. The candidate A stars were selected from a strip 0.04 mag wide, just above the early-A reddening line shown in Fig. 1, and the candidate F stars were selected from a strip 0.08–0.09 mag above the same line. The use of both F and A stars ensure the heliocentric distance distribution is well sampled, as the selected F stars will lie closer on average than the intrinsically brighter A stars.

¹ PPMXL (Roeser, Demleitner & Schilbach 2010) is a catalogue of positions and proper motions referred to the ICRS (International Celestial Reference System).

² LAMOST Spectroscopic Survey of the Galactic Anticentre (Xiang et al. 2017). LAMOST is the Large Sky Area Multi-Object Fibre Spectroscopic Telescope.

³ The Apache Point Observatory Galactic Evolution Experiment (DR12 release; see Alam et al. 2015).

⁴ Isaac Newton Telescope.

⁵ WHT (William Herschel Telescope) Enhanced Area Velocity Explorer (Dalton et al. 2016).

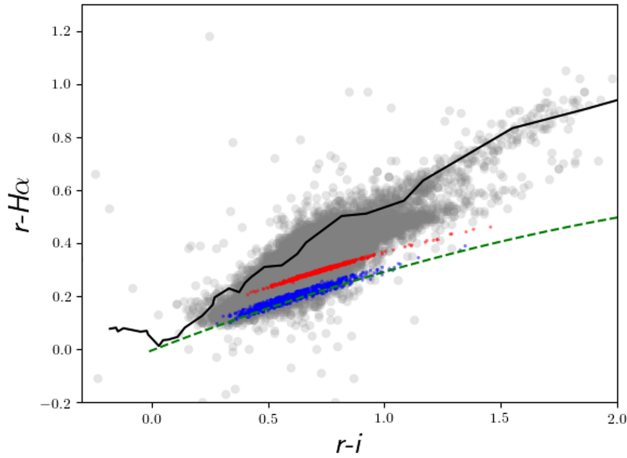


Figure 1. IPHAS colour–colour diagram with HectoSpec targets overlaid. The grey points are IPHAS sources with $r < 19$. The HectoSpec stars fall in two distinct selection strips: the top strip selecting F-type stars (red points) and the bottom strip selecting A-type stars (blue points). The black line is an empirical unreddened main-sequence track, and the green dashed line is the early-A reddening line.

2.2 Observations and selection of data for analysis

The spectra were gathered using the MMT’s multi-object spectrograph, HectoSpec (Fabricant et al. 2005), with the 600 lines mm^{-1} grating providing $\sim 2.4 \text{ \AA}$ resolution as measured from narrow sky lines. The observations were performed over six nights in 2011 September to November and cover a wavelength range of 6532–9045 \AA with a sampling of 0.56 \AA . Table 1 details the observations on each date, giving the i magnitude range targeted, exposure time, achieved count range, and number of targets.

The HectoSpec data were reduced using the HSRED⁶ pipeline, and a mean sky spectrum is determined using dedicated sky fibres. This is subtracted off all target fibres in the same configuration. An example of a sky-subtracted spectrum of an A star (blue line) and its corresponding sky spectrum (orange line) can be seen in Fig. 2. The wavelength range shown (8470–8940 \AA) is the region we use for measuring RVs and stellar parameters. Whilst much smaller than the total range covered by the data, it is chosen as it covers the CaT lines and some prominent Paschen lines. It is also relatively unaffected by telluric absorption lines. The only other strong photospheric feature potentially available to us is $H\alpha$, which is very far away in wavelength, and close to the blue limit of the MMT spectra. The region between the red dashed lines in Fig. 2 is excluded from further analysis since it is particularly dominated by bands of telluric emission which have proved difficult to subtract cleanly in many cases. The region also excludes the diffuse interstellar band at 8620 \AA .

A quality cut was applied to the data, accepting spectra with an average count level of more than 2000 (between 8475 and 8675 \AA), to ensure a large enough signal-to-noise ratio (S/N) for reliable RV and stellar parameter measurements. The wavelength-averaged minimum S/N corresponding to this is 23. There are 887 spectra at $\ell = 118^\circ$ and 434 spectra at $\ell = 178^\circ$ that survive this cut. Fig. 3 shows the count levels versus apparent i magnitude, with the horizontal line representing the minimum accepted count level. The distinct trends are due to weather, varying levels of moonlight, and

exposure time changes (see Table 1). The configurations exposed on 19-09-2011 and 18-11-2011, both for targets with $i \leq 16.5$, present contrasting count levels due to a significant transparency change. The effective magnitude faint limit is $i \sim 17.5$ –18.

HectoSpec spectra that show signs of red-leak contamination are betrayed by an upturn in the continuum at the red end reversing the decline seen shortward of $\sim 8600 \text{ \AA}$. These spectra are removed from the sample, leaving 855 target spectra in the $\ell = 118^\circ$ sightline and 409 in the $\ell = 178^\circ$ sightline.

3 ANALYSIS OF SPECTRA

3.1 Spectral fitting process

3.1.1 Overview

RVs and the stellar parameters (effective temperature, T_{eff} , surface gravity, $\log g$, and rotational velocity, $v \sin i$) were measured using Markov Chain Monte Carlo (MCMC) full-parameter fits over the CaT range (8470–8940 \AA). The target spectra are compared with a template set, interpolated as needed, by mapping the templates directly on to the observations and hence eliminating the need for separate continuum fitting to both the template spectrum and target spectrum.

The alternative method of RV measurement by cross-correlation was also explored. Each target spectrum was cross-correlated with every template, and the stellar parameters were adopted from the template which produced the tallest cross-correlation function peak. However, a significant weakness of this method is that it does not lend itself easily to error propagation. Consequently, the MCMC method has been favoured. The RV measurements for both methods are in agreement within the errors, with a slight bias to more negative values in the case of cross-correlation. The median difference between MCMC and cross-correlation RV measurements is 2.0 km s^{-1} – an amount that falls inside the median RV error estimate of $\sim 4.4/6.8 \text{ km s}^{-1}$ for F stars/A stars.

3.1.2 Template spectra

In order to determine the needed quantities from the target spectra obtained, comparisons need to be made with a set of synthetic spectra. These synthetic spectra were calculated using the approach of Gebran et al. (2016) and Palacios et al. (2010). These authors have used SYNPEC48 (Hubeny & Lanz 1992) to calculate the spectra based on ATLAS9 model atmospheres (Kurucz 1992), which assume local thermodynamic equilibrium, plane parallel geometry, and radiative and hydrostatic equilibrium. We collected 735 spectra that sample the parameter domain as follows:

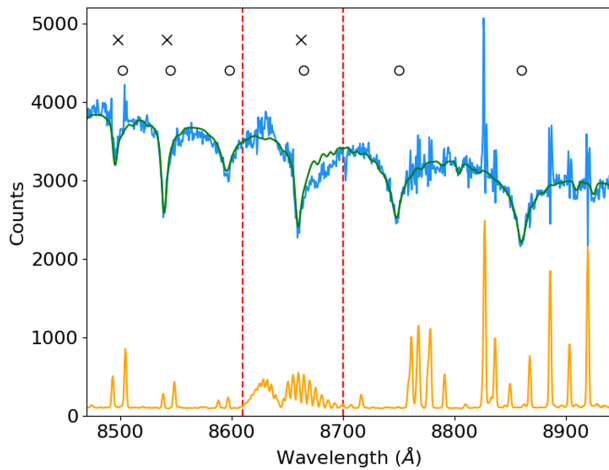
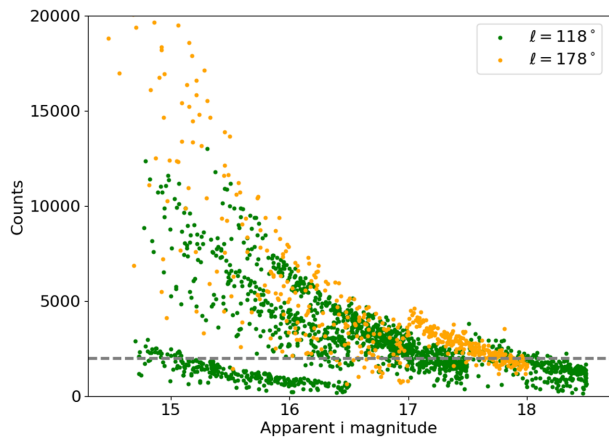
- (i) $[\text{Fe}/\text{H}] = 0, -0.5$
- (ii) $[\alpha/\text{Fe}] = 0$
- (iii) $5000 \leq T_{\text{eff}} \text{ (K)} \leq 15000$, in steps of 500 K
- (iv) $3.0 \leq \log g \leq 5.0$, in steps of 0.5
- (v) $0 \leq v \sin i \text{ (km s}^{-1}\text{)} \leq 300 \text{ km s}^{-1}$, in steps of 50 km s^{-1} .

The metallicity is not treated as a free parameter: instead we use two distinct template sets, one with $[\text{Fe}/\text{H}] = 0$ and the other $[\text{Fe}/\text{H}] = -0.5$, and compare the results. We do this because of the limited spectral coverage and resolution of our data. Our numerical trials of metallicity as a free parameter showed it to be underconstrained and prone to interfere with the descent on to the values of other parameters. Nevertheless, there is an expectation that with increasing heliocentric distance along both pencil beams, there

⁶Information on the latest version of HSRED can be found at <https://www.mmt.org/node/536>

Table 1. The details of the observations: date of observation, i magnitude range targeted, exposure time, achieved count range, number of targets observed, and Galactic longitude of sightline.

Date of observation	i magnitude	Exposure (min)	Count range	Number of spectra	ℓ ($^\circ$)
17-09-2011	16.5–17.5	140	390–5163	266	118 $^\circ$
18-09-2011	16.5–17.5	135	1000–4012	259	
19-09-2011 (a)	≤ 16.5	75	204–2983	258	
19-09-2011 (b)	17.5–18.5	265	143–2843	264	
21-10-2011	≤ 17.5	135	869–13 003	256	
18-11-2011 (a)	≤ 16.5	75	1452–12 352	253	
17-11-2011	≤ 18	165	1192–4607	252	178 $^\circ$
18-11-2011 (b)	≤ 17.5	120	662–41 194	262	

**Figure 2.** Close-up of the CaT region in the spectrum of an A star from the HectoSpec data set (blue) and the corresponding sky spectrum (orange). The latter has been scaled down to 15 percent of the original counts. The region between the red dashed lines is excluded from the MCMC full-parameter fitting procedure since this region is affected by sky lines that frequently do not subtract well. The green line is the MCMC template fit. The narrow emission-like features in the star spectrum are incompletely subtracted sky lines. The prominent \sim triangular absorption lines are Paschen lines, indicated by a circle. In later type stars, the CaT lines, indicated by a cross at 8498, 8542, and 8662 Å become obvious, strengthening as the Paschen lines fade.**Figure 3.** Count level versus apparent i magnitude for $\ell = 118^\circ$ (green) and $\ell = 178^\circ$ (orange). The grey dashed line represents the minimum accepted count level of 2000. There are 749 stars with counts < 2000 , and 1321 with counts ≥ 2000 .

is likely to be a gradual decline in metallicity. Friel et al. (2002), Chen, Hou & Wang (2003) and Rolleston et al. (2000) found the metallicity gradient in the Milky Way to be ~ -0.06 dex kpc^{-1} . At the median distances for the targets in each sightline, $R_G \sim 11$ kpc for $\ell = 118^\circ$ and $R_G \sim 13$ kpc for $\ell = 178^\circ$, this corresponds to $[\text{Fe}/\text{H}] \sim -0.18$ and $[\text{Fe}/\text{H}] \sim -0.29$, respectively. In contrast, Twarog, Ashman & Anthony-Twarog (1997) and Yong, Carney & Teixeira de Almeida (2005) found $[\text{Fe}/\text{H}] = -0.5$ at $R_G \geq 10$ kpc. Hence, it is appropriate to gauge the effect of modest changes in adopted metallicity.

The model spectra have a resolution of $R = 10000$, cover 3600–9650 Å and have a constant wavelength sampling of 0.05 Å. However, for this work, the templates have been broadened with a Gaussian filter to match the resolution of the target spectra and rebinned to a sampling of 0.56 Å (also to match the data).

3.1.3 MCMC-assisted full-parameter fitting

The parameters of astrophysical interest that we need to derive from each spectrum are T_{eff} , $\log g$, $v \sin i$, and RV. The first step in this process has to be a mapping of template spectra on to each observed spectrum. The mapping function we have adopted is linear which we find to be an adequate approximation over the short wavelength range considered. This introduces two extra free parameters to be fit: the gradient and the intercept of the mapping function. This approach is preferred over the alternative of separate continuum fits to the template and observed spectra because it is then possible to monitor how the mapping numerically influences the outcome.

The posterior probability distributions of the six free parameters (T_{eff} , $\log g$, $v \sin i$, RV, normalization gradient, and intercept) are obtained assuming a likelihood function of the form:

$$\mathcal{L}(\mu, \sigma^2; x_1, \dots, x_n) \propto e^{-\frac{1}{\alpha} \sum_i \frac{(x_i - \mu_i)^2}{2\sigma_i^2}}, \quad (1)$$

where x refers to the target star spectrum sampled at pixels $i = 1 \dots n$ and μ refers to the template spectrum. Since the pixels in a resolution element are not independent, we compensate by dividing the summation by the number of pixels per resolution element, α . This is 4.3 in our case. σ_i is the noise level of the target star at pixel i , given by

$$\sigma_i = \sqrt{\sigma_{\text{sky}+\text{star},i}^2 + \sigma_{\text{sky},i}^2}, \quad (2)$$

where $\sigma_{\text{sky}+\text{star},i}^2$ is the count level of the raw spectrum (the sky and star together), and $\sigma_{\text{sky},i}^2$ is the count level of the sky spectrum. This likelihood function assumes the target spectrum has Gaussian errors.

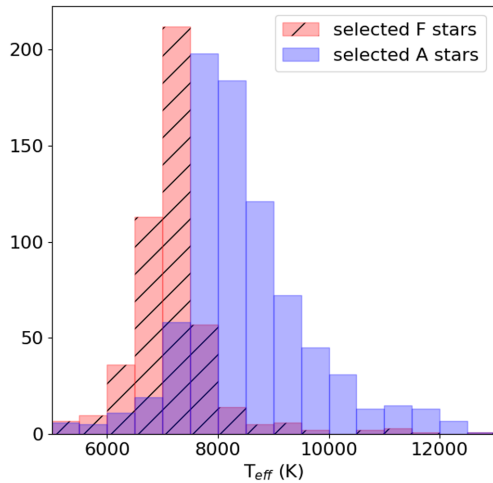


Figure 4. Superposed distributions of measured T_{eff} values (for both sightlines combined) of stars selected as probably F type (red histogram) and A type (blue histogram). Of the stars initially selected as A type, only 12 per cent are cooler F/G stars.

By linearly interpolating the template grid, templates with intermediate parameter values are produced and hence the model parameter space is continuous. The RV range is sampled by shifting the wavelength axis of the template according to the Doppler formula.

The ‘EMCEE’ PYTHON package (Foreman-Mackey et al. 2013) is used to execute the MCMC parameter space exploration. Our procedure is set up for 200 ‘walkers’. The priors used are flat for all parameters, with the range available to each parameter matching the range in the template set. The range of the RV prior covers all realistic values ($\pm 500 \text{ km s}^{-1}$). The slope and intercept of the function mapping the template on to the target spectrum are nuisance parameters, for which the range on the prior was determined by experimentation with the data set. After many steps, the walkers converge (we use 2000 steps with a 700 step burn-in) and the distribution of parameter values returned by them define the posterior probability distribution of the parameters. These are typically of the form of a 2D Gaussian. The medians of the marginalized distributions are adopted as the best estimates of parameter values and the uncertainties are based on the 16th and 84th percentiles. Fig. 2 shows an example of a template (green line) with best-estimate parameters for the observed spectrum (blue line).

3.2 Derived stellar parameters

3.2.1 T_{eff}

The measured T_{eff} distribution for both sightlines combined can be seen in Fig. 4. The red bars represent the stars originally selected from the IPHAS $r - i$, $r - H\alpha$ colour–colour diagram as F stars, and the blue bars represent the A stars. 78 per cent of the stars selected as candidate F stars have measured T_{eff} values of 6000–7500 K (typical of F stars), and 81 per cent of the candidate A stars have T_{eff} values of 7500–10 000 K (typical of A stars). It is necessary to point out that the template set spans temperatures inclusive of G stars ($T_{\text{eff}} \leq 6000 \text{ K}$) and B stars ($T_{\text{eff}} > 10 000 \text{ K}$). Stars measured as G stars make up only 2 per cent of the total sample and B stars 4 per cent. These are mainly stars that have contaminated the selected IPHAS $r - i$, $r - H\alpha$ regions. Given the modest levels of contamination (e.g. only 12 per cent of the initial A-star selection turned out to be

cooler than 7500 K), the method of selection is shown to be very effective and practically viable. For simplicity in the remainder of the paper, we label stars as either F or A type, with $T_{\text{eff}} = 7500 \text{ K}$ as the boundary dividing them.

The positive and negative errors in T_{eff} as a function of T_{eff} are shown in the top panel of Fig. 5. The median of the positive and absolute values of the negative errors combined is $\sim 150 \text{ K}$; however, the average error increases with temperature and there are a number of targets that have large asymmetric errors, betraying an unresolved fit dilemma. As temperature increases, the Paschen line depths increase until $T_{\text{eff}} \sim 9000 \text{ K}$, thereafter they become more shallow again. This means that there can be a degeneracy where the Paschen line profiles of a lower temperature template are similar to that of a higher temperature template, with the addition of line broadening effects from the $\log g$ and $v \sin i$ parameter. This set of stars, with large T_{eff} errors ($> 1000 \text{ K}$), consists of only 85 of the 1261 targets, and are henceforth removed from the sample. These are represented by empty circles in Fig. 5.

Finally, this leaves a total sample made up of 705 A stars ($T_{\text{eff}} > 7500 \text{ K}$) and 471 F stars ($T_{\text{eff}} \leq 7500 \text{ K}$): broken down into the sightlines, there are 473 A stars and 310 F stars in the $\ell = 118^\circ$ sample, and 232 A stars and 161 F stars in the $\ell = 178^\circ$ sample.

3.2.2 $\log g$

The middle panel of Fig. 5 shows the positive and negative errors in $\log g$ from the posterior distributions as a function of T_{eff} , for the A and F stars at solar metallicity. It is clear from the figure that the formal $\log g$ error rises steadily with decreasing effective temperature. The median error at $T_{\text{eff}} > 7500 \text{ K}$ is 0.09, while below this it increases to 0.14. This trend most likely tracks the growing importance of H^- continuum opacity with decreasing effective temperature, causing the wings of the CaT lines to become less sensitive to surface gravity. Gray & Corbally (2009) have noted a ‘dead zone’ among mid-late F stars in which dwarf and giant spectra are nearly indistinguishable.

In F stars with appreciably reduced Paschen line profiles, in particular, this underlying astrophysical trend is compounded to an extent by the moderate spectral resolution of the data. We find for these cooler stars that the fits begin to exhibit a three-way degeneracy for combinations of temperature, gravity, and metallicity. An example of this degeneracy at work in the CaT in cooler F stars was presented by Smith & Drake (1987). However, with metallicity fixed, it is possible to identify temperature and gravity albeit with greater error on the latter. The returned F-star $\log g$ distribution is skewed strongly in favour of near-MS objects, with a median value of 4.5 and interquartile range 4.1–4.8, tapering off into a tail reaching down to one object with $\log g \simeq 3.0$ (the lower bound on the template set).

The distribution of best-fitting $\log g$ values for the A stars can be seen in Fig. 6. The peak of the distribution lies close to where we would expect it to be. Also shown is the distribution of $\log g$ for A stars from a Besançon model (Robin et al. 2003) for $\ell = 118^\circ$, after convolving with a Gaussian of $\sigma = 0.09$ to emulate the HectoSpec measurement error, for a more useful comparison. The measured HectoSpec distribution has a tail at large values of $\log g$ that is not seen in the Besançon model, and its peak is not perfectly matched. A shift of the Besançon distribution of +0.15 brings the two distributions into rough alignment. This could be evidence of a bias in our measurements. We appraise the impact of this in Section 5.2.

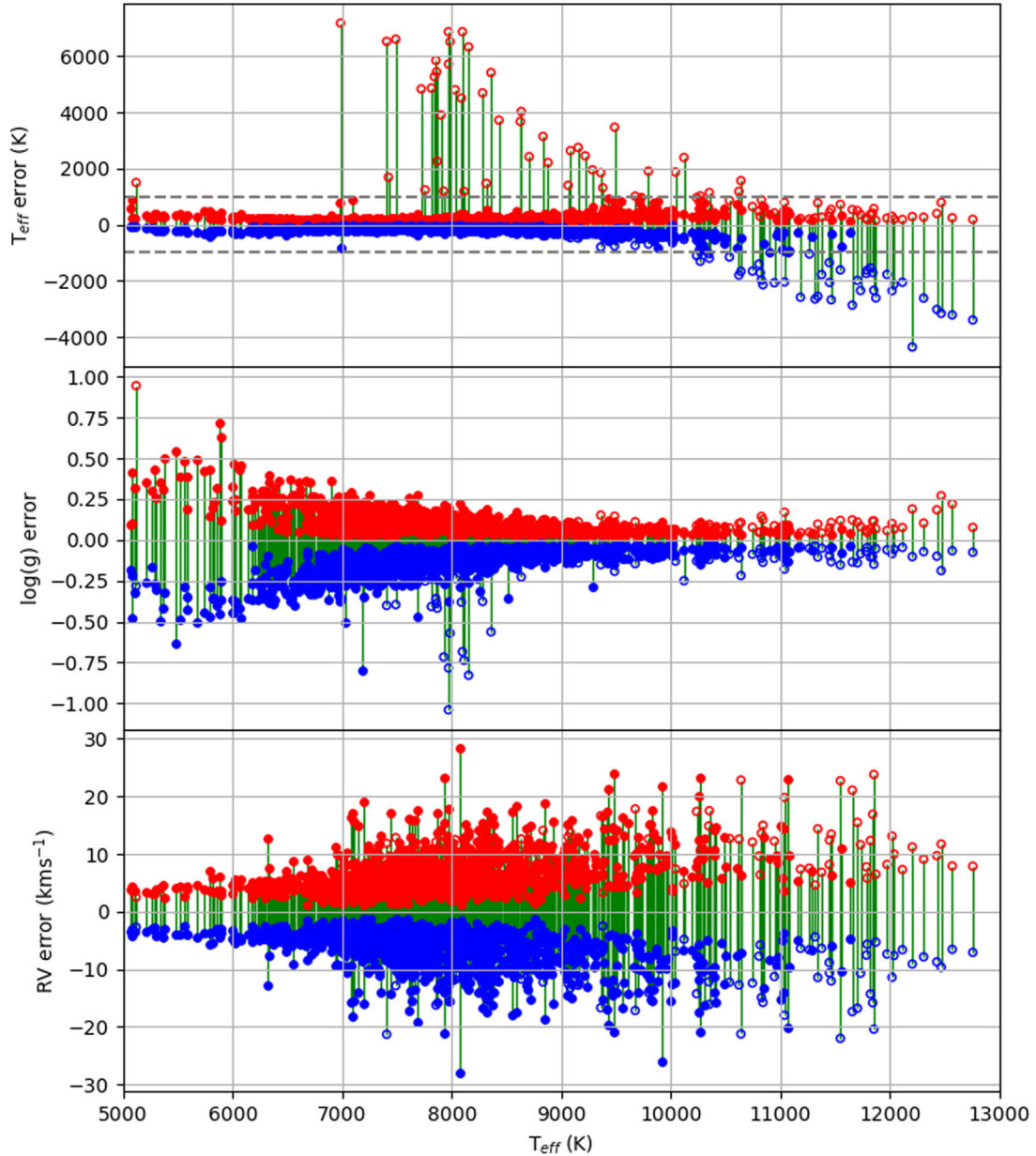


Figure 5. Positive (red) and negative (blue) errors in T_{eff} (top panel), $\log g$ (middle panel) and RV (bottom panel) as a function of T_{eff} . The grey dashed lines in the top panel represent the T_{eff} error cut: points with $|\text{error}| > 1000$ K that are removed from the sample are shown in this figure, represented by empty circles. The green bars connect the positive and negative errors for each individual target.

The stars occupying the high-end tail, which appears more extended than in the Besançon model distribution, are mainly cooler objects carrying larger-than-median errors (see Fig. 5).

3.2.3 $v \sin i$

Fig. 7 shows the measured $v \sin i$ distribution for both sightlines combined, separated into F stars (red bars) and A stars (blue bars). The distribution is as expected, with generally low values for F stars and a spread from low to high values for A stars (Royer 2014). The median error on $v \sin i$ is $\sim 20 \text{ km s}^{-1}$, increasing to $\sim 40 \text{ km s}^{-1}$ for $T_{\text{eff}} > 10000 \text{ K}$ – as expected for stars that are more commonly fast rotators. Unsurprisingly, there is evidence of a slight negative correlation between individual $\log g$ and $v \sin i$ parameter fits.

3.2.4 RV

Fig. 5 shows the errors on RV as a function of T_{eff} . The median error is $\sim 4.4 \text{ km s}^{-1}$ for F stars and $\sim 6.8 \text{ km s}^{-1}$ for A stars. This difference is attributable to the growing contrast of the CaT lines with decreasing effective temperature. The solar motion needed to convert from the heliocentric to the LSR frame is taken as $(U, V, W) = (-11, +12, +7) \text{ km s}^{-1}$ (Schönrich, Binney & Dehnen 2010).

3.3 A comparison with higher resolution long-slit spectra

As a check on the reliability of the derived parameters and their errors, we obtained additional long-slit red and blue spectra for seven HectoSpec targets – the positions and apparent i magnitudes

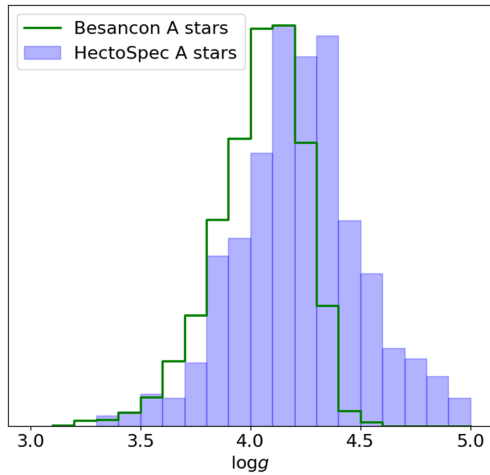


Figure 6. Distribution of measured $\log g$ values of A stars for both sightlines combined (blue histogram). The distribution of $\log g$ values of A stars from a Besançon model for $\ell = 118^\circ$ is also shown (green histogram). This has been convolved with a Gaussian of $\sigma = 0.09$ to emulate the HectoSpec measurement error.

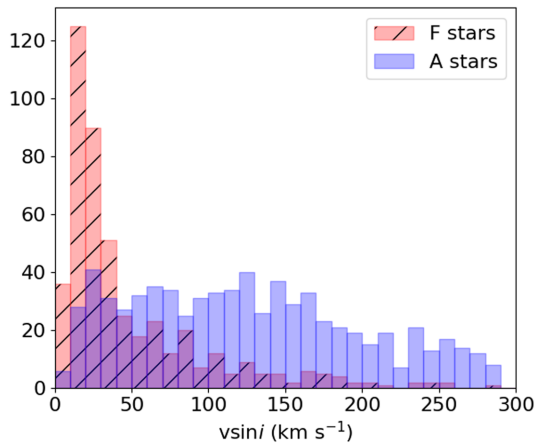


Figure 7. The distributions of measured $v \sin i$ values, separated into F stars (red) and A stars (blue), and shown overplotted. The two lines of sight are merged within each distribution.

Table 2. Positions and apparent i magnitudes of the objects used for the HectoSpec-ISIS comparison.

Target	RA	Dec.	i mag	ISIS red T_{eff} (K)
1	00:03:41	64:29:43	14.94	$7665 \pm_{101}^{115}$
2	00:06:36	64:22:38	14.89	$7703 \pm_{73}^{76}$
3	00:03:47	64:17:12	14.77	$7769 \pm_{95}^{89}$
4	00:07:37	64:07:51	14.78	$8331 \pm_{219}^{2957}$
5	00:05:36	63:57:55	14.84	$11\,043 \pm_{1332}^{344}$
6	00:04:02	64:29:49	14.91	$11\,299 \pm_{1710}^{158}$
7	00:07:13	64:46:18	14.82	$11\,370 \pm_{378}^{202}$

of which are shown in Table 2. These were accompanied by five RV standard stars (with three observed more than once). Of particular interest in this comparison are the measured surface gravities and RVs. The seven objects reobserved are spread in $\log g$ from 3.5 to 4.5, as determined from the HectoSpec data, lying across the peak of the distribution in Fig. 6. The T_{eff} range, again determined

from the HectoSpec data, spans $\sim 7900\text{--}9500$ K, with one object outside this range with $\sim 11\,900 \pm_{2600}^{150}$ K – the large error indicating the unresolved fit dilemma described in Section 3.2.1.

These spectra were gathered as service observations using the Intermediate-dispersion Spectrograph and Imaging System (ISIS) of the 4.2-m William Herschel Telescope during three nights in 2016 October to December. ISIS is a high-efficiency, double-armed, medium-resolution ($8\text{--}121 \text{ \AA mm}^{-1}$) spectrograph. The R1200B grating was used on the blue arm, and the R1200R grating on the red arm, providing resolution elements for a 1 arcsec slit of 0.85 and 0.75 \AA , respectively. The wavelength coverage of the blue spectra is 3800–4740 \AA and of the red spectra is 8110–9120 \AA . Both the blue and red spectra have a constant wavelength sampling of 0.22 and 0.24 \AA , respectively.

The raw images were processed and sky-subtracted and the resultant spectra was wavelength calibrated, all with use of the Image Reduction and Analysis Facility (IRAF). The spectra were then passed through the MCMC full-parameter fitting method. For the red spectra, the same wavelength limits were adopted as for HectoSpec, and for the blue the wavelength range used was 4000–4600 \AA , covering some of the Balmer series whilst excluding the Ca II K and H lines since they suffer from interstellar absorption. The measured parameters and RV were then compared to those measured from the HectoSpec spectra, or to values from the literature in the case of the RV standards, to reveal any systematic differences. A method check was performed by comparing the measured parameters from the red and blue ISIS spectra, eliminating the potential for differences due to a change of instrument. The weighted mean difference between measured RV for the ISIS RV standard stars and RV from the literature is -0.7 km s^{-1} for the blue spectra and $+0.1 \text{ km s}^{-1}$ for the red spectra. Hence, we are confident that the ISIS wavelength scale is reliable.

Fig. 8 shows the difference between the ISIS measurements (blue points for blue spectra and red points for red spectra) and the HectoSpec measurements. The targets are in ascending order of T_{eff} , as determined from the ISIS red spectra. In general, the differences in outcome are reassuringly modest and show the method is working satisfactorily. The dashed lines represent the weighted mean difference between the ISIS red and HectoSpec measurements (red line) and ISIS blue and HectoSpec measurements (blue line). The weighted mean difference between the red ISIS and HectoSpec measurements, and the standard deviation of the spread, are: $\Delta T_{\text{eff}} = -215 \pm 1335 \text{ K}$, $\Delta \log g = -0.36 \pm 0.18$, $\Delta v \sin i = -24 \pm 53 \text{ km s}^{-1}$ and $\Delta RV = -1.9 \pm 3.5 \text{ km s}^{-1}$. The small mean difference in measured RV indicates the HectoSpec wavelength calibration is systematically offset by an amount well below measured random errors. The larger difference in $\log g$ suggests that there may be a bias towards larger values in the HectoSpec data. This potential bias is not the first evidence: the comparison between our A-star $\log g$ distribution and that from a Besançon model is shown in Section 3.2.2 and we see the HectoSpec distribution peaks at a slightly larger value. We return to the impact of this possible bias in Section 5.2.

The blue data points in Fig. 8 provide the comparison between the ISIS blue and HectoSpec data. The weighted mean offsets and standard deviations obtained are: $\Delta T_{\text{eff}} = -289 \pm 1017 \text{ K}$, $\Delta \log g = -0.43 \pm 0.32$, $\Delta v \sin i = -18 \pm 63 \text{ km s}^{-1}$ and $\Delta RV = -7.7 \pm 8.8 \text{ km s}^{-1}$. As with the red, there is a sizable offset in $\log g$, suggesting the HectoSpec data may carry a positive bias. The RV difference is larger than that measured for the red spectra, potentially as a result of the fewer absorption lines fitted in the blue region and hence lower accuracy.

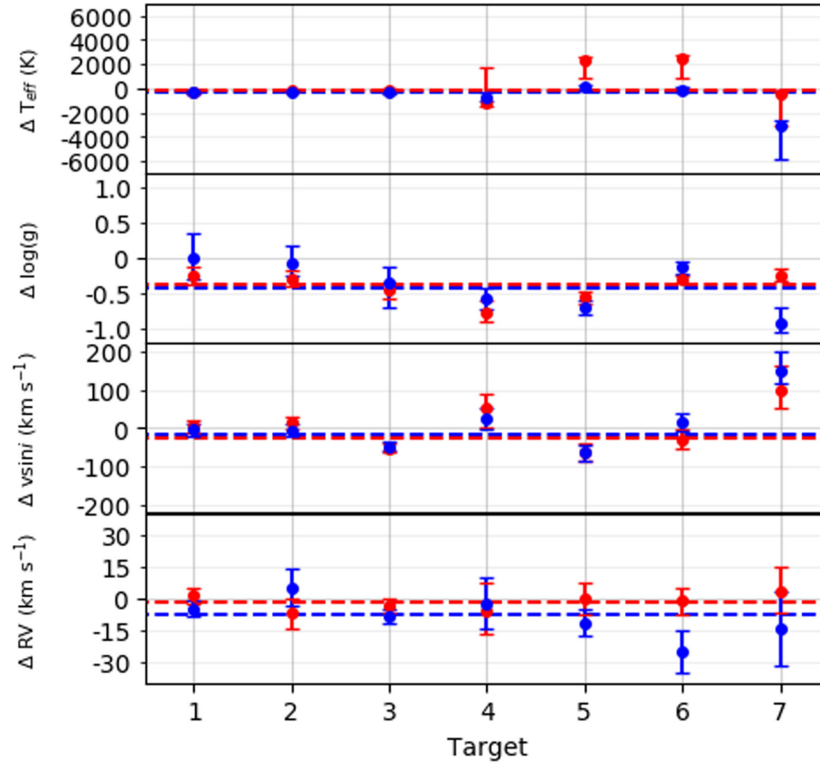


Figure 8. Differences between ISIS and HectoSpec measured stellar parameters. The blue points represent the differences between measurements from the blue ISIS and HectoSpec spectra, and the red points specify differences between the red ISIS and HectoSpec spectra. The targets are in ascending order of T_{eff} , as determined from the ISIS red spectra. The error shown on each data point is the quadratic sum of the HectoSpec error and ISIS error. The dashed lines represent the weighted mean difference between the ISIS red and HectoSpec measurements (red line) and ISIS blue and HectoSpec measurements (blue line).

We have also reviewed the differences between parameters derived from the ISIS blue measurements and the ISIS red and HectoSpec data. Hales et al. (2009) performed a similar comparison between the red and blue ranges as observed with ISIS, and found a tendency for the red determined spectral type to be earlier by 0.9 subtypes. They attributed this to strengthening of the Ca II H and K absorption lines by an interstellar component. Although we exclude these lines in the fitting procedure, we find a modest offset in effective temperature, with the red suggesting a slightly hotter star of 112 K with very little change in surface gravity (0.02 dex).

The comparison with higher resolution spectra has provided useful insights – the offsets between the ISIS and Hectospec measurements are reassuringly modest and are similar to those expected due to random errors. Our employed method is working well. The larger offset in the derived surface gravities suggest a bias could be present to which we will continue to pay attention.

3.4 Extinction, absolute magnitudes, and distance moduli

The distance modulus, μ , of each star is calculated via the following equation

$$\mu = m_i - A_i - M_i, \quad (3)$$

where m_i is the apparent magnitude in the i band, A_i is the extinction, and M_i is the absolute magnitude. The absolute magnitudes used are from Padova isochrones, interpolated with T_{eff} and $\log g$ scales (Bressan et al. 2012; Chen et al. 2015). We choose a value for M_i on the basis of the median $\log g$ and T_{eff} returned by the fits. Where $\log g$ exceeds the maximum present in the Padova isochrones for the specified T_{eff} , we reset $\log g$ to this value. The median error on

the absolute magnitudes (due to stellar parameter uncertainties) is ~ 0.3 . This is the dominant error source in our final results.

The extinction of each target was calculated using

$$A_i = 2.5[(r - i)_{\text{obs}} - (r - i)_{\text{int}}], \quad (4)$$

where $(r - i)_{\text{obs}}$ is the observed colour of the star, taken from IPHAS photometry, and $(r - i)_{\text{int}}$ is the intrinsic colour of the star. The intrinsic colours are calculated from the template grid via synthetic photometry and the value for each target star is interpolated on this grid based on the measured T_{eff} and $\log g$. The coefficient of 2.5 is the ratio of A_r to A_i for main-sequence A/F stars with reddening levels similar to the HectoSpec data. We use the Fitzpatrick law with $R_V = 3.1$. The median error on intrinsic colour (due to stellar parameter uncertainties) is ~ 0.01 , and on A_i (due to stellar parameter and photometric uncertainties) is ~ 0.05 . After dereddening the observed magnitudes, μ is obtained: across the entire sample the interquartile range for the error in μ is 0.2–0.4. The smallest errors are associated with early A stars (median error ~ 0.2).

Fig. 9 shows the A_i extinctions as a function of estimated distance modulus for both sightlines. Also shown are the mean extinction trends due to Sale et al. (2014) across the two pencil beams, including the expected dispersion in extinction (grey-shaded region). This comparison provides some insight into the plausibility of the distance modulus distribution of our sample. An important difference to be aware of is that the Sale et al. (2014) trends were computed from IPHAS photometry of all probable A–K stars, down to apparent magnitudes that are appreciably fainter (to $i \sim 20$) than those typical of our analysed spectra ($i < 18$). In both sightlines, there is evidence that the spectroscopic samples favour lower extinctions

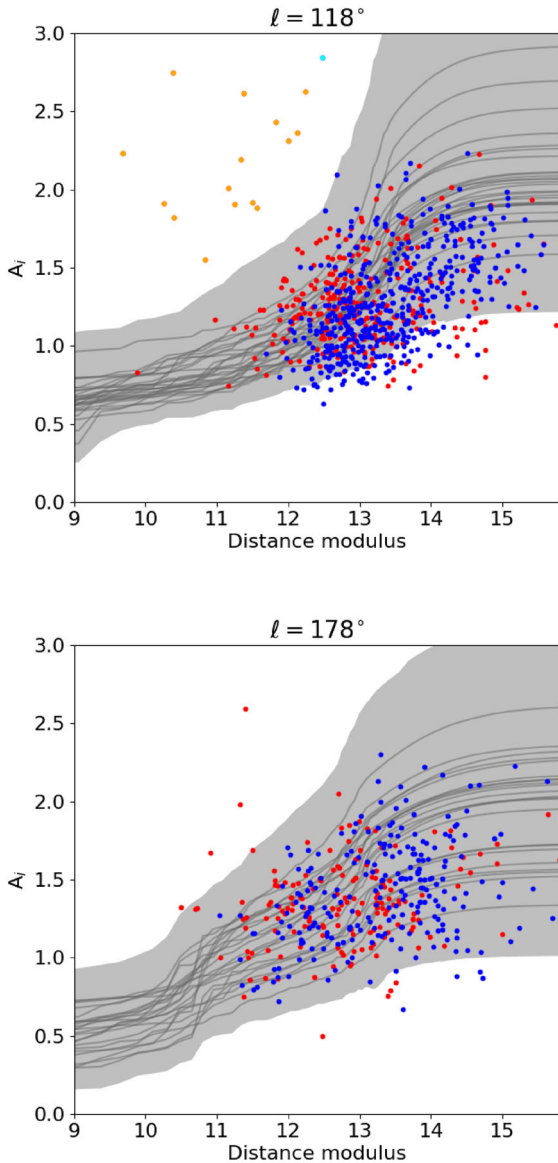


Figure 9. The extinction, A_i , of F stars (red points) and A stars (blue points) as a function of distance modulus. Top: $\ell = 118^\circ$, bottom: $\ell = 178^\circ$. Also shown in each panel are the photometrically predicted mean extinction trends (grey lines) across the pencil beam (Sale et al. 2014). The grey shaded region defines the expected dispersion in extinction at every distance within the beam. Stars that lie far from the trend in the upper panel are highlighted by a change of colour – orange for the F stars and cyan for one A star. This colouring is preserved in Fig. 11.

than the fainter-weighted photometrically based trends. This is most likely a straightforward selection effect.

To check this, we have examined the impact of the counts cut we placed on the spectra included in the analysis: specifically, we have compared median estimates of extinction, derived from their $r - i$ colour, for the stars analysed (counts >2000), with those for lower count stars not analysed. We find that for both directions the cut biases the typical extinction of the A stars (inferred from the available $r - i$ colours) to lower values: the strength of effect is that the unanalysed objects have a median A_i that is greater by 0.4 mag. This helps explain the tendency for the blue A-star data points, particularly, to sit lower in Fig. 9. Among the cooler, on-the-whole

closer, F stars there is little difference. The alternative explanation for this – overlarge distance moduli – runs into difficulty when it is recalled that there may be systematic overestimation of surface gravities (see Sections 3.2.2 and 3.3). We view this comparison as tensioning against accepting and correcting for such a bias in $\log g$, as this would drive up the distance moduli, creating a yet bigger offset.

3.5 The effect of metallicity

So far all the parameters obtained and described have been computed for solar metallicity.

Stellar parameters and RVs have been measured again, as described in Section 3.1.3, but with $[\text{Fe}/\text{H}]$ set to -0.5 for the A stars. A new Padova absolute magnitude scale, suitable for the changed metallicity, was used for determining distance moduli. The reduced-metallicity fits typically return cooler temperatures ($\Delta T_{\text{eff}} \sim -400$ K). The $\log g$ values are also lower ($\Delta \log g \sim -0.17$), partly compensating for the cooler temperatures in the estimation of distance. The net effect on the distance modulus scale is a small increase compared with the solar metallicity scale ($\Delta \mu \sim +0.12$). The RVs measured adopting $[\text{Fe}/\text{H}] = -0.5$ are slightly more negative: the median difference is ~ -3.0 km s $^{-1}$.

In the case of the F stars, there is a growing degeneracy between T_{eff} , $\log g$, and metallicity (see Section 3.2.2). In a trial of $[\text{Fe}/\text{H}] = -0.5$ in fitting the F stars, we found the returned gravities to be unrealistically low for a population of objects that is more localized than the A stars whilst sharing the same faint magnitude limit. Moreover, it is highly improbable that many among the F-star sample would present $[\text{Fe}/\text{H}]$ significantly less than 0, since the great majority of these fainter objects should lie within a distance of 5 kpc. We estimate this limiting radius for the case of a warmer main-sequence F star with $T_{\text{eff}} = 7000$ K, $i = 17.5$ (see Fig. 3), $A_i \sim 1.3$ (typical HectoSpec value – see Fig. 9), and $M_i = 2.6$. At $\ell = 118^\circ$, a distance of 5 kpc corresponds to a Galactocentric radius of ~ 10.6 kpc, or a metallicity change of ~ 0.2 . Consequently, throughout this paper we will fix the metallicity of the HectoSpec F stars at $[\text{Fe}/\text{H}] = 0$.

4 THE SIGHTLINE RADIAL VELOCITY TRENDS

The trend of RV with distance modulus can be compared with what we would expect to see as an averaged trend if consensus views of the Galactic rotation law apply. If all the stars move on circular orbits about the Galactic Centre, we would expect to observe a trend of RVs that are a spread (due to velocity dispersion) around a curve whose shape depends on the sightline observed, the assumed rotation curve, and LSR parameters (circular velocity and Galactocentric distance of the LSR, V_0 , and R_0). The comparisons made in this section are with a flat rotation curve with LSR parameters $R_0 = 8.3$ kpc, $V_0 = 240$ km s $^{-1}$, and with the slowly rising rotation curve derived in Brand & Blitz (1993) with their adopted parameters $R_0 = 8.5$ kpc and $V_0 = 220$ km s $^{-1}$. We begin with the results for $\ell = 178^\circ$, the control direction, where the rotational component of motion of the stars is effectively nullified.

4.1 $\ell = 178^\circ$

The trend of RV with μ for this pencil beam is shown in Fig. 10. The red dashed line shows the expected average trend based on a flat rotation curve (although at this sightline the shape of the rotation

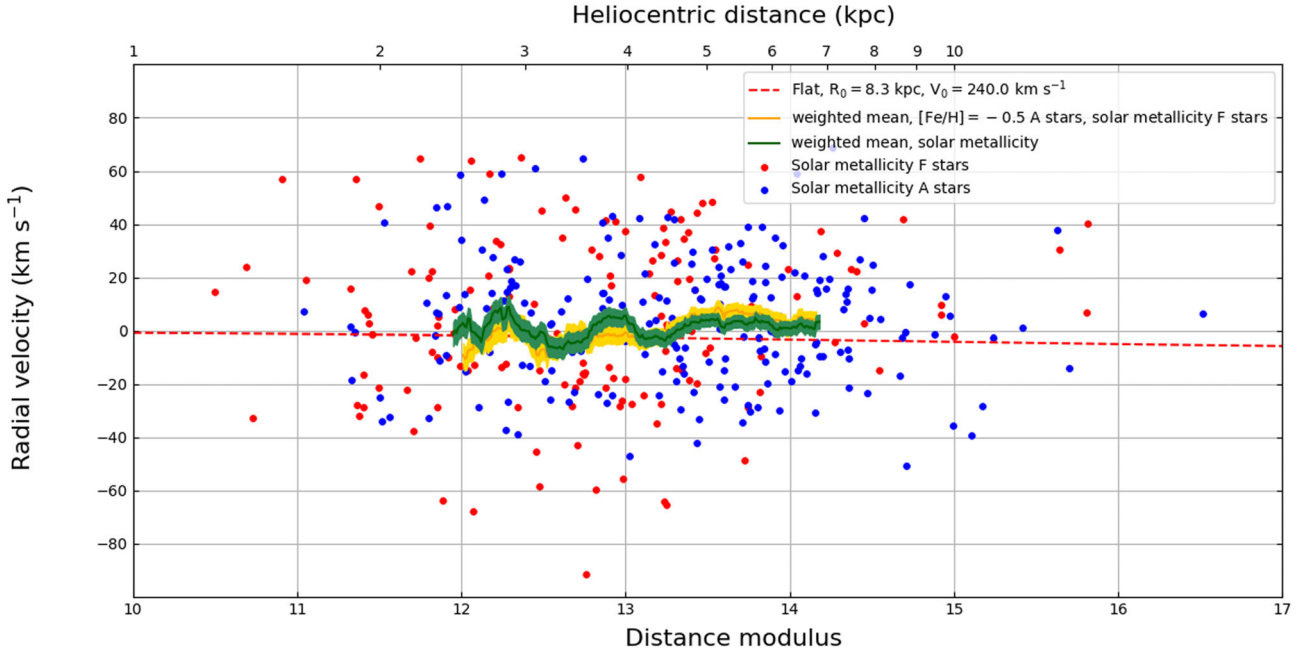


Figure 10. The trend of RVs with distance modulus for $\ell = 178^\circ$. The green line is the weighted mean of the RVs of the solar metallicity stars, and the yellow line is obtained on combining $[\text{Fe}/\text{H}] = -0.5$ A stars with solar metallicity F stars. The shaded regions represent the standard error of the mean in RV. The blue points are A stars and the red points F stars, both with metallicity assumed as solar. The red dashed line shows the expected trend for a flat rotation law, which at this sightline will fall close to \sim zero regardless of the V_0 , R_0 , or shape of the rotation law adopted.

curve makes little difference). The green line is the weighted mean of the RVs for the solar metallicity stars, plotted as individual data points, at each step in μ . The yellow line is the weighted mean for A stars with $[\text{Fe}/\text{H}] = -0.5$ and F stars with solar metallicity. The weighted RV is calculated via the following process:

- (i) Every (μ, RV) data point is assigned a normalized Gaussian error distribution with $\sigma = \sigma_\mu$, where σ_μ is the error on μ .
- (ii) At the i th step ($\mu = \mu_i$), the data points (μ_n, RV_n) with error distributions in μ overlapping μ_i are included in forming the running average, provided $|\mu_n - \mu_i| < \sigma_{\mu_n}$. The weighting per data point is in proportion to the value of its Gaussian error function at μ_i – thereby taking into account the error in μ in all data points.
- (iii) In obtaining the mean RV at $\mu = \mu_i$, the contributing RV values are also weighted in proportion to their errors.
- (iv) A final weighting is applied in computing the mean in order that the contribution from data points at $\mu < \mu_i$ balances the contribution from data points at $\mu > \mu_i$. This limits the influence of data from the most densely populated part of the μ distribution on the mean trend.
- (v) The minimum number of points required for calculation of the mean to either side of $\mu = \mu_i$ is 50.

The shaded region around the mean trend line represents its error – the standard error of mean RV at each μ_i .

In Fig. 10, the F stars dominate the lower end of the range in μ , while the A stars mostly occupy a spread from $\mu \sim 12$ to $\mu \sim 15$ (or a heliocentric distance range from 2 to 10 kpc). Of the F stars, 90 per cent (145 of 165) lie within $\mu = 11.4$ –14.5 ($d = 1.9$ –7.8 kpc). 90 per cent of the A stars with $[\text{Fe}/\text{H}] = 0$ (209 of 232) lie within $\mu = 11.8$ –14.8 ($d = 2.3$ –9.0 kpc), and 90 per cent of the A stars with $[\text{Fe}/\text{H}] = -0.5$ (130 of 144) lie within $\mu = 11.6$ –15.1 ($d = 2.1$ –10.6 kpc). Ruphy et al. (1996) found a radial cut-off of the stellar disc at $R_G = 15 \pm 2$ kpc, and Sale et al. (2010) found that the stellar density of young stars declines exponentially out to a truncation

radius of $R_G = 13 \pm 0.5_{\text{statistical}} \pm 0.6_{\text{systematic}}$ kpc, after which the stellar density declines more sharply. The density of our sample in this sightline also drops off at these distances, but at this stage we cannot be sure whether this decline originates in the Galactic disc or is a selection effect.

We find that the overall trend in RV follows the expected flat behaviour, although it is offset in velocity by a mean amount of 3.5 km s^{-1} . The results adopting $[\text{Fe}/\text{H}] = -0.5$ for the A stars are very similar as expected, but with a slightly smaller mean offset of 3.0 km s^{-1} . There was evidence of a possible small wavelength calibration offset arising from the comparison of the HectoSpec observations with independent higher resolution spectra, effecting the RV scale by only a couple of km s^{-1} , as described in Section 3.3. Taking these findings together we infer that the RV scale is reliable to within $\sim 5 \text{ km s}^{-1}$ but cannot rule out the presence of a small positive bias in the measurements.

We have computed the RV dispersion of the sample stars, in broad spectral type groups, around the measured mean trend, in order to compare them with the expected dispersions from Dehnen & Binney (1998, see Table 3)). Clearly the measured dispersions are larger than the Dehnen & Binney (1998) results. Part of this discrepancy is attributable to our measurement errors, but the larger share of it may be a consequence of stellar multiplicity. At least a half of the sample objects are likely to be members of multiple systems, and of those around 15 per cent may be in nearly equal mass ratio binaries (Duchêne & Kraus 2013). Whilst the spectroscopic resolution of our data is insufficient to pick out spectroscopic binaries, there can nevertheless be binary orbital motions present up to a level of $\sim 40 \text{ km s}^{-1}$ (depending on phase) in typical cases (for total system masses of $3M_\odot$, with period $P \sim 40$ d). As the data in Table 3 indicate, the excess dispersion on top of measurement error is in the region of 10 km s^{-1} for all three spectral type groups. We look at this in more detail in Section 5.

Table 3. Expected RV dispersion from Dehnen & Binney (1998) (σ_{DB}) compared to the measured RV dispersion (σ_{178°) for early A–early F stars (solar metallicity set). Also given are the typical HectoSpec measurement errors (ϵ_{RV}) for the different subtype ranges, and the quadrature sum in combination with σ_{DB} . Finally, the excess σ required to reconcile σ_{DB} and σ_{178° are provided. These excesses are compatible with the extra dispersion likely to be introduced by the presence of spectroscopic binaries in the sample (of the order of 10 km s^{-1}).

Stellar type	T_{eff} range	No. of stars	σ_{DB}	ϵ_{RV}	$\sqrt{\sigma_{\text{DB}}^2 + \epsilon_{\text{RV}}^2}$	σ_{178°	Excess σ
Early A]8500–10 000]	67	14	7.2	15.7	20.7	13.5
Late A]7500–8500]	151	19	5.5	19.8	21.7	8.9
Early F]6500–7500]	139	23	4.2	23.4	27.8	15.0

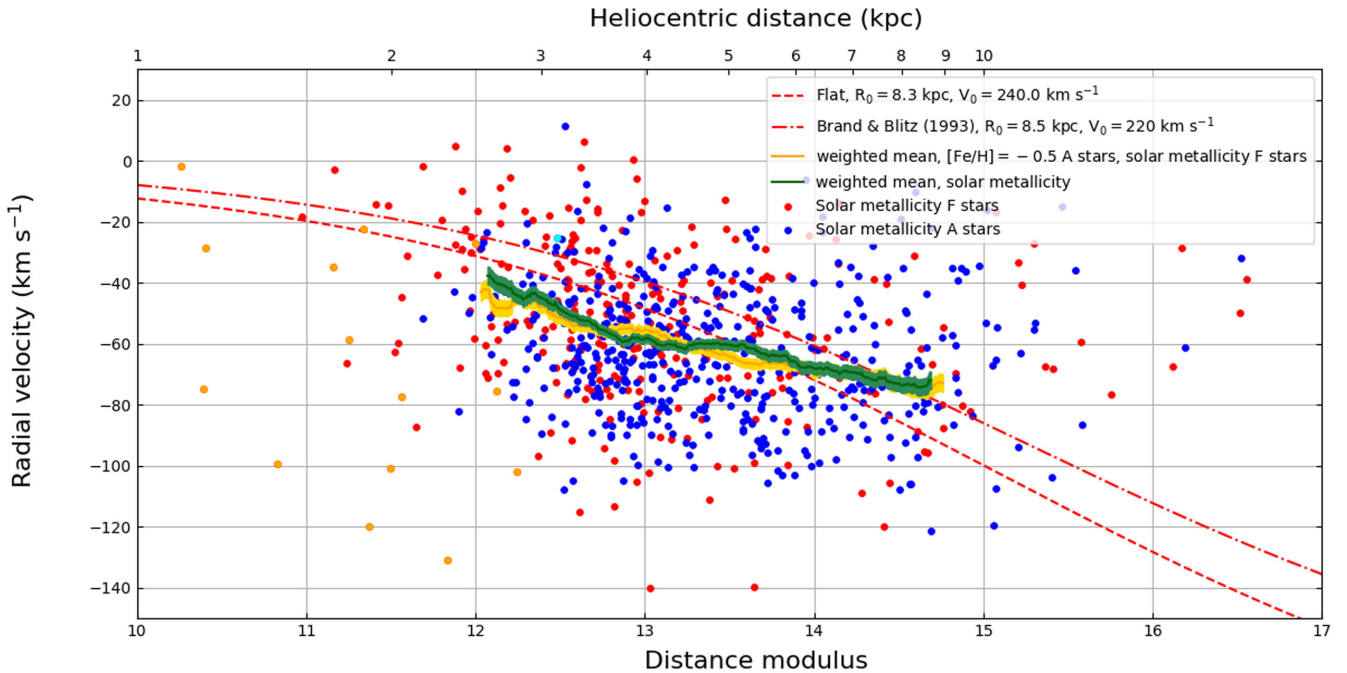


Figure 11. The trend in RV with distance modulus at $\ell = 118^\circ$. The red dashed/dotted lines show the expected trends for a flat rotation law and the Brand & Blitz (1993) slowly rising rotation law (see legend). The green line is the weighted mean of the RVs obtained using stellar parameters returned for solar metallicities, and the yellow line is the alternative result obtained on swapping in A-star data computed for $[\text{Fe}/\text{H}] = -0.5$. The shaded regions represent the standard error of the mean in RV. The individual data points in blue are obtained from A stars, while red is used for the F stars (computed for solar metallicity). The cyan point is the A star identified as lying far from the IPHAS mean extinction trend, and the orange points the F stars (see Fig. 9).

4.2 $\ell = 118^\circ$

The results for this sightline are shown in Fig. 11. Again, the green line is the mean trend for solar metallicity stars and the yellow for $[\text{Fe}/\text{H}] = -0.5$ A stars and solar metallicity F stars. The mean trends, calculated in the same way as for $\ell = 178^\circ$ described in Section 4.1, deviate more strongly from expectations based on a flat or slowly rising rotation curve (shown in the figures by the red dashed/dotted lines). The measured trends are appreciably flatter. The $\ell = 118^\circ$ results are similar for both A-star metallicities, indicating that metallicity is not having a strong effect on the interpretation of the results. The mean RV trend (for either A-star metallicity) spans the heliocentric distance range from 2.5 to 9 kpc ($R_G \simeq 9.7\text{--}14.8$ kpc), with the RV decreasing slowly from ~ -40 to -70 km s^{-1} .

For context, we note that the Perseus Arm is likely to pass closest to this line of sight at a distance of 2.5–3 kpc (Reid et al. 2014). This overlaps the bottom end of the distance range that we sample. In Fig. 11, there is no clear sign of a distinct localized RV perturbation that might be attributed to the arm. Spiral arm perturbations are discussed further in Section 5.3.

The velocity dispersions around the RV mean trend for the three spectral type groups specified in Table 3 at the $\ell = 118^\circ$ sightline are: 19.8 km s^{-1} for the early A stars, 21.1 km s^{-1} for the late A stars, and 24.3 km s^{-1} for the early F stars. These values are similar to those measured for the anticentre sightline (shown in Table 3), which permits the same interpretation that binary orbital motions are a third factor contributing to the overall observed dispersion.

In the next section, we consider whether the photometric consequences of binarity could distort the results, discuss the observed departure from a flat or slowly rising rotation law, and consider the possibilities for detecting spiral arm perturbations.

5 DISCUSSION

5.1 Potential bias from binaries and distance error

The relatively flat distribution of RVs seen at $\ell = 118^\circ$ in place of the expected falling trend may possibly be a consequence of unrecognized binaries placed at inappropriately short distances, or of significant smearing due to distance error.

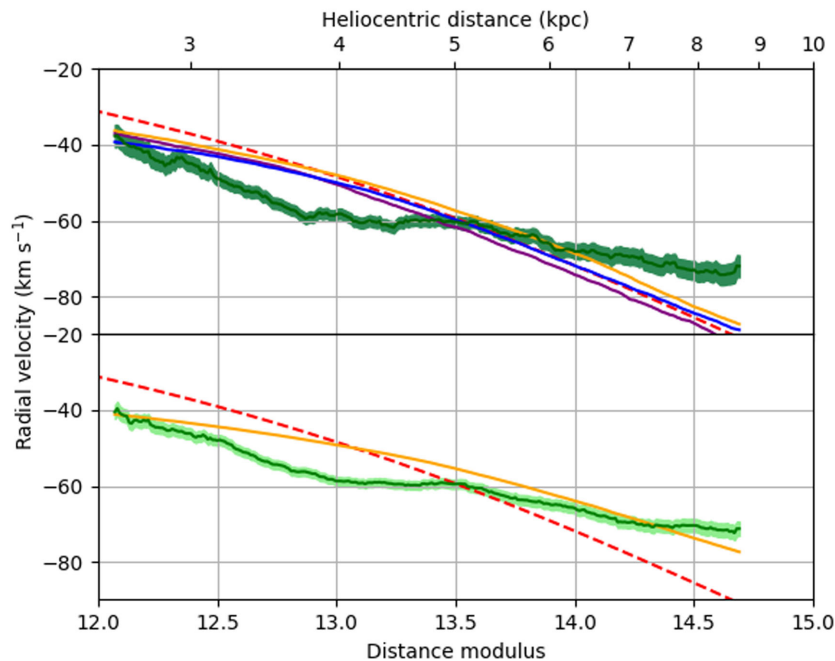


Figure 12. The results of simulations to test the effects on the mean RV trend of undetected binaries and distance modulus errors. In the top panel, the purple line is the mean RV trend for the simulation incorporating unresolved binaries. The orange line is the result from the simulation testing the effect of distance modulus error only, while the blue line shows the simulated effect of both unresolved binaries and distance modulus errors. The observed RV trend is overlaid in green. In the bottom panel, we test the effect of doubling our distance modulus errors (orange line). The greater error induces more flattening. The light green line in this case is the mean RV trend of the HectoSpec data obtained on adopting doubled distance modulus errors.

If a target star is actually an unresolved binary system, the measured apparent magnitude will be brighter than if it were a single star. In effect, the absolute magnitude adopted in our analysis is then too low, and hence the distance will be underestimated. Similarly, if the component masses are unequal, the colour will be redder than if the system were a single star, resulting in overestimation of the extinction and further underestimation of distance. The additional velocity component from the motion around another star in a binary system does not produce a bias on the RV results since the space orientation of binary orbital axes across a large sample is random and must cancel out. The photometric effect will be most pronounced in nearly equal mass binary systems, and has been quantified by Hurley & Tout (1998). Since the binary mass ratio distribution in A/F stars is not far from flat, we might expect of the order of 10–20 per cent of our sample to be misconstrued as closer to the Sun by up to 0.75 in μ . In principle, this might erroneously flatten the overall RV distribution by bringing in a group of objects at more negative RV to mix with less negative values at smaller μ .

In order to test the effect of binarity on the calculated weighted average RV trend, we have performed an outline simulation that focuses on this factor. Our method is as follows. We select three sets of stars of different spectral type groups: early A, late A, and early F. The size of the sets are the same as the HectoSpec $\ell = 118^\circ$ groups (early A: 168 stars, late A: 281 stars, early F: 259 stars). 70 per cent of stars in each group are randomly selected as binaries – these are assigned a primary mass, m_1 , and the secondary mass, m_2 , is assigned at random according to a mass ratio fraction, q , obeying the distribution $f(q) = q^{-0.5}$ (Duchêne & Kraus 2013). The distance modulus assigned to each star is sampled from the HectoSpec μ distribution for its spectral type group. In order to compensate for the expected net decrease in μ associated with treating output binary stars as single, these reference distributions are first

modified by a uniform retrospectively determined shift of $+0.16$. The assigned RVs follow a flat rotation curve with $V_0 = 240 \text{ km s}^{-1}$ at $\ell = 118^\circ$, broadened by an amount consistent with the scatter defined by Dehnen & Binney (1998) and measurement error. The final adjustment is to include a component of binary orbital motion. To achieve this, a period, P , inclination, i , and phase, ϕ , must be randomly assigned for each binary star. The period is selected from the distribution of A-star periods shown in fig. 2 in Duchêne & Kraus (2013). The inclination is chosen from a uniform distribution in $\cos i$, and the phase from a uniform distribution between 0 and 2π . In the final reconstruction of the observed RV distribution, each simulated binary star has its distance modulus reduced to the equivalent single value according to the computed difference in intrinsic colour and absolute magnitude.

The simulation of 708 stars was performed 10 000 times, and the mean RV trend was calculated each time. The mean of these 10 000 trends is shown as the purple line in Fig. 12. The binary stars are pulled by varying amounts to shorter distances and bring with them their on-average more negative RV. A flattening of trend is seen, but our numerical experiment indicates it is modest. The deviation away from a flat rotation law we find at $\ell = 118^\circ$ (Fig. 11) is much more pronounced, leading us to conclude that an appeal to stellar multiplicity to explain it falls well short, quantitatively.

Another factor that will cause some flattening of the $\ell = 118^\circ$ trend is distance error. The derived distance distribution is essentially the true distance distribution broadened by the uncertainty. Consequently, the mean RV trend spans this slightly broader distribution, causing a flattening. To test the extent of this, we performed a simulation similar to the one described above used to test the effect of unresolved binaries. However, this time we disregard binary stars, and after assigning a suitably scattered RV with measurement error to each notional star, we shifted the corresponding distance modulus

by an amount within the typical level of error from the HectoSpec data. The result is shown as the orange line in Fig. 12. The resultant mean trend is somewhat flattened, but not by an amount that makes it parallel to the result from observation. To complete the picture, we performed this simulation again but now including unresolved binaries as described above. The blue line in Fig. 12 shows the result. The amount of flattening is similar to that due to the distance errors alone. At shorter distances it is slightly more pronounced, and at further distances it is less. This is expected since the binaries are pulled to shorter distances, bringing with them their on-average more negative RV.

In order to achieve a flattening of the simulated curve by an amount that begins to mimic the trend deduced from the A/F star data, we find we need to double the distance errors relative to those propagated from the data as described in Section 3.4. The second panel of Fig. 12 illustrates this. Whilst it is certainly a possibility that the estimation of distance errors in our sample is optimistic at ~ 15 per cent ($\Delta\mu = 0.3$), growing them all by as much as a factor of two is rather less credible.

5.2 Comparisons of results with other tracers and earlier work

Using H II region data, Brand & Blitz (1993) presented sparse-sampled measurements that mainly captured heliocentric distances out to ~ 4 kpc at the Galactic longitudes of interest here (see their fig. 1). The overlap with our results thus runs roughly from 2 to 4 kpc. Near the anticentre, Brand & Blitz (1993) generally favoured slightly negative radial velocities, ranging from -18 to $+8$ km s $^{-1}$ (9 data points, from their table 1), to be compared with a small positive bias here (Fig. 10). In the longitude range $110^\circ < \ell < 130^\circ$, the relevant measurements are spread between -30 and -56 km s $^{-1}$ (13 data points). This is entirely compatible with our results.

A denser comparison between our results and other studies can be made using RV data of H I and CO clouds. Since both sightlines miss the latitude of peak gaseous emission for their longitudes, the total amount of both H I and CO is not particularly large. Nevertheless, the measured gaseous RV distributions are broadly consistent with our findings from HectoSpec, and the detail is informative. H I 21cm data from EBHIS (The Effelsberg-Bonn H I Survey; Winkel et al. 2016) in the $\ell = 178^\circ$ sightline scatter around $RV \simeq 0$ at much reduced dispersion compared to the A/F stars – as expected. We find that the mean RV measures from our optical spectroscopy are shifted relative to the H I data by $\sim +8$ km s $^{-1}$, and regard this mainly as evidence that the H I column samples a greater column through the outer disc than our stellar sample.

The comparison with EBHIS data at $\ell = 118^\circ$ shown in Fig. 13 shows the A/F star data line up with the main ~ -60 km s $^{-1}$ H I emission peak, while the peak at ~ 0 km s $^{-1}$ (from the Local Arm, seen in H I) is clearly absent. This is to be expected given that none of the A/F stars selected and measured will be in or near the Local Arm. The H I data also present a peak at ~ -90 km s $^{-1}$ that is largely absent from the stellar data. This is unsurprising since our central result from the $\ell = 118^\circ$ sightline is the RV flattening that implies a relative absence of stars in this more negative velocity range (at distances where a flat or gently rising rotation law would predict they exist). A reasonable inference from this is that the H I gas at the most negative radial velocities lies mainly outside the range sampled by the A/F stars. We note that the CO data from the COMPLETE (Coordinated Molecular Probe Line Extinction and Thermal Emission; Ridge et al. 2006) survey exhibit the same RV peaks as the H I data. This difference either indicates that the H I and CO gases lie beyond $d \sim 9$ kpc or that the distance range

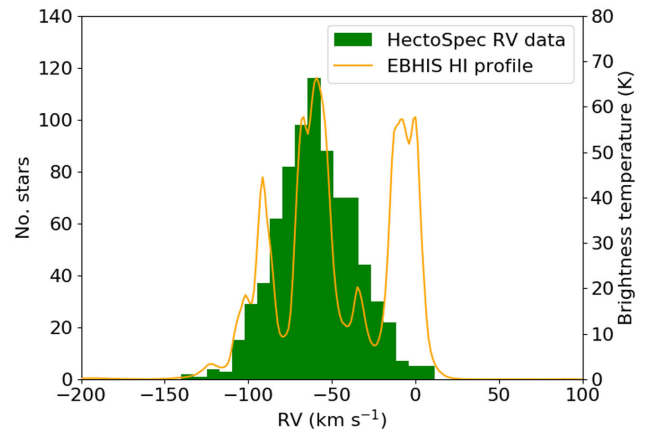


Figure 13. The H I profile at $\ell = 118^\circ$ (orange line), overlaid on the HectoSpec RV data (green histogram).

occupied by our sample of stars does not extend to the distances where existing rotation laws would predict $RV \sim -90$ km s $^{-1}$. From Fig. 11, it can be seen that these laws associate a distance of ~ 8 kpc with this RV. We argue below that the stars in our sample placed at ~ 8 kpc are not simple because of distance error.

Huang et al. (2016) have used red clump giants drawn from a wide range of Galactic longitudes sampling the outer disc to find a broadly flat longitude-averaged rotation law within $R_G < 25$ kpc, with typical circular speed $V_0 = 240 \pm 6$ km s $^{-1}$. But over our sampled region, between $R_G \simeq 10$ – 15 kpc, their inferred rotation law is quite sharply rising out of a dip at $R_G \sim 11$ kpc. Fig. 14 compares the Huang et al. (2016) results (red line) with the rotation curve derived from the mean RV trend we obtain at $\ell = 118^\circ$ adopting solar metallicity (green line). In constructing this figure, we choose the same LSR parameters as favoured by Huang et al. (2016), $R_0 = 8.3$ kpc, and $V_0 = 240$ km s $^{-1}$. The agreement is very good.

We commented before in Sections 3.2.2 and 3.3 that there may be a positive bias in the derived stellar surface gravities. The amount of bias may very well be in the region of $\Delta \log g = +0.15$, as suggested by Fig. 6. The remeasurements of just seven objects find in favour of a larger bias (see Section 3.3), but we do not otherwise see evidence that the distance range of our stellar sample, strongly influenced by $\log g$, is significantly underestimated (cf. Fig. 9 and the linked discussion). We have also considered whether there is a bias in the measured RV. The best evidence we have of this comes from the seven remeasurements at red and blue wavelengths: the weighted mean offset obtained is -2.7 km s $^{-1}$. If all stellar surface gravities are corrected down by 0.15 dex, and this potential RV bias is also taken out uniformly, the trend in circular speed acquires the form of the blue line in Fig. 14. The main impact of these changes is to stretch the results out to an increased Galactocentric radius, in response to the $\log g$ shift. The outcome remains consistent with the Huang et al. (2016) results. Another factor playing a role is the presumed metallicity for the A stars: the orange line in the figure shows the rotation curve when setting $[\text{Fe}/\text{H}] = -0.5$ for the A stars. It can be seen that this change also has little impact.

So we have that both the clump giants and, now, our A/F star sample favour a rotation law that rises out to $R_G \sim 14$ kpc, after a minimum near ~ 11 kpc. But we have also demonstrated how distance error can modify the observed RV–distance trend. And indeed Binney & Dehnen (1997) presented a thought experiment that drew attention to how a linear increase in Galactic rotation

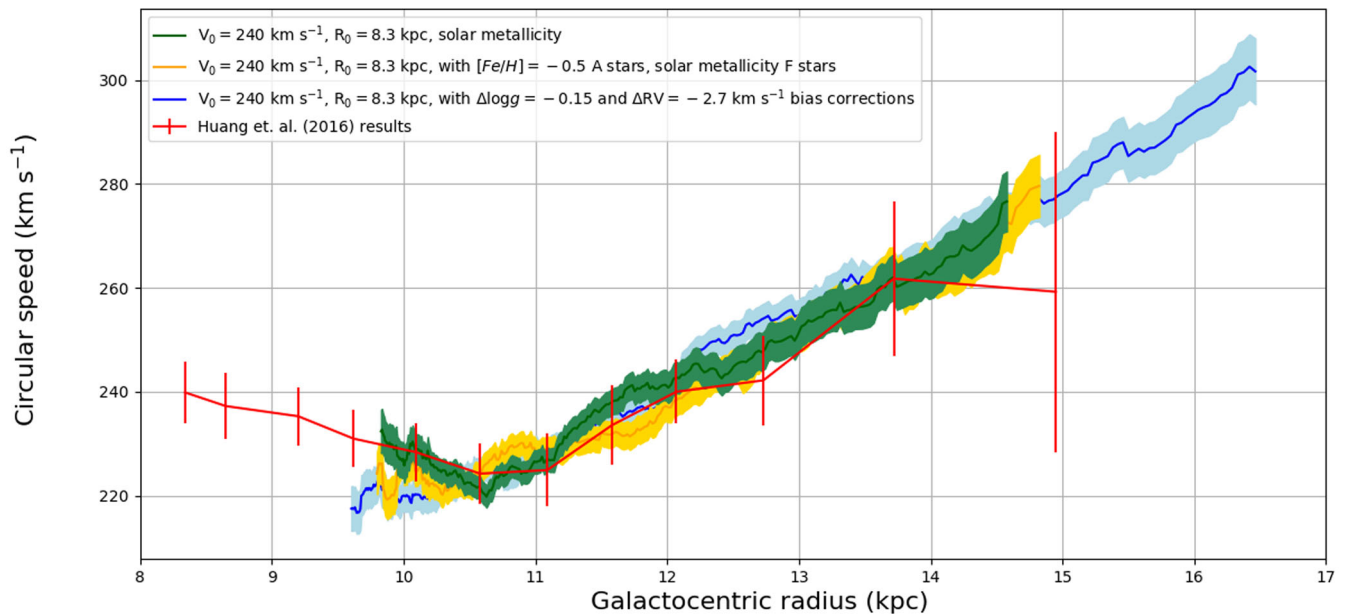


Figure 14. Galactic disc circular speed results from Huang et al. (2016) are reproduced in red. The circular speeds derived from the mean RV trend for results at $\ell = 118^\circ$, adopting solar metallicity, are in green. Results obtained with $\Delta \log g = -0.15$ and $\Delta RV = -2.7 \text{ km s}^{-1}$ potential bias corrections are shown in blue. Orange is used for the results obtained when the A-star parameters for $[Fe/H] = -0.5$ are used in place of solar metallicity parameters. The shaded region around each HectoSpec line represents its error – propagated from the error on the mean trend in Fig. 11.

into the outer disc would arise this way. The particular example they presented was of the inferred law from tracers confined within a ring – mimicking gas tracers associated with spiral arms – at 1.6 times the Sun’s Galactocentric radius. These were subject to distance uncertainties similar to the larger errors considered in the lower panel of Fig. 12. This extreme is avoided here. The facts of the spread in stellar parameters ($\Delta M_i \sim 2$) and apparent magnitudes ($\Delta m_i \sim 1.5$, see Fig. 3) combine with gently rising extinction (see Fig. 9) to yield an underlying stellar distribution that should span at least 5 kpc – nor is there an expectation these stars would be confined to e.g. just the Perseus Arm. This leaves us cautiously supporting the case for an increase in circular speed outside the Solar Circle and looking forward to the more extensive studies needed to clarify the situation.

5.3 Spiral arm perturbations

Spiral arms in galactic discs are widely viewed as linked with non-axisymmetric kinematic perturbations. To assess whether our data can expose such an effect, we examine the $\ell = 178^\circ$ sightline, since it is close to the radial direction that minimizes shear due to Galactic rotation and more easily reveals low-amplitude perturbations that may be associated with spiral arm structure. Monguió, Grosbøl & Figueras (2015) used B4–A1 stars to find a stellar overdensity due to the Perseus spiral arm at a heliocentric distance of 1.6 ± 0.2 kpc in the anticentre direction, and Reid et al. (2014) used parallaxes of 24 star-forming regions to find the arm to be located at 2 kpc. The Perseus Arm is therefore located just short of the sampled region in this work. However, Reid et al. (2014) also found evidence that an Outer Arm is located at a heliocentric distance of 6 kpc in the anticentre direction. This arm lies near the far end of our sampled region.

The scale of radial velocity perturbation depends on the model adopted for the origin of the perturbation. On the one hand, Monari, Famaey & Siebert (2016) simulated the effect of a spiral potential

on an axisymmetric equilibrium distribution function (emulating the Milky Way thin stellar disc) and found radial velocity perturbations of order -5 km s^{-1} within the arms and $+5 \text{ km s}^{-1}$ in between them. On the other hand, Grand et al. (2016) favour the transient winding arm view and find the perturbation of young stars (<3 Gyr) to be considerably stronger at up to 20 km s^{-1} .

We do not see any clear signs of perturbations, negative or positive, aligned with the Outer Arm in the HectoSpec results. However, since the HectoSpec RV error is comparable with predicted perturbations at the lower end of the expected range, and the stellar sample is subject to distance error, it is not obvious that we should expect to observe their signal in our data. In order to test this, we conducted another simulation. A sample of stars the same size as the HectoSpec $\ell = 178^\circ$ sample and with the same distance distribution were assigned RVs according to a sinusoidal waveform – three separate tests were conducted with amplitudes of 5, 10, and 20 km s^{-1} . Two spiral arms were put at 2 and 6 kpc. Velocity scatter, RV error, and distance error were then applied to the distribution, and a mean trend was computed as in Section 4.1.

The results obtained for the small perturbations (5 km s^{-1}) exhibited no clear signs of the input sinusoid’s phasing or wavelength, giving a mean trend compatible with zero for most of the sampled range. In contrast, the results for the larger amplitude perturbations did show signs of the input phasing, wavelength, and amplitude. We conclude that spiral arm perturbations of small amplitude would be unlikely to appear with clear statistical significance in our results, but those of larger amplitude would.

Returning to the HectoSpec $\ell = 178^\circ$ results themselves (Fig. 10), we do observe a wave-like structure in the mean RV trend with amplitude $\sim 5\text{--}10 \text{ km s}^{-1}$, but not at an implied phase or long-enough wavelength that would make sense in comparison with the expected locations of the Perseus Arm and Outer Arms (at ~ 2 and ~ 6 kpc in this sightline, respectively). If the RV wobble is real, rather than a sample size effect, it is most likely a local effect unconnected with the larger scale structure of the Galactic disc. But we must discard

the possibility of large amplitude ($10\text{--}20\text{ km s}^{-1}$) perturbations in this direction. The results for this sightline are in keeping with the findings of Fernández, Figueras & Torra (2001), who used both OB stars and Cepheids to limit perturbations to under 3 km s^{-1} .

Finally, we comment on the form of the $\ell = 118^\circ$ results (Fig. 11). Specifically, can a spiral arm perturbation explain the observed deviation from the trend predicted by a flat rotation law? To make this comparison, the same three simulations as described above for the $\ell = 178^\circ$ sightline were conducted for $\ell = 118^\circ$. In this case, the spiral arms are located at 3 and 6.5 kpc (Reid et al. 2014) and account is taken of the expected combination of Galactic azimuthal and radial perturbations along the line of sight. In this case, the observed RV trend, when compared with the simulation alternatives, shows a deviation from the flat rotation law of a scale similar to that of the largest (20 km s^{-1}) perturbation investigated. This stands in clear contrast to the low-amplitude perturbation compatible with the $\ell = 178^\circ$ sightline. Hence, it appears that there is no simple coherent way of interpreting our radial velocity trends in terms of one class of spiral arm perturbation model.

6 CONCLUSIONS

For the first time, we have demonstrated that A/F star spectroscopy, even when restricted to a small region around the CaT lines, can provide useful insights into the kinematics of the Milky Way disc. With the use of the method employed in this paper, stellar parameters and radial velocities can be measured for the very large samples of these stars, with $i < 18$ (Vega), which will be accessible to future massive-multiplex instruments such as the WEAVE and 4MOST spectrographs being constructed for the William Herschel and VISTA telescopes, respectively.

This first result, deploying a dense sample of ~ 800 A/F stars within just one pencil beam, 1 deg in diameter, at $\ell = 118^\circ$, fits in well with the trend of a rising mean circular speed within the Galactic disc reported recently by Huang et al. (2016), over the Galactocentric radius range $11 < R_G$ (kpc) < 15 . Interpreting these RV measurements in terms of spiral arm perturbation is more difficult as then it becomes hard to reconcile the $\ell = 118^\circ$ and $\ell = 178^\circ$ results. The Huang et al. (2016) sample of clump giants is much larger, comprising $\sim 16\,000$ stars, drawn from a very broad fan of outer-disc longitudes ($100^\circ < \ell < 230^\circ$, roughly) – hence, their results describe a longitude average, in contrast to ours. Further dense-sampling studies like ours will be needed to discover whether the rotation law is closely axisymmetric as has usually been assumed, hitherto. This first comparison passes the test. However, both stellar results are at variance with the maser-based study of Reid et al. (2014), which obtained evidence of a very nearly flat rotation law to $R_G = 16$ kpc, as well as with the long-established Brand & Blitz (1993) law. The origin of this difference may rest in the very limited maser data at all longitudes beyond $R_G = 12$ kpc (see fig. 1 of Reid et al. 2014). On the other hand, caution still needs to be exercised that some of the inferred steepening may prove to be a consequence of uncertainties in stellar distances derived from spectroscopic parallax. If the steepening is correct, it would lend support to previous evidence of a ring of dark matter in the outer disc at R_G between 13 and 18 kpc (see e.g. Kalberla et al. 2007).

Our goal is to open up the use of A/F stars in studies of Galactic disc structure at red wavelengths that mitigate the effects of extinction. It is more common to derive stellar parameters for these earlier type stars in the blue optical and so it was not evident at the outset whether fitting to the red range only would suffer from

biases or degeneracies in parameter determination. For the present purpose, it has become clear that degeneracies are less troublesome for A stars than F stars, although it would be desirable in future to better disentangle effective temperature and metallicity, even for A stars – better spectral resolution and wider wavelength coverage can both help here. We plan to examine these options. The basic method of target selection, using IPHAS colours, is certainly very efficient (see also Hales et al. 2009). We have assessed possible bias in our numerical results: whilst there appears to be some, our tests examining their impact have so far shown that the impact is modest. Furthermore, we find that the random error on the mean trend in circular speed with increasing Galactocentric radius, achieved with our dense localized sampling, is generally better than $\pm 5\text{ km s}^{-1}$, and represents an advance on previous measurements.

Since the single biggest source of uncertainty in a study like this originates in the stellar distances, we look forward to the new opportunity that starts to take shape with the stellar astrometry in the *Gaia* DR2 release in 2018 April. A representative i magnitude among our selected A/F stars is ~ 17 (or *Gaia* G approaching 18): at this brightness, the anticipated DR2 (end-of-mission) parallax and proper motion errors are likely to be 150 (100) μas and 80 (50) $\mu\text{as yr}^{-1}$, respectively (see ESA website and Katz & Brown 2017). Whilst distances cannot be nailed down for individual stars, over the range of interest here from ~ 2 to almost 10 kpc (parallaxes of 500 down to 100 μas), significantly improved constraints will become available. There will also be the opening to bring into account full space motions, on folding in *Gaia* proper motion data. As our next step to prepare for this, we are building customized forward simulations based on Galactic models aimed at predicting full space motion distributions. As part of this, we will examine in further detail the roles played by our methods of target selection and analysis. We have already checked one of the more obviously significant issues that concerns us – no weeding of binary stars – and have found that to be a small effect.

Another experiment for the future will be to examine the differences in performance of A-star and clump-giant samples, on the same sightline. Based on what we have learned here, there is reason to expect A-star samples to be especially valuable in characterizing the outer Galactic disc, where these younger less-scattered stars are relatively more common.

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