A spurious correlation between difference scores in evidence accumulation model parameters

> James A. Grange Keele University, UK

Stefanie Schuch RWTH Aachen University, Germany

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Author Note

The authors share first authorship. Please address correspondence to James A. Grange (grange.jim@gmail.com) or Stefanie Schuch (schuch@psych.rwth-aachen.de).

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Abstract

Evidence-accumulation models are a useful tool for investigating the cognitive processes that give rise to behavioural data patterns in reaction times (RTs) and error rates. In their simplest form, evidence-accumulation models include three parameters: The average rate of evidence accumulation over time (drift rate) and the amount of evidence that needs to be accumulated before a response becomes selected (boundary) both characterise the response-selection process; a third parameter summarises all processes before and after the response-selection process (non-decision time). Researchers often compute experimental effects as simple difference scores between two within-subject conditions and such difference scores can also be computed on model parameters. In the present paper, we report spurious correlations between such model parameter difference scores, both in empirical data and in computer simulations. The most pronounced spurious effect is a negative correlation between boundary difference and non-decision difference, which amounts to r = -.70 or larger. In the simulations, we only observed this spurious negative correlation when either (a) there was no true difference in model parameters between simulated experimental conditions, or (b) only drift rate was manipulated between simulated experimental conditions; when a true difference existed in boundary separation, non-decision time, or all three main parameters, the correlation disappeared. We suggest that care should be taken when using evidence-accumulation model difference scores for correlational approaches, because the parameter difference scores can correlate in the absence of any true inter-individual differences at the population level.

Keywords: Diffusion modelling; Individual differences; RT difference scores; Correlations

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In recent years, renewed attempts have been made to bridge the long-recognized gap between experimental cognitive psychology on the one hand, and inter-individual differences research on the other (e.g., Borsboom, Kievit, Cervone, & Hood, 2009; Cronbach, 1957; Euler & Schubert, 2021; Hedge et al., 2017; Miller & Ulrich, 2013; Parsons, Kruijt, & Fox, 2019; Rouder & Haaf, 2019; Rouder et al., 2019). However, these two branches of psychological research use different methodologies, making it difficult to bridge the gap.

One problem is the so-called "reliability paradox" (Hedge et al., 2017): It has repeatedly been observed that standard experimental effects such as the Stroop effect, the Simon effect, or the task-switch cost—effects that have been replicated in thousands of studies—have surprisingly low split-half and retest reliability. Moreover, when the same effect is measured as response time (RT) difference score and error difference score, even these two measures of the same effect often do not correlate (e.g., Hedge et al., 2018). Part of the problem is that experimental psychology and inter-individual differences psychology focus on two different kinds of reliability: Experimental psychology aims to provide effects that occur in all (or almost all) individuals and are of similar size in all individuals, and therefore are replicable in group-level analyses across different samples. In contrast, psychological research into inter-individual differences looks for effects that consistently and reliably differ across individuals (see also Rouder & Haaf, 2019 for a discussion of this distinction). Here, an effect is reliable when the same rank-ordering of individuals can be reproduced across different data sets from the same group of individuals. Hence, reliability in the sense of experimental research and reliability in the psychometric sense are two different concepts that are not easily reconciled.

Evidence Accumulation Models

As a possible way of increasing the reliability of experimental effects in the psychometric sense, researchers have started to use formal computational modelling, such as evidence accumulation models, taking model parameters instead of behavioural measures (such as mean RT and mean error rates) as primary dependent variables (e.g., Lerche & Voss, 2017; Lerche et al., 2020; Hedge et al., 2018, 2019, 2021; Ratcliff & Childers, 2015; Schubert et al., 2015, 2016, 2021; for using evidence-accumulation models for correlational approaches in cognitive neuroscience, see e.g., Forstmann et al., 2011, 2016). Evidence-accumulation models are a class of formal computational models that can be applied to speeded choice RT tasks with two or more response alternatives. Such models assume that evidence for the different response alternatives is accumulated over time until an evidence threshold/boundary for one response alternative is reached; this response alternative then becomes selected. In their simplest form, these models include two parameters for the response-selection process: the average rate of evidence accumulation over time (drift rate), and the height of the threshold/boundary that needs to be reached (boundary separation). A third parameter in these models summarises all processes before and after the response-selection process, and is often called non-decision time. Prominent examples of evidence-accumulation models are the drift-diffusion model (DDM) introduced by Ratcliff and colleagues (e.g., Ratcliff & McKoon, 2008; Ratcliff et al., 2016; see Figure 1), and the Linear Ballistic Accumulator (LBA) model by Heathcote and Brown (2008). More complex models have been developed that include additional parameters (see, e.g., Servant, Montagnini, & Burle, 2014; White, Servant, & Logan, 2018, for discussion and comparison of models designed to account for performance in conflict tasks).

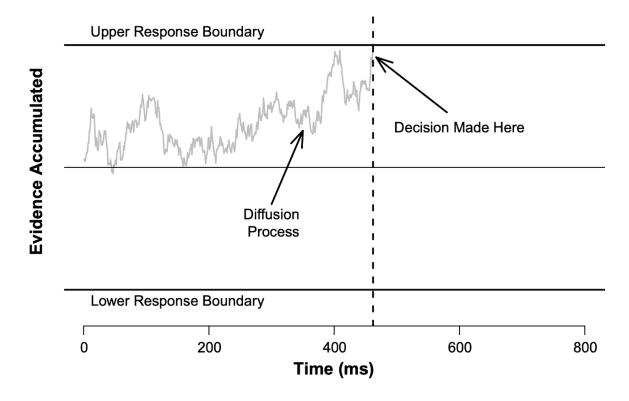


Figure 1. Schematic representation of trial processing in the Drift Diffusion Model. Note some researchers refer to the response boundary as an "evidence threshold". Figure available at https://www.flickr.com/photos/150716232@N04/46893547582 under CC license https://creativecommons.org/licenses/by/2.0/.

Evidence accumulation models can be useful for a better understanding of the relationship between experimental psychology and interindividual differences research. For instance, Hedge et al. (2018) investigated the surprising lack of a consistent correlation between RT difference scores and error difference scores of the same effect using evidence-accumulation models. They demonstrated that this lack of correlation between behavioural difference scores of the same effect can be understood when considering difference scores in DDM parameters. In general, the experimental effect (be it the Stroop effect, Simon effect, task-switch cost, or other) is computed as the within-subject difference between two conditions, which can be termed the "easy" and "hard" conditions for sake of generality. Hard-minus-easy difference scores can be computed on behavioural measures as well as on model parameter values. If participants differ in the size of their difference score in

the evidence accumulation parameter, then RT difference scores and error difference scores will be *positively* correlated across participants. If, in addition, participants differ in their overall threshold setting, the same difference in evidence accumulation between hard and easy conditions will produce larger RT effects—and at the same time smaller error effects—in those individuals with higher thresholds than in those individuals with lower thresholds. This latter effect can produce a negative, or close-to-zero, correlation between RT difference scores and error difference scores across individuals. Hence, relying on behavioural difference scores alone does not make much sense for correlational approaches, because correlations between behavioural difference scores can be positive, negative, or non-existent, depending on the underlying cognitive processes that cause the interindividual variability in the behavioural difference scores.

In light of these insights, it may be tempting to rely more on model-parameter difference scores instead of behavioural difference scores. In fact, in experimental psychology, several researchers have investigated common experimental effects with simple evidence accumulation models, and computed model-parameter difference scores, for example for the response-effect compatibility effect (Janczyk & Lerche, 2019), the backward-crosstalk effect in dual-tasking (Durst & Janczyk, 2019; Janczyk, Büschelberger, & Herbort, 2017); task-switch costs (Schmitz & Voss, 2012, 2014); N–2 task-repetition costs in task switching (Kowalczyk & Grange, 2020; Schuch, 2016, Schuch & Grange, 2019; Schuch & Konrad, 2017) and speed–accuracy tradeoff effects (Forstmann et al., 2011; see Heitz, 2014, for a review).

Such difference scores in model parameters obtained from experimental psychology could in turn be used for correlational approaches, potentially yielding more reliable

correlations. Thus, difference scores in model parameters could be a promising tool for integrating cognitive experimental psychology and inter-individual differences research.

Overview of the Present Paper

Regarding the possibility of using difference scores from evidence-accumulation model parameters for investigating inter-individual differences, in the present paper we highlight a potential problem with such model-based difference scores. We incidentally observed a strong negative correlation between two parameters of a simple evidence-accumulation model in our own data sets and set out to investigate this finding in a more systematic way. In particular, when applying a simple drift-diffusion model, we observed a pronounced correlation between the boundary separation parameter difference score and the non-decision time parameter difference score: Those participants who show a higher boundary in the hard than easy condition typically show a smaller non-decision time in the hard than easy condition, and vice versa. This incidental finding raised our curiosity, and we checked several more of our own data sets. We observed a pronounced negative correlation in all of them of around r = -.70 between the difference scores in boundary separation parameter and the difference scores in non-decision time parameter across participants. We also checked whether this negative correlation was present in data collected independently of either of our research groups by reanalysing some of the data from Dutilh et al. (2019), and found it was indeed present.

This incidental finding made us wonder whether this is a theoretically interesting effect, or perhaps a methodological artefact of some sort. We therefore conducted a series of computational simulations where we knew the true population parameter values and could manipulate them systematically. The simulations revealed that even in the absence of any differences in population parameter values between the easy and hard conditions, a

correlation of difference scores in DDM parameters emerged. The pronounced negative correlation consistently occurs between the difference score in boundary separation parameter and the difference score in non-decision time; at the same time, there are no such pronounced correlations of one of these difference scores with the difference score in the evidence accumulation rate parameter (although we sometimes did observe a moderate positive correlation between boundary separation difference score and evidence accumulation difference score).

Notably, the pronounced negative correlation in the simulations is *only* observed between parameter *difference scores* of boundary separation and non-decision time, while at the same time, the overall values of boundary separation and non-decision time parameters within a condition are not highly correlated. That is, we observed a pronounced negative correlation between the hard-minus easy *difference score* in boundary separation parameter and the hard-minus-easy *difference score* in non-decision time parameter, while there are no such pronounced correlations between boundary separation parameter and non-decision time parameter within the hard condition, or within the easy condition.

Our further investigations revealed that this spurious correlation of model difference scores is not constricted to one particular kind of evidence accumulation model, or to the fitting algorithms of one particular software package; rather, we observed the correlation both when using the Ratcliff drift-diffusion model and the Linear Ballistic Accumulator Model (Brown & Heathcote, 2008), and with different software packages (*fast-dm-30*: Voss, Voss, & Lerche, 2015; Voss & Voss, 2007; *EZ-diffusion model*: Wagenmakers et al., 2007; *rtdists*: Singmann et al., 2020).

Diffusion models fall within the class of so-called "sloppy" models where parameters are known to be highly correlated—a characteristic typical of many biologically plausible

models—which can impact on the efficiency and accuracy of parameter estimation (Boehm et al., 2019; Heathcote et al., 2019). Indeed, recent studies have shown that when independent research teams attempt to fit versions of the diffusion model to a single data set, the teams often produce quite different estimates of best-fitting model parameters, and these differences sometime lead to different inferences (Boehm et al., 2019; Dutilh et al., 2019). Documenting the extent of these correlations is therefore of importance for researchers wishing to draw valid inferences from their modelling. Our findings imply that care should be taken when interpreting diffusion-model difference scores in boundary-separation parameter and non-decision time parameter. These difference scores can correlate in the absence of any population-level differences between two within-subjects experimental conditions. Moreover, the difference scores in these two model parameters should not be used in individual-differences research, because they do not necessarily reflect true inter-individual differences at the population level.

In the following, we will first describe the spurious correlation in two empirical data sets of previously published studies, one from our own labs (Schuch & Grange, 2019), and one from a different lab (Duthil et al., 2019). Then we will describe in detail the set of computational simulations, and we will conclude with some considerations on what could cause the spurious correlation and some recommendations for researchers wishing to apply these models.

Reanalysis of Behavioural Data

In several of our own data sets (from published and unpublished studies), we observed a pronounced negative correlation between participants' boundary-separation parameter difference score and their non-decision time parameter difference score when applying a simple drift-diffusion model. In the following, we exemplarily present a reanalysis of a

previously published study of ours (Schuch & Grange, 2019), where this correlation amounted to about r = -.70 in all experimental conditions.

Schuch and Grange (2019)

In the Schuch and Grange's (2019) study, N-2 task repetition costs were measured, which are a kind of task-switch cost where different types of task sequences are compared. N-2 task repetition costs denote the finding of worse performance in task sequences of the type ABA (where the task performed in trial N is the same as the task performed in trial N-2) as compared to type CBA (where the task in trial N is not the same as in trial N-2). The performance decrement in ABA versus CBA is usually taken as an indicator of persisting task-level inhibition (Mayr & Keele, 2000; see Gade, Schuch, Druey, & Koch, 2014; Koch, Gade, Schuch, & Philipp, 2010; Mayr, 2007, for reviews). The reasoning is that task A becomes inhibited when switching from A to B, and this inhibition decays slowly over time; the sooner one switches back to the previously inhibited task, the more persisting inhibition needs to be overcome. While Schuch and Grange (2019) focused on a different research question (investigating aftereffects of N-2 repetition costs; not relevant for the present context), the data can be summarized as an assessment of N-2 repetition costs in four different experimental conditions. In particular, ABA and CBA trials were obtained in the experimental conditions I, II, III, and IV (condition I: short task-preparation interval and task sequence preceded by another ABA sequence; condition II: short task-preparation interval and task sequence preceded by another CBA sequence; condition III: long task-preparation interval and task sequence preceded by another ABA sequence; condition IV: long task-preparation interval and task sequence preceded by another CBA sequence). All independent variables were manipulated within-subjects, meaning that for each subject, four different N-2 repetition costs (calculated as the difference score of ABA minus CBA) can be computed (one for each experimental condition I, II, III, and IV). From here we refer to this as the "difference score". We took the diffusion modelling results from Schuch and Grange (2019), and correlated the difference score in boundary separation parameter with the difference score in non-decision time across participants, separately for each condition I, II, III, and IV.

The DDM analysis in the Schuch and Grange (2019) study was conducted with the software "fast-dm-30" (Voss et al., 2015). The parameters drift rate (v), boundary separation (a), non-decision time (t0), and trial-by-trial variability of non-decision time (st0) were estimated separately for each individual and each condition. The starting point bias was set to 0.5a (i.e., in the middle between the two boundaries). The lower and upper boundaries were set to reflect correct and wrong responses, respectively. All other parameters implemented in fast-dm were set to 0. The Kolmogorov–Smirnov (KS) statistic was used for fitting.

From here onwards, we use the labels v, a, and $t\theta$ to refer to the three main diffusion model parameters drift rate, boundary separation, and non-decision time respectively, and we use the terms v-difference, a-difference, and $t\theta$ -difference, to refer to the parameter difference scores between two within-subject conditions.

Experiment 1 from Schuch and Grange (2019)

In Experiment 1 from Schuch and Grange (2019) with N = 32, and about 100 trials per condition and participant (mean = 102, SD = 10, min. = 53, max. = 121), the correlation between the *a*-difference and the *t0*-difference was r = -.767, r = -.706, r = -.701, and r = -.565, in conditions I, II, III, and IV, respectively (see Table 1). These correlations are visualised in Figure 2. At the same time, the *a*-difference was correlated moderately positive with the *v*-difference (r = .398, r = .355, r = .543, r = .327, in conditions I, II, III, and IV);

correlations between t0-difference and v-difference were weak or close to zero (r = -.063, r = .182, r = -.078, r = .298 in conditions I, II, III, and IV, respectively).

Table 1. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 from Schuch & Grange (2019), Experiment 1. easy: CBA condition; hard: ABA condition; diff: hard-minus-easy difference in the corresponding parameter; conditions I-IV: different experimental conditions; see main text for details

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	I: 0.725	_							
	II: 0.803								
	III: 0.723 IV: 0.843								
	14. 0.043								
v (easy)	I: -0.427	I: -0.551	_						
	II: -0.362	II: -0.501							
	III: -0.575 IV: -0.711	III: -0.531 IV: -0.691							
v (hard)	I: -0.603	I: -0.496	I: 0.705	_					
	II: -0.580 III: -0.652	II: -0.531 III: -0.343	II: 0.666 III: 0.782						
	IV: -0.727	IV: -0.616	IV: 0.885						
t0 (easy)	I: -0.084	I: 0.127	I: -0.187	I: -0.080	_				
	II: -0.161	II: -0.034	II: -0.137	II: 0.178					
	III: 0.050 IV: 0.154	III: 0.357 IV: 0.250	III: -0.116 IV: -0.174	III: -0.138 IV: -0.189					
	14. 0.134	IV. 0.230	1V0.1/4	170.109					
t0 (hard)	I: 0.039	I: -0.109	I: -0.174	I: -0.118	I: 0.803	_			
	II: -0.118	II: -0.223	II: -0.149	II: 0.204	II: 0.865				
	III: 0.048 IV: 0.167	III: 0.111 IV: 0.134	III: -0.130 IV: -0.201	III: -0.182 IV: -0.148	III: 0.857 IV: 0.910				
	17. 0.107	17.0.131	17. 0.201	17. 0.110	17. 0.510				
a diff	I: -0.196	I: 0.532	I: -0.259	I: 0.035	I: 0.285	I: -0.204	_		
	II: -0.208	II: 0.416	II: -0.270	II: 0.015	II: 0.191	II: -0.186			
	III: -0.056 IV: -0.106	III: 0.650 IV: 0.446	III: -0.135 IV: -0.093	III: 0.222 IV: 0.071	III: -0.461 IV: 0.206	III: 0.107 IV: -0.031			
	170.100	17. 0.440	170.093	1V. 0.071	IV. 0.200	170.031			
v diff	I: 0.028	I: 0.304	I: -0.737	I: -0.041	I: 0.187	I: 0.134	I: 0.398	_	
	II: -0.241	II: -0.008	II: -0.453	II: 0.363	II: 0.384	II: 0.430	II: 0.355		
	III: -0.157	III: 0.256	III: -0.270	III: 0.389	III: -0.041	III: -0.089	III: 0.543		
	IV: 0.193	IV: 0.351	IV: -0.522	IV: -0.064	IV: 0.028	IV: 0.160	IV: 0.327		
t0 diff	I: 0.192	I: -0.373	I: -0.004	I: -0.072	I: -0.191	I: 0.431	I: -0.767	I: -0.063	_
to uni	II: 0.048	II: -0.385	II: -0.057	II: 0.093	II: -0.035	II: 0.471	II: -0.706	II: 0.182	
	III: -0.011	III: -0.494	III: -0.004	III: -0.054	III: -0.422	III: 0.106	III: -0.701	III: -0.078	
	IV: 0.015	IV: -0.292	IV: -0.043	IV: 0.112	IV: -0.308	IV: 0.115	IV: -0.565	IV: 0.298	

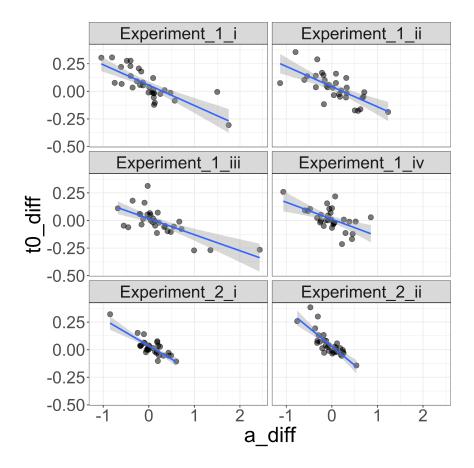


Figure 2. Plots of the correlation between a_difference and $t\theta$ _difference from all conditions across Experiments 1 and 2 from the Schuch and Grange (2019). Points represent individual participant difference scores in diffusion model parameters and the lines represent a linear model (with shading denoting 95% confidence intervals around the linear model predictions).

Experiment 2 from Schuch and Grange (2019)

Experiment 2 from Schuch and Grange (2019) with N = 32 new participants was similar to Experiment 1, but involved a larger number of trials. In Experiment 2, a task-preparation interval of intermediate length was used in three out of four trials; only in every fourth trial, the task-preparation interval was long or short. When analyzing the trials with intermediate task-preparation interval, a larger number of trials per condition was available (Mean = 285, SD = 35, min. = 186, max. = 346). For these trials, there were only two experimental conditions (condition I: task sequence preceded by another ABA sequence;

condition II: task sequence preceded by another CBA sequence). Again, there was a pronounced negative correlation between a-difference and $t\theta$ -difference, which amounted to r = -.81 in both experimental conditions (see Table 2, again visualised in Figure 2). At the same time, there were no strong correlations between a-difference and v-difference (r = .15 and r = .03 in conditions I and II, respectively) or between $t\theta$ -difference and v-difference (r = .16 and r = .41 in conditions I and II).

We also observed the negative correlation between *a*-difference and *t0*-difference in another empirical data set (task-switching paradigm; unpublished data); there we checked whether this correlation depends on particularities of the diffusion-model settings. We still observed the correlation when using the maximum-likelihood (ML) instead of the KS criterion for the fitting procedure, and when allowing *st0* to vary across conditions versus fixing it across experimental conditions (both changes were inspired by the diffusion-modelling procedure reported in Janczyk & Lerche, 2018). We observed the spurious correlation in all four combinations of fitting criterion (ML versus KS) and *st0* setting (variable versus fixed across conditions); moreover, when using the EZ-diffusion model (Wagenmakers, van der Maas, & Grasman, 2007) instead of *fast-dm*, we again obtained similar results.

To summarize, we consistently observed a pronounced negative correlation between a-difference and $t\theta$ -difference when applying a simple drift-diffusion model to empirical task-switching data. The correlation occurred in different experimental conditions, and with different diffusion-model settings.

Table 2. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 from Schuch & Grange (2019), Experiment 2, trials with intermediate CSI. easy: CBA condition; hard: ABA condition; diff: hard-minus-easy difference in the corresponding parameter; conditions I-II: different experimental conditions; see main text for details

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	I: 0.846 II: 0.846	_							
v (easy)	I: -0.530 II: -0.410	I: -0.587 II: 0.372	_						
v (hard)	I: -0.446 II: -0.261	I: -0.501 II: -0.200	I: 0.912 II: 0.835	_					
t0 (easy)	I: -0.098 II: -0.223	I: -0.122 II: -0.310	I: 0.044 II: 0.055	I: -0.018 II: -0.012	_				
t0 (hard)	I: 0.007 II: -0.117	I: -0.233 II: -0.185	I: -0.008 II: -0.071	I: -0.014 II: 0.005	I: 0.883 II: 0.836	_			
a diff	I: 0.020 II: -0.429	I: 0.551 II: 0.119	I: -0.271 II: 0.132	I: -0.240 II: 0.147	I: -0.075 II: -0.108	I: -0.447 II: 0.531	_		
v diff	I: 0.348 II: 0.262	I: 0.372 II: 0.303	I: -0.510 II: -0.296	I: -0.112 II: 0.278	I: -0.145 II: -0.116	I: -0.049 II: 0.133	I: 0.153 II: 0.026	_	
t0 diff	I: 0.193 II: 0.534	I: -0.273 II: 0.110	I: -0.063 II: -0.209	I: 0.003 II: 0.026	I: 0.060 II: 0.079	I: 0.522 II: 0.613	I: -0.813 II: -0.808	I: 0.159 II: 0.409	_

Reanalysis of Dutilh et al. (2019)

To check for the generality of this finding, in a next step we reanalysed an empirical data set collected independently from our own research groups. We selected the data set of Dutilh et al. (2019), which was utilised in a "many-analysts" examination of the variability of model-based inferences of two-choice RT data. Dutilh et al. created 14 data sets; each data set comprised two conditions, and in most data sets some aspect of participants' behaviour was manipulated to selectively induce changes in model parameters across two conditions

("Condition A" and "Condition B"). The primary task in all experiments was a random dot motion task where a cloud of dots were presented to participants; a proportion of the dots moved in a consistent direction, and the remainder moved in a random direction. The task required participants to judge the direction of the coherently moving dots.

Of the 14 data sets, we reanalysed three; these were selected as either no DDM parameter was expected to change across conditions (i.e., data set from Experiment 1), or only one parameter was expected to change across conditions (i.e., data sets from Experiments 2 & 3). In the data set from Experiment 1, there were no experimental differences between the two conditions, and therefore there should be no differences in DDM parameters across conditions. Therefore, the labelling of "Condition A" and "Condition B" is somewhat arbitrary in this Experiment, but it does allow us to explore whether the spurious correlation is present in a data set with no condition-differences in model parameters. The data comprising Experiment 2 was obtained via a manipulation of task difficulty between Conditions A and B; specifically, the proportion of coherently moving dots in the cloud presented on each trial was 20% in Condition A, and 10% in Condition B; Condition B can thus be considered a "hard" condition, and Condition A a (relatively) "easy" condition. The data comprising Experiment 3 was obtained via a manipulation of response caution between Conditions A and B; specifically, in Condition A participants were instructed to respond with an emphasis on *speed*, and to respond with an emphasis on *accuracy* in Condition B. This speed–accuracy manipulation influences the response boundary parameter typically in drift-diffusion modelling (see e.g., Heitz, 2014).

The data for each experiment—and for each condition within each experiment—was extracted as described in Dutilh et al. (2019) and fit with *fast-dm-30* using maximum likelihood criterion with v, a, and $t\theta$ free to vary across conditions A and B. The model was

fit to each experiment separately. The correlation coefficients among all parameters is shown in Table 3.

The negative correlation between a-difference and $t\theta$ -difference was very large in Experiment 1 (r = -.964) and Experiment 2 (r = -.899), but was absent in Experiment 3 (r = .056). At the same time, the a-difference was correlated moderately positively with the v-difference in Experiment 1 (r = .299), but this correlation was moderate and negative in Experiments 2 (r = -.315) and 3 (r = -.216); the correlation between $t\theta$ -difference and v-difference was small and negative in Experiment 1 (r = -.173), but was moderate and positive in Experiments 2 (r = 0.435) and 3 (r = 0.379).

To summarise the reanalysis of Dutilh et al. (2019), we found the spurious correlation between a-difference and t0-difference in two of the three data sets. Surprisingly, we did not find the correlation in Experiment 3. In that experiment, response caution was manipulated via speed–accuracy emphasis instructions; such instructions have been shown to selectively influence estimates of boundary separation in drift-diffusion model fitting (e.g., Forstmann et al., 2011; Heitz, 2014; but see Rae et al., 2014). This raises an interesting possibility that the spurious correlation observed between a-difference and t0-difference only occurs when the experimental manipulations do not affect the boundary separation parameter. We explore this question—among others—in a set of simulations studies.

Table 3. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 from Dutilh et al. (2019) Experiments 1–3 (conditions A and B). diff = difference score for model parameters calculated as condition B minus condition A. See main text for details

	a (A)	a (B)	v (A)	v (B)	t0 (A)	t0 (B)	a diff	v diff	t0 diff
a (A)	_								
a (B)	1: 0.327 2: 0.269 3: -0.177	_							
v (A)	1: 0.090 2: -0.125 3: 0.172	I: -0.247 2: 0.286 3: -0.072	_						
v (B)	1: 0.021 2: -0.167 3: 0.332	1: -0.161 2: 0.231 3: -0.267	1: 0.907 2: 0.966 3: 0.689	_					
t0 (A)	1: -0.483 2: -0.406 3: -0.324	1: -0.091 2: -0.008 3: 0.089	1: 0.549 2: 0.673 3: 0.422	1: 0.568 2: 0.708 3: -0.050	_				
t0 (B)	1: 0.085 2: 0.100 3: -0.362	1: -0.358 2: -0.374 3: 0.096	1: 0.712 2: 0.311 3: 0.005	1: 0.673 2: 0.386 3: -0.182	1: 0.702 2: 0.675 3: 0.572	_			
a diff	1: -0.749 2: -0.642 3: -0.510	1: 0.381 2: 0.566 3: 0.937	1: -0.261 2: 0.335 3: -0.124	1: -0.133 2: 0.327 3: -0.351	1: 0.408 2: 0.341 3: 0.193	1: -0.335 2: -0.383 3: 0.212	_		
v diff	1: -0.161 2: 0.065 3: 0.130	1: 0.202 2: -0.326 3: -0.190	1: -0.231 2: -0.952 3: -0.606	1: 0.201 2: -0.840 3: 0.160	1: 0.035 2: -0.572 3: -0.629	1: -0.100 2: 0.197 3: -0.206	1: 0.299 2: -0.315 3: -0.216	_	
t0 diff	1: 0.747 2: 0.616 3: -0.101	1: -0.332 2: -0.467 3: 0.023	1: 0.174 2: -0.410 3: -0.408	1: 0.100 2: -0.358 3: -0.161	1: -0.435 2: -0.338 3: -0.319	1: 0.335 2: 0.466 3: 0.595	1: -0.964 2: -0.899 3: 0.056	1: -0.173 2: 0.435 3: 0.379	_

Simulation Studies

In this section, we conducted a series of simulations to explore the correlation between a-difference and t0-difference. We were primarily interested in understanding whether the observed correlation was peculiar to the empirical data sets investigated above or whether it was a general result that might be found in other situations. Simulations are

important to explore such questions as we are able to generate synthetic data where the values for the true data-generating parameters are known, which is not possible with real data.

Simulation 1: No Difference in Parameters

In Simulation 1, we wanted to explore whether we would observe the correlation between *a*-difference and *t0*-difference in a data set where no true difference exists in any of the main DDM parameters between two experimental conditions. This provides a strong test of whether the observed correlation is an artefact of real behavioural data or whether it is an emergent and general property of DDM model fits: If we observe a correlation between *a*-difference and *t0*-difference in the absence of a true difference in parameter values between conditions then the correlation must be a general property of DDM fitting. This simulation is thus similar in design to Experiment 1 from Dutilh et al. (2019), where there was no experimental manipulation of participant behaviour between the two experimental conditions.

We conducted a simulation where data were generated from 1,000 artificial participants in two experimental conditions; we refer to these as an "easy" condition and a "hard" condition throughout, even though in this particular simulation no differences in parameters existed. For each participant, 1,000 trials were simulated in each condition; such large trial numbers have been shown to lead to excellent parameter recovery (see Lerche et al., 2017) and as such noise in the parameter estimation routine is minimised. In Simulation 1, the diffusion parameters used to generate the data were randomly selected for each participant, but importantly the exact same parameters were used for each participant to generate data in both the easy and the hard condition. Specifically, parameters for each participant in the easy condition were sampled from a uniform distribution with the following minimum and maximum values: v [0.0–4.0], a [0.5–2.0], and t0 [0.2–0.5] (see Lerche et al., 2017, for similar values); the exact same parameters for the easy condition were then used for

the hard condition. Throughout all simulations reported in this paper, we fixed the starting point of the diffusion process equidistant between response boundaries (i.e., parameter zr was set to 0.5), and all variability parameters were set to zero. Data were simulated using the *fast-dm-30* software (Voss et al., 2015) using the *construct-samples* routine with precision set to 3^1 . The simulated behavioural data showed similar response times in the easy condition (M = 0.625 s, SD = 0.206 s) and the hard condition (M = 0.626 s, SD = 0.207 s), and the accuracy was identical in both conditions (M = 84.6%, SD = 14.4%).

The diffusion model was then fit to the simulated behavioural data. During fitting, only the three main parameters—v, a, and t0—were allowed to freely vary across conditions. The starting point parameter zr was fixed at 0.5, and all variability parameters were fixed at zero². Maximum likelihood was used as the optimisation criterion throughout all simulations. Recovery of the generating parameter values used to generate simulated data was excellent in the fitting routine. The correlation between the parameter values used to generate simulated data and the recovered best-fitting parameter values were all above r = .995 (see Appendix A).

The fit routine returned the set of best-fitting parameters per participant, namely v (easy), v (hard), a (easy), a (hard), $t\theta$ (easy), and $t\theta$ (hard). We then calculated difference scores on each parameter, calculated as the estimate for the easy condition subtracted from the estimate for the hard condition, namely v-difference, a-difference, and $t\theta$ -difference. We then computed the product-moment correlation coefficient matrix across all of the parameters. Due to the large participant numbers in the simulation, we did not calculate statistical significance. Instead, we interpret the correlation coefficient as an effect size, and

¹ Precision values control the accuracy of the calculated density functions in *fast-dm-30*. Higher values lead to higher accuracy of prediction, but leads to slower simulation time. Voss et al. (2015) recommend setting *precision* to values between 2.0–5.0.

Usually, trial-to-trial variability in non-decision time (implemented in *fast-dm-30* via the st0 parameter) is not fixed to zero to account for very rapid responses often present in real data sets (Voss et al., 2015). We repeated Simulation 1 with st0 allowed to be a free parameter during the model fitting, and found qualitatively identical results to those reported in the text body. In all simulations were therefore fixed st0 to zero, which also has the benefit of reducing simulation time.

use r = |0.1| to denote a small effect, r = |0.3| to denote a medium effect, and r >= |0.5| to denote a large effect. The correlation matrix is shown in Table 4.

Table 4. Product-moment correlation coefficients between the fitted parameters from the fast-dm-30 fitting routine in Simulation 1. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.991	_							
v (easy)	0.043	0.039	_						
v (hard)	0.009	0.042	0.994	_					
t0 (easy)	-0.045	-0.041	-0.001	-0.001	_				
t0 (hard)	-0.049	-0.052	0.005	0.003	0.998	_			
a diff	-0.020	0.117	-0.026	0.025	0.027	-0.022	_		
v diff	-0.038	0.027	-0.072	0.036	-0.002	-0.017	0.473	_	
t0 diff	-0.056	-0.158	0.080	0.057	-0.023	0.043	-0.743	-0.215	

As can be seen, we found a large negative correlation (r = -.743) between the difference score in boundary separation (a-difference) and the difference score in non-decision time (t0-difference), replicating the finding in the Schuch and Grange (2019) data set, as well as Experiments 1 and 2 from the reanalysis of Dutilh et al. (2019). This correlation was present despite there being no correlation between the boundary separation parameter and the non-decision time parameter for either the easy or the hard conditions. Aside from the expected large correlations between matching parameters across conditions (e.g., v[easy] and v[hard]), no other correlations were above medium in effect size. Within the difference scores, we observed a medium positive correlation between a-difference and v-difference which we also observed in the reanalysis of Experiment 1 of Schuch and Grange (2019), and in Experiment 1 of the reanalysis of Dutilh et al. (2019). In addition, there was a

small negative correlation between ν -difference and $t\theta$ -difference, which we did not observe consistently in the real data sets.

To check that the observed correlations were not due to the model estimation programme used, we fitted the EZ-diffusion model (Wagenmakers, van der Maas, & Grasman, 2007) to the behavioural data generated by the simulation³. The correlation matrix for this fitting routine is shown in Table 5, and shows qualitatively similar results, and in particular the correlation between a-difference and $t\theta$ -difference remained large and negative. Note, though, that the correlation between a-difference and v-difference—whilst still positive—reduced in size to a small effect. The small negative correlation between v-difference and $t\theta$ -difference was absent in the EZ model fit.

Table 5. Product-moment correlation coefficients between the fitted parameters from the EZ-diffusion fitting routine in Simulation 1. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.978	_							
v (easy)	0.033	0.040	_						
v (hard)	0.033	0.047	0.993	_					
t0 (easy)	-0.062	-0.039	0.008	0.005	_				
t0 (hard)	-0.057	-0.067	-0.003	-0.004	0.974	_			
a diff	-0.015	0.192	0.037	0.070	0.104	-0.053	_		
v diff	-0.003	0.053	-0.070	0.050	-0.024	-0.012	0.273	_	
t0 diff	0.024	-0.118	-0.046	-0.039	-0.174	0.055	-0.683	0.053	_

⁻

³ As the EZ diffusion model is a closed-form solution where the main DDM parameters are calculated from mean RT, RT variance, and percentage accuracy, edge corrections are required when accuracy is at 100%, 50%, or 0%. We used the same correction as reported by Lerche et al. (2017): When accuracy was 100%, we set accuracy equal to 100 - 100 / (2n), where n is the number of trials used in the simulation (here n = 1000); when accuracy was 50%, it was corrected to 50 + 100 / (2n), and to 100 / (2n) when accuracy was 0%.

Simulation 2: Introducing Differences in Each Main Parameter

Although Simulation 1 provides a strong test of the correlation between a-difference and t0-difference due to no true parameter difference between conditions, it does present a somewhat unrealistic representation of the type of real data analysts are likely to use the diffusion model for, where some experimental manipulation is known to lead to differences between conditions. In Simulation 2 we therefore explored the impact of a true condition difference on the observed negative correlation between a-difference and t0-difference. We conducted a series of simulations wherein we systematically generated artificial data where just one parameter changed between easy and hard conditions, whilst the other parameters remained fixed. We repeated the simulations to generate data that exhibited a small (Cohen's d = 0.3), medium (d = 0.5), and large (d = 0.8) effect size. This allows us to explore the impact of selectively changing just one parameter between two conditions on the correlation between a-difference and t0-difference. After this, we then explored the effect of changing all parameters between conditions.

Changing One Main DDM Parameter Between Conditions

The values for the manipulated parameter for simulated participants were sampled from a multivariate normal distribution (with the constraint that all parameters should be positive values) with means and standard deviations that allowed the various effect sizes of interest. For example, when the drift rate was manipulated to have a small effect size across conditions, the parameter values for drift rate were sampled from a multivariate normal distribution with means M(easy) = 2.3, M(difficult) = 2.0, and standard deviations SD(easy) = 1, SD(hard) = 1, constrained to have a correlation r = 0.5 between the two parameters at the population level. The other parameters were selected as in Simulation 1 by sampling parameters for the easy condition from a uniform distribution, and using the exact same

parameters in the hard condition (see Table 6 for full parameter-generating details). These parameter values were then used to simulate data using the *construct-samples* routine in *fast-dm-30*.

We generated parameter values for 1,000 artificial participants in each factorial combination of manipulated parameter and effect size. For each combination of manipulated parameter and effect size, 1,000 trials were simulated per condition per participant. The diffusion model was then fitted to the simulated data in the same way as in Simulation 1.

Table 6. Parameter sampling values used to generate simulated data in Simulation 2. Each row represents a separate sub-simulation, wherein one key parameter was manipulated to have either a small, medium, or large effect across easy and hard conditions.

	v (easy)	v (hard)	a (easy)	a (hard)	t0 (easy)	tθ (hard)
Sub- Simulation						
v (small effect)	$\mu=2.3,\sigma=1$	$\mu = 2.0, \sigma = 1$	unif[0.5-2.0]	= a (easy)	unif[0.2-0.5]	= <i>t0</i> (easy)
v (medium effect)	$\mu=2.5,\sigma=1$	$\mu=2.0,\sigma=1$	unif[0.5-2.0]	= a (easy)	unif[0.2-0.5]	= t0 (easy)
v (large effect)	$\mu=2.8,\sigma=1$	$\mu=2.0,\sigma=1$	unif[0.5-2.0]	= a (easy)	unif[0.2-0.5]	= t0 (easy)
a (small effect)	unif[0.0-4.0]	=v (easy)	$\mu = 1.25$, $\sigma = 0.4$	$\mu=1.37,\sigma=0.4$	unif[0.2-0.5]	= t0 (easy)
a (medium effect)	unif[0.0-4.0]	=v (easy)	$\mu = 1.25$, $\sigma = 0.4$	$\mu=1.45,\sigma=0.4$	unif[0.2-0.5]	$= t\theta$ (easy)
a (large effect)	unif[0.0-4.0]	=v (easy)	$\mu=1.25,\sigma=0.4$	$\mu=1.57,\sigma=0.4$	unif[0.2-0.5]	= t0 (easy)
t0 (small effect)	unif[0.0-4.0]	=v (easy)	unif[0.5-2.0]	= a (easy)	$\mu=0.350,\sigma=0.1$	$\mu=0.385,\sigma=0.1$
t0 (medium effect)	unif[0.0-4.0]	=v (easy)	unif[0.5-2.0]	= a (easy)	$\mu=0.350,\sigma=0.1$	$\mu = 0.400, \sigma = 0.1$
t0 (large effect)	unif[0.0-4.0]	=v (easy)	unif[0.5-2.0]	= a (easy)	$\mu=0.350,\sigma=0.1$	$\mu=0.430,\sigma=0.1$

Note. Where a parameter is manipulated between conditions, μ and σ provide the mean and standard deviation (respectively) for each condition used to draw samples from a multivariate normal distribution with correlation ρ =0.5 between the manipulated parameters. = signifies identical parameters were used to the named column (e.g., = $t\theta$ (easy) means the parameters were identical to those in the $t\theta$ (easy) column. μ = mean of the condition. σ = standard deviation of the condition. Unif refers to a uniform distribution with the range of possible values shown in square brackets.

The results of the simulations are visualised in Figure 3, which shows heat-maps of the correlation matrices for each of the nine combinations of which parameter was manipulated, and to what effect size. The correlation matrices are presented numerically in

Appendix B, together with the numerical correlation matrices resulting from fitting the simulated data with the EZ-diffusion model.

The results showed quite strikingly that the effects of which parameter was manipulated produced remarkably consistent outcomes across all effect sizes (that is, the pattern of correlations in each column is consistent across each effect size magnitude).

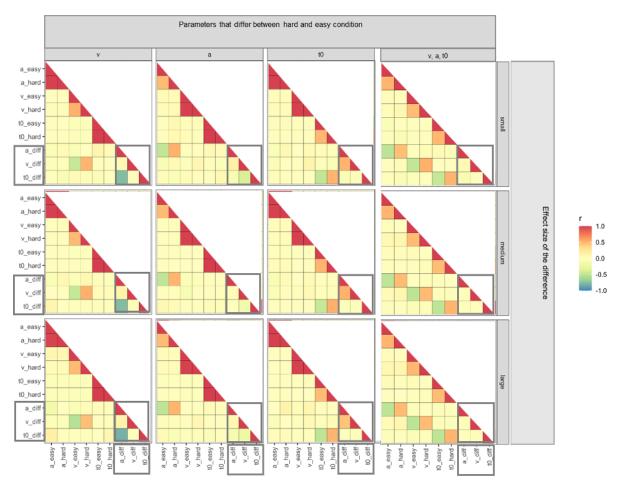


Figure 3. Heatmaps of the product-moment correlation matrices from Simulation 2 where one DDM parameter was changed across conditions, and Simulation 3 where all three parameters were changed across conditions. Columns represent which parameters were manipulated to be different between simulated conditions, and rows represent the effect size of the manipulated difference in those parameters. Diff = difference score. Correlations between difference scores are highlighted by grey rectangles

The negative correlation between a-difference and t0-difference was only present when drift rate was varied across conditions (Column 1 of Figure 3), but not when boundary

separation or non-decision time, or all three parameters, were varied across conditions (Columns 2-4 of Figure 3). The negative correlation between a-difference and t0-difference was large across each manipulated effect size of the drift rate effect (r = -.774 when d was small, r = -.769 when d was medium, and r = -.819 when d was large). These correlations are visualised in Figure 4.

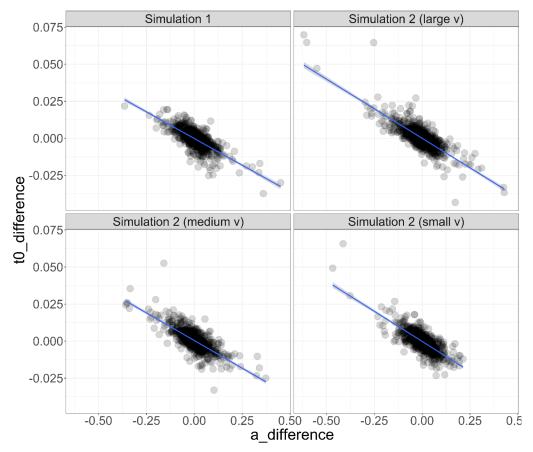


Figure 4. Plots of the correlation between a-difference and $t\theta$ -difference in Simulation 1, and Simulation 2 (with drift rate, v, manipulated to have a small, medium, and large difference across conditions). Points represent simulated participants' difference scores in diffusion model parameters, and the lines represent a linear model (with shading—barely visible—denoting 95% confidence intervals around the linear model predictions).

These correlations were not driven by outlier scores. We assessed the impact of outliers by standardising the data and removing any simulated participant with standardised scores lower than -2.5 or higher than 2.5. The correlations remained negative: rs = -.661,

-.693, -.688, -.705 for Simulation 1, Simulation 2 (small v), Simulation 2 (medium v), and Simulation 2 (large v) respectively.

When t0 was manipulated, we found a moderate positive correlation between a-difference and v-difference, which ranged from r = .455-.521. These correlations were present in Experiment 1 of Schuch and Grange (2019; ranging from r = .33 to .54) and in Experiment 1 of Dutilh et al. (2019; r = .30); this correlation was absent from the reanalysis of Experiment 2 of Schuch and Grange, but was medium and negative in Experiments 2 and 3 of Dutilh et al. (rs = -.32 and -.22, respectively). Similar to the correlation between *a*-difference and *t0*-difference, these correlations were not driven by outlier scores. When we standardised the scores and removed any simulated participant with standardised scores lower than -2.5 or higher than 2.5, the correlations were rs = .350, .389, .355, .328 for Simulation 1, Simulation 2 (small v), Simulation 2 (medium v), and Simulation 2 (large v) respectively.

No other correlations were consistently found between difference parameters. Note that although there was a medium negative correlation between v-difference and $t\theta$ -difference when boundary separation was manipulated to a small effect size, this did not replicate at other effect-size manipulations, nor was it present in the EZ-diffusion fitting.

The only other correlations present are to be expected from the design of the simulations. Namely, when a parameter was not manipulated between conditions, a large positive correlation was found between its fitted estimate in easy- and hard-conditions. When a parameter was manipulated, the fitted estimate for the easy condition was moderately positively correlated with the hard condition (because the data were generated to have an r = .5 correlation). In addition, when a parameter was manipulated, the estimates of that parameter for the easy- and the hard-condition were correlated with the magnitude of the difference score in that parameter (negatively for the easy-condition parameter, and positively for the hard-condition parameter). This latter pattern was found for the drift rate parameter in

the reanalysis of Schuch and Grange (2019): v-difference was consistently negatively correlated with the v estimate in the easy conditions (ranging from r = -.27 to r = -.74), and in some conditions positively correlated with the v estimate in the hard condition (range r = -0.11 to r = 0.39). In the reanalysis of Dutilh et al. (2019), v-difference was negatively correlated with the v-estimate in Condition A (notionally the "easy" condition; range r = -0.23 to -0.95), but was only positively correlated with the v-estimate in Condition B in Experiments 1 and 3 (rs = 0.20 & 0.16, respectively); in Experiment 2 (where drift rate was manipulated behaviourally), the correlation was large and negative (r = -.84).

Changing All Main DDM Parameters Between Conditions

In the next part of the simulation, we simulated data where all three main parameters changed between conditions, again manipulating the size of the changes to be small, medium, and large. The parameters were generated as presented in Table 7, except all three parameters changed across conditions. Again, 1,000 participants were simulated with 1,000 trials per condition. The results of the simulation are shown in Figure 3, most-right column (numerical correlation matrices and EZ-diffusion results are in Appendix B). The results showed only the expected correlations dictated by the simulation design; the negative correlation between *a*-difference and *t0*-difference was not found.

Discussion

Taken together, the results of Simulation 1 and Simulation 2 show that the negative correlation between *a*-difference and *t0*-difference found in the reanalysis of Schuch and Grange (2019) and in Experiments 1 and 2 from Dutilh et al. (2019) appears when there is either no true difference in parameter values across conditions (e.g., Experiment 1 in Dutilh et al., 2019), or the true difference is localised to the drift rate parameter (e.g., Experiments 1

& 2 from Schuch & Grange, 2019, and Experiment 2 from Dutilh et al., 2019). This conclusion is congruent with us not finding the correlation in the reanalysis of Experiment 3 from Dutilh et al. (2019), where the experiment's speed–accuracy tradeoff likely influenced the boundary separation parameter between conditions. In other words, the spurious correlation between a-difference and $t\theta$ -difference emerges whenever there is no true difference in the a and t0 parameters across conditions, irrespective of whether there is a true condition difference in drift rate or not.

Simulation 3: Using rtdists Package

In Simulations 1 and 2, we simulated and fitted the diffusion model using the fast-dm-30 software provided by Voss et al. (2015). We wanted to assure ourselves that the observed negative correlation between a-difference and t0-difference was not due to the use of this software. Therefore, in Simulation 3 we utilised different simulation and fitting software. Specifically, we used the R package rtdists (Singmann, Brown, Gretton, & Heathcote, 2020)⁴ and repeated Simulation 1, where data are simulated with no true difference in parameters across conditions (again using the parameter generation criteria in Table 6). The results of the simulation are shown in the correlation matrix in Table 7.

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⁴ Note that although the rtdists package implements the drift diffusion model in R, it is based on C code underlying the fast-dm-30 software. As the purpose of Simulation 3 was to make sure our results in Simulation 1 and Simulation 2 were not due to peculiarities in the simulation and/or fitting algorithms in fast-dm-30, it might therefore seem problematic to use *rtdists*. However, the code for *rtdists* has been adapted to C++ by Singmann et al. (2020), which then is called by functions written in R. Thus we consider this to be an independent implementation of the drift diffusion model, and is therefore suitable for our purposes.

Table 7. Product-moment correlation coefficients between the fitted parameters from the rtdists fitting routine in Simulation 3. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.991	_							
v (easy)	0.045	0.035	_						
v (hard)	0.050	0.048	0.994	_					
t0 (easy)	-0.051	-0.048	-0.006	-0.004	_				
t0 (hard)	-0.044	-0.048	-0.002	-0.003	0.998	_			
a diff	-0.126	0.011	-0.076	-0.019	0.024	-0.024	_		
v diff	0.043	0.115	-0.099	0.013	0.011	-0.004	0.513	_	
t0 diff	0.098	-0.004	0.052	0.026	-0.009	0.056	-0.741	-0.240	

Replicating Simulation 1, we found a large negative correlation between a-difference and t0-difference. Similar to Simulation 1, the positive correlation between a-difference and v-difference—this time with a large effect size—re-emerged, as did the small negative correlation between v-difference and t0-difference.

The finding of a large negative correlation between *a*-difference and *t0*-difference appears robust across simulation and fitting procedures. As also found in our behavioural data, we found in Simulation 1 a small positive correlation between *a*-difference and *v*-difference; although this was not replicated in the EZ-diffusion fit of the Simulation 1 dataset, the correlation has replicated using the *rtdists* package here in Simulation 3. In addition, Simulation 3 replicated the small negative correlation between *v*-difference and *t0*-difference, again generally consistent with our behavioural data reanalysis. Taken together, the findings of Simulation 3 broadly support the findings of Simulation 1: When no true differences exist in diffusion model parameters between experimental conditions, spurious correlations appear in all of the difference scores of the parameter values.

Simulation 4: Linear Ballistic Accumulator Model

In Simulation 3, we utilised a different simulation and model fitting environment to ensure our findings generalise across different implementations of the drift diffusion model. In Simulation 4, we addressed whether the findings generalise to different theoretical accounts of evidence accumulation during rapid decision making. In particular, we simulated data from the Linear Ballistic Accumulator (LBA) model (Brown & Heathcote, 2008), and fitted the generated data with the LBA model.

The LBA model is similar to the DDM in that it decomposes response times into a decisional and non-decisional component. The decisional component of the LBA assumes—like the DDM—that responses are determined by an evidence accumulation process (see Figure 5 for a schematic overview of the LBA model). However, the LBA assumes that the evidence accumulation process is linear, with the rate of evidence accumulation determined by the drift rate. The drift rate varies on each trial (modelled as a draw from a random distribution with mean v and standard deviation s), which models trial-wise variability in response time. The LBA assumes separate accumulators for each response option (cf., the DDM which assumes a single accumulator can hit one of two response boundaries; see Figure 1), which in our simulations we generalise to include one accumulator for the "correct" response (with mean drift rate v) and one accumulator for the incorrect response (with mean drift rate 1-v). Each accumulator begins each trial with a certain amount of residual evidence, represented by a random starting point of the drift rate between 0-A, where A is a parameter that represents the height of the starting point boundary. A response is selected when an accumulator reaches the threshold (the height of which is represented by parameter b, which is constrained to be larger than A); RT is determined by the time taken for the first accumulator to reach the threshold, and accuracy is determined by whether the accumulator representing the correct response option was the first to reach the

boundary or not. Response caution—equivalent to the boundary separation parameter a in the DDM—is given by b - (A/2). As with the standard diffusion model, the LBA model also has a parameter reflecting non-decisional components of performance (i.e., t0).

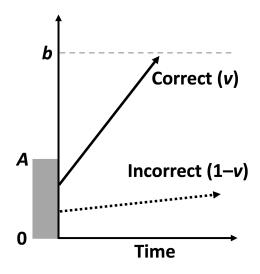


Figure 5. Schematic representation of trial processing in the Linear Ballistic Accumulator Model. Figure available at https://www.flickr.com/photos/150716232@N04/51602517573 under CC license https://creativecommons.org/licenses/by/2.0/.

We simulated 1,000 participants from the LBA model, with 1,000 trials per condition. As in Simulation 1, the parameters were identical for each participant in each condition. All LBA parameters were drawn from uniform distributions with the following minimum and maximum values: mean correct v [1.0–4.0], A [0.5–2.0], b [A + 0.001–2.0], and $t\theta$ [0.2–0.5]. The LBA model was then fitted to the generated data using a gradient descent method (as implemented in R's nlminb function) to find the best set of LBA parameters for each participant and each condition that minimises the negative log-likelihood of the data. Starting parameters for the search routine were generated for each participant and each condition using the following heuristics (see Donkin, Brown, & Heathcote, 2011): $t\theta$ was set at 90% of the fastest response in the data; mean correct drift rate v was set to 0.5 + $\Phi i^{-1}(p)$, where p is the probability of a correct response, and Φ is the normal cumulative distribution function

with mean equal to zero and standard deviation 0.3; A was set as twice the value of the inter-quartile range of all response times; and b was set to $A \times 1.25$.

After the fit routine had found the best-fitting parameters for each participant and each condition, we calculated response caution for each participant and condition (calculated as b–[A/2]) and calculated difference scores for all main parameters (the easy condition parameter value subtracted from the hard condition parameter value). The correlation matrix is shown in Table 8.

Table 8. Product-moment correlation coefficients between the fitted parameters from the LBA simulation and fitting routine in Simulation 4. Note that caution was calculated as b - (A/2). Diff = difference scores on parameters (hard minus easy).

	caution (easy)	caution (hard)	v (easy)	V (hard)	t0 (easy)	t0 (hard)	caution diff	v diff	t0 diff
caution (easy)	_								
caution (hard)	0.925	_							
v (easy)	0.082	0.07	_						
v (hard)	0.060	0.103	0.979	_					
t0 (easy)	-0.147	-0.039	-0.066	-0.052	_				
t0 (hard)	-0.063	-0.165	-0.084	-0.095	0.765	_			
caution diff	-0.156	0.231	-0.018	0.112	0.277	-0.267	_		
v diff	-0.105	0.141	-0.080	0.125	0.068	-0.057	0.635	_	
t0 diff	0.126	-0.181	-0.024	-0.061	-0.375	0.310	-0.793	-0.183	_

The results showed a replication of the large negative correlation between response caution-difference and t0-difference as found in Simulation 1, suggesting that our main finding is reproducible across different theoretical implementations of evidence accumulation models. In addition, we again found a (large) positive correlation between caution-difference and v-difference, and a (small) negative correlation between v-difference and t0-difference.

Simulation 5: True Correlated Difference Scores

So far the Simulations have examined cases where no true correlation exists between difference scores in the diffusion model parameters. We have shown under such circumstances, a spurious correlation emerges between the a-difference and $t\theta$ -difference parameters. In the current simulation, we examine the complement of this whereby we simulate artificial data where a true correlation exists between a-difference and $t\theta$ -difference parameters. The question we wished to address is whether the model fitting procedure is able to recover such a true correlation, or whether recovery is corrupted by whatever is causing the spurious correlations reported in previous simulations⁵.

Recovery of a True Negative Correlation

In the first simulation in this section, we explored recovery attempts from a simulated data set with a true population-level correlation of r = -.7 between the a-difference and t0-difference parameter values. We simulated data consisting of 1,000 trials for 1,000 artificial participants in two conditions ("easy" and "hard"). The method used to generate the parameters that would be used to simulate the data for each participant in the easy condition was the same as in Simulation 1. The method used to generate the parameters that would be used to simulate the data in the hard condition was as follows:

$$v_{
m hard} = v_{
m easy}$$
 $a_{
m hard} = a_{
m easy} + a_{
m diff}$ $t \theta_{
m hard} = t \theta_{
m easy} + t \theta_{
m diff}$

That is, the drift rate was identical for the easy and the hard condition. The boundary separation parameter in the hard condition was generated by taking the boundary separation parameter in the easy condition and adding a difference score to it (a_{diff}) . The non-decision

⁵ We are grateful to an anonymous reviewer for suggesting this simulation study.

time parameter in the hard condition was generated by taking the non-decision time parameter in the easy condition and adding a difference score to it ($t\theta_{\text{diff}}$). The difference scores a_{diff} and $t\theta_{\text{diff}}$ were sampled from a multivariate normal distribution with mean a_{diff} set to zero, SD a_{diff} set to 0.1, mean $t\theta_{\text{diff}}$ set to zero, and sd $t\theta_{\text{diff}}$ set to 0.05. The population correlation between a_{diff} and $t\theta_{\text{diff}}$ was set to r = -.7. Put another way, the population-level difference in boundary separation and non-decision time between the hard and the easy condition was zero, but there was a true correlation in difference scores between a_{diff} and $t\theta_{\text{diff}}$ of r = -.7. The parameter fitting routine was the same as in Simulation 1.

The results of the Simulation can be seen in Table 8. Critically, the "true" negative correlation between a_{diff} and $t\theta_{\text{diff}}$ was relatively well recovered (r = -.673).

Table 8. Product-moment correlation coefficients between the fitted parameters from the "true negative" correlation in Simulation 5. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.996	_							
v (easy)	0.007	-0.005	_						
v (hard)	0.003	-0.001	0.994	_					
t0 (easy)	0.006	0.020	-0.012	-0.011	_				
t0 (hard)	0.009	-0.072	0.031	0.028	0.848	_			
a diff	-0.023	0.237	-0.044	-0.017	0.052	-0.312	_		
v diff	-0.039	0.029	0.002	0.109	0.010	-0.027	0.256	_	
t0 diff	0.007	-0.168	0.077	0.069	-0.036	0.500	-0.673	-0.066	_

Recovery of a True Positive Correlation

In the next Simulation in this section, we repeated the previous Simulation but simulated data so that the true population-level correlation between a_{diff} and $t\theta_{\text{diff}}$ was set to .7. The results of this Simulation can be seen in Table 9. The "true" positive correlation between a_{diff} and $t\theta_{\text{diff}}$ was relatively well recovered (r = .521). Although there is some discrepancy

between the recovered correlation and the "true" generating correlation, this likely reflects sampling error and/or simulation noise.

In general, though, the results of Simulation 5 show that if a true correlation exists between a_{difference} and t0_{difference}, the model fitting procedures of the diffusion model are able to recover this correlation relatively well. Parameter recovery in situations with true correlations between difference scores is therefore not corrupted by whatever is causing the spurious correlations reported in previous simulations.

Table 9. Product-moment correlation coefficients between the fitted parameters from the "true positive" correlation in Simulation 5. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.969	_							
v (easy)	0.004	0.000	_						
v (hard)	-0.005	-0.003	0.994	_					
t0 (easy)	0.009	0.027	-0.006	-0.002	_				
t0 (hard)	0.004	0.084	0.015	0.015	0.868	_			
a diff	-0.036	0.211	-0.016	0.009	0.075	0.323	_		
v diff	-0.076	-0.021	-0.081	0.033	0.039	-0.003	0.216	_	
t0 diff	-0.006	0.122	0.041	0.033	0.006	0.502	0.521	-0.075	_

General Discussion

The use of evidence accumulation models such as the drift-diffusion model hold great promise in addressing the so-called "reliability paradox" (Hedge et al., 2018; Rouder & Haaf, 2019): By analysing individual differences at the latent level (e.g., via DDM parameters) researchers can uncover relationships not apparent at the purely behavioural level. The current work was inspired by an incidental observation that when difference scores of DDM

parameters were analysed, a large and negative correlation emerged between the difference score in the boundary separation parameter and the difference score in the non-decision time parameter. In this paper we have confirmed this finding more formally, via reanalysis of behavioural data (the two experiments of Schuch & Grange, 2019, as well as three experiments from Dutilh et al., 2019) and via a series of computational simulation studies. These simulations were conducted across a range of software implementations of the DDM, as well as using a different evidence accumulation model (the LBA; Brown & Heathcote, 2008). In Appendix C we outline details of additional analyses to explore whether the spurious correlation is caused by difficulties in parameter optimisation when accuracy rates are very high, but find that it had little impact. In addition, in Appendix D we report the results of fitting a Bayesian hierarchical version of the diffusion model (as implemented in the hBayesDM package in R; Ahn et al., 2017) to Experiment 1 data of Dutilh et al. (2019) and again find a large negative correlation. Together, these results using different models and fitting techniques suggest that the result is general.

We begin this discussion by summarising our behavioural and simulation findings; we then offer some suggestions as to the potential cause of the spurious correlation between boundary separation difference and non-decision time difference difference, before providing some recommendations for researchers wishing to use DDM or LBA difference scores in their own work.

Summary of Findings

Correlation Between a-Difference and t0-Difference

The correlation between a-difference and t0-difference emerged in the majority of our analyses. Specifically, it was present in all of the experiments and conditions reanalysed from Schuch and Grange (2019), was present in two out of three experiments in Dutilh et al.

(2019), and was present in the simulations (but not all; see later). Visualisation of this correlation in the Schuch and Grange (2019) data (Figure 2) and in the simulations where it was present (Figure 4) suggest this negative correlation is not driven by outliers in the data, but indeed represents a strong negative linear relationship across the range of difference scores. In the simulations, we only observed the negative correlation when either (a) there was no true difference in model parameters between simulated experimental conditions, or (b) only drift rate v was manipulated between simulated experimental conditions; when a true difference existed in boundary separation, non-decision time, or all three main parameters, the correlation disappeared. This suggests that the spurious correlation occurs only when there is no difference between experimental conditions, or the difference is isolated to the drift rate. This simulation result is congruent with the reanalysis of the behavioural data. For example, Experiment 1 of Dutilh et al. (2019) had no behavioural manipulation between the two experimental conditions, and we observed the negative correlation between a-difference and t0-difference; in Experiment 2, the behavioural manipulation influenced estimates of drift rate, and again we observed the negative correlation; in Experiment 3, however, the behavioural manipulation influenced the boundary separation parameter, and the negative correlation between a-difference and $t\theta$ -difference disappeared.

Further Correlations Between Parameter Difference Scores

While the negative correlation between *boundary*-difference and *non-decision*-difference was the most pronounced and most consistent relationship between parameter difference scores, we also observed some other correlations between parameter difference scores. In particular, we observed medium-to-large correlations between *a*-difference and *v*-difference in the reanalysis of Experiment 1 of Schuch and Grange (2019; ranging from r = .33 to .54) and in Experiment 1 of Dutilh et al. (2019; r = .30); this

correlation was absent from the reanalysis of Experiment 2 of Schuch and Grange, but was medium and *negative* in Experiments 2 and 3 of Dutilh et al. (rs = -.32 and -.22, respectively). This correlation emerged also in Simulation 1 using the DDM (r = .47), and in Simulation 4 using the LBA (r = .64). Recall that these simulations had no true difference in parameter values between conditions. In Simulation 2 where changes in parameters were introduced, we observed the correlation between a-difference and v-difference only when t0 was selectively changed (ranging from r = .46 to .52). When other parameters were selectively changed between conditions, or all three parameters were changed, the correlation disappeared.

This correlation arises due to individuals with larger difference scores in boundary separation having larger difference scores in drift rate; but note that if the difference score in drift rate is positive, this reflects *higher* drift rates in the *hard* condition relative to the *easy* condition. This is because the difference score is calculated as the parameter estimate for the *hard* condition minus the parameter estimate for the *easy* condition, and drift rates tend to be *lower* in harder conditions than in easy conditions. One possibility is that there is some form of tradeoff occurring during the model fitting when no true differences exist between conditions in the boundary separation and drift rate parameters.

We sometimes observed a correlation between v-difference and $t\theta$ -difference. Although not consistently present, it was small-to-medium and positive in Experiment 1 Conditions 2 and 4 (rs = .18 & .30 respectively) and Experiment 2 Conditions 1 and 2 of Schuch and Grange (rs = .16 and .41, respectively), as well as in Experiments 2 and 3 in Dutilh et al. (2019; rs = .44 and .38, respectively); it was small and negative in Experiment 1 of Dutilh et al. (r = -.17). In Simulations 1 and 4, this correlation was small and negative (rs = -.22 & -.24, respectively), but note that it did not replicate in the EZ-diffusion analysis of the same data in Simulation 1. It was however again present in the LBA model in Simulation 4 (r = -.18). It was also present in Simulation 2, but only when boundary separation was manipulated between conditions (rs = -.39, -.17, & -.22 for small, medium, and large effect size differences, respectively). Hence, from the simulation studies, it seems that a small negative spurious correlation between v-difference and $t\theta$ -difference emerges when the third parameter, boundary separation, is manipulated between conditions, or when there are no differences between the conditions at all.

In general, the simulation results seem to suggest that when there is a difference between conditions in one of the main parameters (or no difference between conditions at all), a spurious correlation tends to occur between the difference scores of the other two parameters. The size of the spurious correlation between difference scores is largest for the relationship between a-difference and t0-difference, and medium-to-small for the relationship between v-difference and a-difference, and v-difference and a-difference.

Recommendations for Researchers

In all of the simulations reported in the paper (and indeed the model fits to behavioural data), we allowed all three main parameters to freely vary across experimental conditions. Such an approach is common in the literature when wishing to draw inferences on meaningful parameter changes across conditions (see Donkin et al., 2011; Donkin et al., 2019). However, it could be that the spurious correlation between *a*-difference and *t0*-difference is exacerbated by unnecessary model flexibility (i.e., when parameters are allowed to vary freely across conditions even when there was no true parameter difference in the data-generating process). To assess this, we conducted an additional simulation similar to the design of Simulation 1 where no true difference exists between two experimental conditions in the generated data; however, during model fitting, drift rate—although still a free parameter—was constrained to take on the same value across conditions. The correlation

between best-fitting parameters using *fast-dm-30* are shown in Table 10. The correlation between *a*-difference and *t0*-difference was still large and negative. Of course, this model is still more flexible than the "true" data-generating model, but constraining boundary separation and/or non-decision time to be equal across conditions would prohibit us from examining the difference score in these parameters.

Table 10. Product-moment correlation coefficients between the fitted parameters from the fast-dm-30 fitting routine with drift rate not free to vary between conditions. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v	t0 (easy)	t0 (hard)	a diff	t0 diff
a (easy)	_						
a (hard)	0.994	_					
v	0.042	0.036	_				
t0 (easy)	-0.047	-0.043	0.004	_			
t0 (hard)	-0.041	-0.042	0.006	0.998	_		
a diff	-0.090	0.016	-0.058	0.037	-0.011	_	
t0 diff	0.096	0.016	0.029	-0.068	-0.003	-0.752	

This leads us to a recommendation for researchers wishing to use evidence accumulation models in assessments of individual differences: Only allow parameters to vary freely across conditions during the fitting process if there is strong a priori theoretical justification for supposing parameter differences are expected, or formal model selection/competition techniques have suggested that models with additional free parameters are justified (Donkin et al., 2011; see Heathcote et al., 2015 for an excellent overview of this and other general recommendations to researchers using formal modelling). Formal model selection techniques, such as Bayesian information criterion (BIC) and Akaike's Information Criterion (AIC), can be used to temper quality of model fit with a penalty term for additional free parameters: All else being equal, if two models fit equally well, the simpler model—that is, the model with fewer free parameters—will be preferred. With this approach, difference

scores on certain model parameters will only be calculated by the researcher when the model-selection process has suggested that a model where these certain model parameters change across conditions fits the data better than a model where the parameters are fixed across conditions. This would then avoid the spurious correlation reported in the current paper as we do not find the spurious correlation between *a*-difference and *t0*-difference when the true data-generating model had real differences in either of these parameters across conditions.

To exemplify the technique of model competition, and how it would avoid the calculation of a spurious correlation between a-difference and $t\theta$ -difference, we conducted formal model selection techniques on the data generated in Simulation 1, where no true differences in parameter values existed across conditions in the data-generating process. Eight possible models were then constructed (see Table 11); each model differed on the eligibility of one or more DDM parameters to freely vary across conditions. The simplest model—Model 1, which has only three free parameters (v, a, and $t\theta$, which are not free to vary across conditions)—is correctly selected by the model selection technique of choosing the model with the lowest AIC value (or BIC value).

In this case, the researcher would not be justified in interpreting a model where *a* and *t0* are free to vary across conditions, thus avoiding the spurious correlation between *a*-difference and *t0*-difference. In addition, note that in Simulation 2 where the data were generated from a "true model" with all three main parameters changing across conditions we did not observe the spurious negative correlation (see Figure 3). In this situation, a model where all three parameters are free to vary would win the model competition, and the spurious correlation would likely not be present in any subsequent individual differences analysis.

However, recall that in Simulation 5 we generated simulated data with no true difference between any of the main parameters between conditions but with a large correlation between *a*-difference and *t0*-difference. We were interested in whether this correlation could be recovered by the model-fitting procedure, and found that it could. However, as no true difference was present between any of the three main parameters across conditions, model competition techniques select a model in which the main parameters are not allowed to freely vary across conditions (see Appendix E); as such, researchers would miss the true correlation between *a*-difference and *t0*-difference because they would fit a model to the data where these parameters do not change across condition (so there are no difference scores in parameters).

The recommendation we provide to engage in model competition appears to minimise exposure to the spurious correlation—which likely arises only in overly flexible models—but also leaves the possibility that a true correlation between *a*-difference and *t0*-difference could be missed if the best-fitting model is one where the parameters are not free to vary across conditions. In summary, we believe the cost of finding a spurious correlation outweighs the cost of missing a true correlation and recommend engaging in model competition techniques and only analysing further the winning model.

The recommendation we provide to engage in model competition appears to minimise exposure to the spurious correlation—which likely arises only in overly flexible models—but also leaves the possibility that a true correlation between a-difference and t0-difference could be missed if the best-fitting model is one where the parameters are not free to vary across conditions. Note, however, that such a situation where there is a true correlation between the a-difference and t0-difference—but at the same time the mean difference across participants in both parameters is zero—probably does not occur very often in real data. In summary, we believe the cost of finding a spurious correlation outweighs the cost of missing a true

correlation and recommend engaging in model competition techniques and only analysing further the winning model.

Table 11. Results of the model competition approach to analysing data generated from Simulation 1. Each row depicts a different model based on whether drift rate (v), boundary separation (a), and non-decision time (t0) is free to vary across conditions or not (if yes, denoted by a tick, and by a cross if not). LL is the log-likelihood of the fit. AIC and BIC refer to the total Akaike's and Bayesian Information Criteria, respectively, summed across all simulated participants. W_{AIC} and W_{BIC} represent Akaike weights for each model based on the AIC and BIC values, respectively. Bold & underlined model represents the winner of the model competition.

Model	Vary v?	Vary a?	Vary t0?	LL	AIC	BIC	W _{AIC}	$\mathbf{W}_{\mathrm{BIC}}$
Model 1	<u>x</u>	<u>X</u>	<u>x</u>	<u>-715,490</u>	1,436,982	1,453,784	1	<u>1</u>
Model 2	✓	X	X	-715,956	1,439,912	1,462,316	0	0
Model 3	X	✓	X	-715,946	1,439,893	1,462,296	0	0
Model 4	X	X	✓	-716,093	1,440,185	1,462,589	0	0
Model 5	X	✓	✓	-716,684	1,443,367	1,471,372	0	0
Model 6	✓	X	✓	-716,637	1,443,274	1,471,279	0	0
Model 7	✓	✓	X	-716,401	1,442,803	1,470,807	0	0
Model 8	✓	✓	✓	-717,127	1,446,253	1,479,858	0	0

An additional tool to use for model selection is Akaike Weights (e.g., Wagenmakers & Farrell, 2004). Selecting a model based on raw AIC or BIC scores becomes challenging when two (or more) models' IC scores differ by a small amount. Although one can still select the model with the smallest IC score, the researcher is left wondering how strongly they can disregard the next-best model. Akaike weights estimates the probability that each model in the set of all models considered will be superior when applied to new data (McElreath, 2020). As such, these weights can be used to quantify the degree of superiority of the winning model. As can be seen in Table 11, the winning model has a Weight of 1, indicating decisive

support for this model. For more information and further use-cases of Akaike Weights, see Wagenmakers and Farrell (2004). Importantly, both of the model selection techniques discussed—that based on overall AIC or BIC values, and that based on Akaike Weights—can be applied to group-averaged data (as above) or applied to the individual participant level. A model that is superior at the group level may not be superior for each participant.

As an alternative (or complement) to formal model selection, researchers could use a structural equation modelling approach for estimating the parameters of evidence accumulation models (e.g., Schubert et al., 2022)⁶. In such a framework, the evidence accumulation model parameters can be conceptualised as latent variables (which are estimated repeatedly on the basis of different subsets of the raw data; for example, separate estimations on the basis of odd-numbered and even-numbered trials). The difference scores in evidence accumulation model parameters can then be estimated as latent change scores, which are derived by regressing the parameter estimates from the "hard" condition on the parameter estimates from the "easy" condition (for reviews of latent change score modelling see Kievit et al., 2018 and McArdle, 2009). The latent change scores representing the difference scores can then be correlated. In Appendix F, we report first investigations of the spurious correlations with latent change score models. We observed a Heywood case: small and non-significant variances of latent change scores, but large correlations between change scores, including a large negative correlation between the latent change score for boundary separation and non-decision time (i.e., the spurious correlation). However, we found that in models where correlations could occur between indicator diffusion model parameters within a condition, the spurious correlation was absent. This provides preliminary evidence that the correlations of model parameters within a condition could play a role for the spurious

⁶ We would like to thank Anna-Lena Schubert for this idea.

correlations between difference scores to occur and that latent change score modelling might be a useful approach to mitigate its impact.

Conclusion

We have identified—both in behavioural data and via computational simulations—that spurious correlations can arise between model parameter difference scores when using evidence accumulation models. Researchers wishing to use this class of models for inter-individual differences research should be aware of these spurious correlations, and should bear them in mind when wishing to draw conclusions from difference-scores. One way we have identified to mitigate the impact of these spurious correlations—but we submit that there will be other solutions we have not thought of—is to conduct formal model competition to ensure that difference scores are only calculated for a model parameter when model competition has shown that such parameter flexibility is warranted by the data.

Open Practices Statement

All raw data, analysis code, and model simulation code are available for download from https://osf.io/2h4jt/.

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Appendices

Appendix A—Parameter Recovery Visualisations for Simulation 1

Appendix B—Simulation 2 Numerical Correlation Matrices

Appendix C—Examining the Impact of High Accuracy

Appendix D—Bayesian Hierarchical Diffusion Modelling

Appendix E—Model Competition for Simulation 5

Appendix F—Latent Change Score Modelling

Appendix A—Parameter Recovery Visualisations for Simulation 1

Recovery of the generating parameter values used to generate simulated data was excellent in the fitting routine. The correlation between the parameter values used to generate simulated data and the recovered best-fitting parameter values were as follows: a-easy: r = .995, t0-easy: r = .999, v-easy: r = .997, a-hard: r = .996, t0-hard: r = .999, v-hard: r = .997. The correlations are visualised in Figure A1.

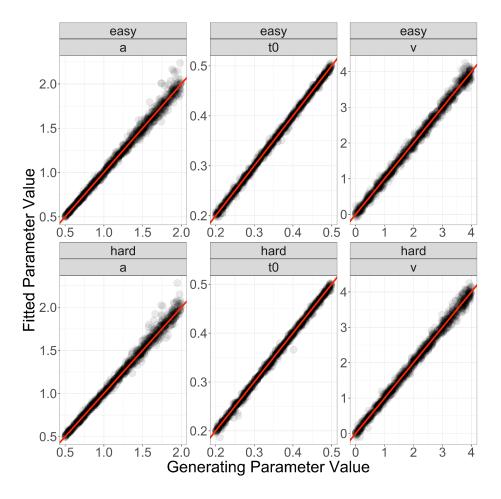


Figure A1. Visualisation of correspondence between parameter values used to generate simulated data (x-axis) and the recovered best-fitting parameter value (y-axis) for each simulated participant (shown as grey circles). Results are shown for the three main diffusion model parameters in both the "easy" and the "hard" condition. The diagonal red lines correspond to location representing perfect recovery.

Appendix B—Simulation 2 Correlation Matrices

v Small

Table B1. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.991	_							
v (easy)	0.004	-0.006	_						
v (hard)	-0.033	-0.033	0.517	_					
t0 (easy)	-0.016	0.000	-0.046	-0.051	_				
t0 (hard)	-0.015	-0.007	-0.043	-0.049	0.997	_			
a diff	-0.081	0.051	-0.073	-0.001	0.114	0.058	_		
v diff	-0.038	-0.028	-0.473	0.510	-0.006	-0.007	0.072	_	
t0 diff	0.010	-0.092	0.052	0.034	-0.083	-0.011	-0.774	-0.017	_

Table B2. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.981	_							
v (easy)	-0.011	-0.005	_						
v (hard)	-0.046	-0.035	0.515	_					
t0 (easy)	-0.028	0.004	-0.043	-0.046	_				
t0 (hard)	-0.021	-0.017	-0.048	-0.051	0.981	_			
a diff	-0.073	0.123	0.028	0.054	0.166	0.021	_		
v diff	-0.036	-0.030	-0.470	0.515	-0.005	-0.004	0.028	_	
t0 diff	0.037	-0.108	-0.024	-0.020	-0.191	0.005	-0.746	0.004	_

a Small

Table B3. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.487	_							
v (easy)	0.058	0.051	_						
v (hard)	0.047	0.058	0.993	_					
t0 (easy)	0.011	0.074	0.030	0.029	_				
t0 (hard)	0.014	0.067	0.033	0.028	0.996	_			
a diff	-0.491	0.521	-0.006	0.011	0.063	0.054	_		
v diff	-0.092	0.060	-0.026	0.089	-0.007	-0.043	0.150	_	
t0 diff	0.028	-0.077	0.035	-0.010	-0.013	0.080	-0.104	-0.391	_

Table B4. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.492	_							
v (easy)	0.054	0.040	_						
v (hard)	0.042	0.041	0.993	_					
t0 (easy)	-0.018	0.053	0.043	0.042	_				
t0 (hard)	0.013	0.058	0.033	0.030	0.971	_			
a diff	-0.506	0.502	-0.014	-0.001	0.070	0.045	_		
v diff	-0.097	0.007	-0.051	0.070	-0.014	-0.025	0.104	_	
t0 diff	0.128	0.026	-0.039	-0.045	-0.076	0.165	-0.101	-0.049	

t0 Small

Table B5. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.991	_							
v (easy)	0.035	0.035	_						
v (hard)	0.027	0.034	0.9994	_					
t0 (easy)	-0.037	-0.031	0.018	0.014	_				
t0 (hard)	-0.006	-0.011	0.011	0.003	0.497	_			
a diff	-0.063	0.070	0.000	0.056	0.045	-0.035	_		
v diff	-0.069	0.000	0.013	0.123	-0.035	-0.068	0.514	_	
t0 diff	0.031	0.020	-0.007	-0.011	-0.493	0.510	-0.079	-0.034	

Table B6. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.979	_							
v (easy)	0.043	0.039	_						
v (hard)	0.036	0.039	0.994	_					
t0 (easy)	-0.048	-0.038	0.014	0.006	_				
t0 (hard)	-0.013	-0.029	0.003	-0.003	0.496	_			
a diff	-0.087	0.119	-0.022	0.016	0.050	-0.082	_		
v diff	-0.062	0.006	0.004	0.117	-0.064	-0.054	0.331	_	
t0 diff	0.035	0.008	-0.011	-0.009	-0.4899	0.515	-0.132	0.009	

v Medium

Table B7. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.989	_							
v (easy)	-0.024	-0.032	_						
v (hard)	-0.026	-0.015	0.492	_					
t0 (easy)	0.005	0.010	-0.027	0.012	_				
t0 (hard)	0.014	0.010	-0.026	0.010	0.997	_			
a diff	-0.078	0.072	-0.051	0.072	0.030	-0.028	_		
v diff	-0.002	0.016	-0.481	0.527	0.039	0.035	0.122	_	
t0 diff	0.114	-0.002	0.020	-0.039	-0.053	0.023	-0.769	-0.058	

Table B8. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.980	_							
v (easy)	-0.043	-0.036	_						
v (hard)	-0.042	-0.038	0.496	_					
t0 (easy)	-0.003	0.015	-0.011	0.023	_				
t0 (hard)	0.009	-0.001	-0.021	0.018	0.980	_			
a diff	-0.082	0.118	0.031	0.020	0.088	-0.049	_		
v diff	-0.001	-0.003	-0.482	0.522	0.034	0.040	-0.011	_	
t0 diff	0.060	-0.078	-0.051	-0.021	-0.123	0.077	-0.686	0.029	_

a Medium

Table B9. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.488	_							
v (easy)	0.016	-0.032	_						
v (hard)	0.015	-0.030	0.994	_					
t0 (easy)	0.004	-0.008	-0.001	-0.002	_				
t0 (hard)	0.011	-0.004	0.000	-0.003	0.996	_			
a diff	-0.501	0.511	-0.048	-0.044	-0.012	-0.014	_		
v diff	-0.011	0.023	-0.104	0.009	-0.014	-0.028	0.033	_	
t0 diff	0.080	0.052	0.014	-0.006	-0.041	0.043	-0.028	-0.172	

Table B10. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.473	_							
v (easy)	0.012	-0.035	_						
v (hard)	0.014	-0.032	0.993	_					
t0 (easy)	-0.003	-0.010	-0.008	-0.010	_				
t0 (hard)	0.018	-0.016	-0.009	-0.010	0.973	_			
a diff	-0.508	0.519	-0.046	-0.044	-0.007	-0.033	_		
v diff	0.014	0.031	-0.105	0.011	-0.018	-0.010	0.017	_	
t0 diff	0.089	-0.026	-0.003	0.001	-0.051	0.181	-0.112	0.033	_

t0 Medium

Table B11. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.989	_							
v (easy)	0.031	0.030	_						
v (hard)	0.022	0.030	0.994	_					
t0 (easy)	0.022	0.025	0.010	0.013	_				
t0 (hard)	0.036	0.034	0.002	0.003	0.508	_			
a diff	-0.097	0.049	-0.004	0.052	0.016	-0.014	_		
v diff	-0.082	-0.006	-0.044	0.064	0.021	0.016	0.521	_	
t0 diff	0.015	0.011	-0.009	-0.009	-0.465	0.526	-0.030	-0.005	

Table B12. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.983	_							
v (easy)	0.022	0.028	_						
v (hard)	0.015	0.026	0.994	_					
t0 (easy)	0.003	0.011	0.016	0.019	_				
t0 (hard)	0.026	0.014	0.004	0.008	0.497	_			
a diff	-0.094	0.091	0.033	0.061	0.045	-0.064	_		
v diff	-0.067	-0.020	-0.050	0.060	0.023	0.043	0.253	_	
t0 diff	0.024	0.004	-0.012	-0.010	-0.464	0.537	-0.110	0.021	

v Large

Table B13. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.985	_							
v (easy)	0.089	0.076	_						
v (hard)	0.041	0.049	0.490	_					
t0 (easy)	-0.055	-0.049	-0.053	-0.048	_				
t0 (hard)	-0.041	-0.047	-0.052	-0.051	0.996	_			
a diff	-0.178	-0.003	-0.082	0.041	0.041	-0.030	_		
v diff	-0.051	-0.030	-0.538	0.471	0.007	0.004	0.123	_	
t0 diff	0.165	0.022	0.010	-0.033	0.003	0.089	-0.819	-0.042	_

Table B14. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where drift rate (v) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.971	_							
v (easy)	0.061	0.069	_						
v (hard)	0.031	0.046	0.492	_					
t0 (easy)	-0.044	-0.045	-0.046	-0.044	_				
t0 (hard)	-0.028	-0.063	-0.052	-0.049	0.981	_			
a diff	-0.090	0.149	0.035	0.063	-0.003	-0.148	_		
v diff	-0.032	-0.025	-0.532	0.476	0.003	0.005	0.027	_	
t0 diff	0.081	-0.097	-0.038	-0.028	0.016	0.212	-0.744	0.011	_

a Large

Table B15. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.479	_							
v (easy)	0.047	0.029	_						
v (hard)	0.042	0.033	0.995	_					
t0 (easy)	-0.027	0.014	-0.024	-0.023	_				
t0 (hard)	-0.023	0.007	-0.026	-0.026	0.997	_			
a diff	-0.509	0.512	-0.017	-0.009	0.040	0.029	_		
v diff	-0.045	0.034	-0.019	0.084	0.010	-0.009	0.077	_	
t0 diff	0.053	-0.083	-0.023	-0.046	-0.063	0.020	-0.133	-0.220	_

Table B16. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where boundary separation (a) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.473	_							
v (easy)	0.038	0.011	_						
v (hard)	0.034	0.009	0.994	_					
t0 (easy)	-0.040	0.012	-0.015	-0.016	_				
t0 (hard)	-0.005	0.012	-0.024	-0.026	0.972	_			
a diff	-0.530	0.497	-0.027	-0.024	0.050	0.016	_		
v diff	-0.045	-0.020	-0.049	0.058	-0.016	-0.019	0.026	_	
t0 diff	0.146	0.000	-0.040	-0.041	-0.116	0.123	-0.144	-0.010	_

t0 Large

Table B17. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.991	_							
v (easy)	0.006	0.011	_						
v (hard)	-0.001	0.011	0.994	_					
t0 (easy)	-0.019	-0.017	0.024	0.027	_				
t0 (hard)	0.012	0.010	-0.003	0.002	0.483	_			
a diff	0.002	0.134	0.042	0.092	0.015	-0.009	_		
v diff	-0.065	-0.004	-0.047	0.062	0.030	0.048	0.455	_	
t0 diff	0.030	0.027	-0.026	-0.024	-0.509	0.508	-0.023	0.049	_

Table B18. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 2 where non-decision time (t0) was manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.981	_							
v (easy)	0.011	0.005	_						
v (hard)	0.004	0.003	0.993	_					
t0 (easy)	-0.024	-0.006	0.011	0.012	_				
t0 (hard)	0.006	0.001	0.002	0.009	0.472	_			
a diff	-0.060	0.134	-0.033	-0.005	0.091	-0.025	_		
v diff	-0.064	-0.017	-0.055	0.061	0.013	0.063	0.244	_	
t0 diff	0.029	0.007	-0.009	-0.003	-0.518	0.509	-0.113	0.049	_

Simulation 3: Differences in All Parameters

All Small

Table B19. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.514	_							
v (easy)	0.045	0.022	_						
v (hard)	0.037	0.075	0.483	_					
t0 (easy)	-0.061	-0.009	-0.005	-0.005	_				
t0 (hard)	-0.041	-0.093	-0.037	-0.027	0.504	_			
a diff	-0.518	0.467	-0.025	0.036	0.054	-0.051	_		
v diff	-0.007	0.053	-0.490	0.526	0.000	0.009	0.060	_	
t0 diff	0.019	-0.086	-0.033	-0.023	-0.483	0.513	-0.105	0.009	

Table B20. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a small effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.515	_							
v (easy)	0.028	0.024	_						
v (hard)	0.029	0.066	0.483	_					
t0 (easy)	-0.070	-0.015	0.000	-0.002	_				
t0 (hard)	-0.045	-0.111	-0.040	-0.025	0.500	_			
a diff	-0.511	0.473	-0.005	0.036	0.056	-0.065	_		
v diff	0.002	0.042	-0.492	0.525	-0.002	0.014	0.041	_	
t0 diff	0.024	-0.097	-0.041	-0.024	-0.482	0.518	-0.121	0.016	

All Medium

Table B21. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.512	_							
v (easy)	0.021	0.003	_						
v (hard)	0.072	0.098	0.488	_					
t0 (easy)	0.045	0.027	0.045	-0.002	_				
t0 (hard)	0.010	0.007	-0.025	-0.056	0.480	_			
a diff	-0.511	0.477	-0.019	0.025	-0.019	-0.003	_		
v diff	0.049	0.093	-0.518	0.494	-0.047	-0.030	0.043	_	
t0 diff	-0.034	-0.019	-0.069	-0.053	-0.515	0.506	0.016	0.017	

Table B22. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a medium effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.500	_							
v (easy)	-0.003	-0.015	_						
v (hard)	0.062	0.068	0.487	_					
t0 (easy)	0.043	0.025	0.050	-0.002	_				
t0 (hard)	0.024	0.002	-0.021	-0.049	0.475	_			
a diff	-0.525	0.475	-0.012	0.004	-0.019	-0.023	_		
v diff	0.063	0.082	-0.519	0.494	-0.052	-0.027	0.016	_	
t0 diff	-0.018	-0.023	-0.069	-0.046	-0.512	0.513	-0.004	0.024	

All Large

Table B23. Product-moment correlation coefficients between the fitted parameters from fast-dm-30 fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.506	_							
v (easy)	0.028	-0.005	_						
v (hard)	0.080	0.093	0.499	_					
t0 (easy)	0.053	0.017	0.047	-0.012	_				
t0 (hard)	0.015	0.002	-0.024	-0.055	0.483	_			
a diff	-0.507	0.487	-0.034	0.012	-0.036	-0.013	_		
v diff	0.051	0.097	-0.523	0.478	-0.059	-0.030	0.046	_	
t0 diff	-0.038	-0.015	-0.070	-0.042	-0.511	0.506	0.023	0.029	_

Table B24. Product-moment correlation coefficients between the fitted parameters from EZ-diffusion fitting routine from Simulation 3 where all parameters were manipulated between easy and hard conditions to have a large effect size.

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.489	_							
v (easy)	-0.005	-0.028	_						
v (hard)	0.060	0.053	0.495	_					
t0 (easy)	0.039	0.014	0.053	-0.009	_				
t0 (hard)	0.019	-0.018	-0.011	-0.037	0.476	_			
a diff	-0.519	0.492	-0.022	-0.008	-0.024	-0.037	_		
v diff	0.064	0.080	-0.525	0.480	-0.062	-0.025	0.014	_	
t0 diff	-0.019	-0.032	-0.062	-0.028	-0.508	0.516	-0.013	0.036	_

Appendix C—Examining the Impact of High Accuracy

The analysis reported in this Appendix was inspired by a comment by a Reviewer⁷ who suggested that a potential cause of the spurious correlation between *a*-difference and *t0*-difference could be the difficulty of diffusion models to accurately identify model parameters when accuracy is very high (as the parameter optimisation routine has few error trials to constrain parameter values); it might be then that the spurious correlation is caused (or exacerbated) by the presence of (real or simulated) participants with very high accuracy.

In an initial exploration of this, we re-analysed the data from Simulation 1 as suggested by the Reviewer. Specifically, we plotted the relationship between *a*-difference and *t0*-difference, but colour-coded individual data points by mean accuracy across "easy" and "hard" conditions (see Figure C1).

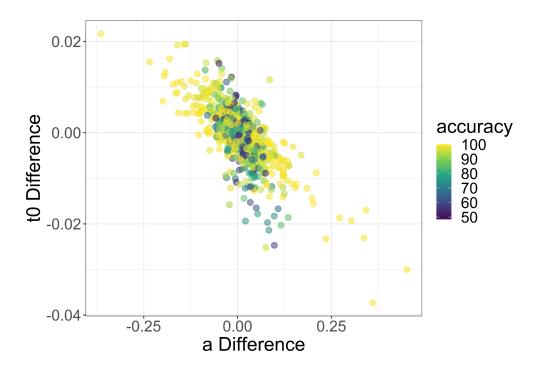


Figure C1. Scatterplot of the relationship between a-Difference and t0-Difference scores from Simulation 1, colour-coded by mean accuracy for each participant.

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⁷ We are extremely grateful to Craig Hedge for this comment.

Consistent with the Reviewer's observation, it does indeed appear that individuals with high levels of accuracy exhibit a strong negative correlation, whereas data points with lower accuracy tend to cluster more around the centre of the plot. We wished to therefore explore further the contribution of high accuracy performance to the occurrence of the spurious correlation reported in the main body of the paper.

New Simulation

In a first approach we conducted a new simulation where the model was forced to have lower accuracy performance. If the spurious correlation is caused by high accuracy rates causing issues with parameter identification (and hence, accurate parameter estimation), we should not observe the correlation when accuracy is forced to be lower. To achieve this, we repeated Simulation 1 but limited the random selection of the boundary separation parameter between 0.2–0.8 (in contrast to a range of 0.5–2.0). All other aspects of the simulation were identical to Simulation 1. The results of the correlation of interest—again colour-coded by accuracy as in Figure C1—are shown in Figure C2.

The mean accuracy rate across all participants in this simulation was 70.95%; only 0.4% of participants had a mean accuracy above 95%, and only 8.4% of participants had an accuracy above 90%. This suggests that the simulation was successful in reducing overall accuracy in simulated participants. Despite this lower accuracy, we still observed the strong negative correlation between a-difference and $t\theta$ -difference, r = -.622.

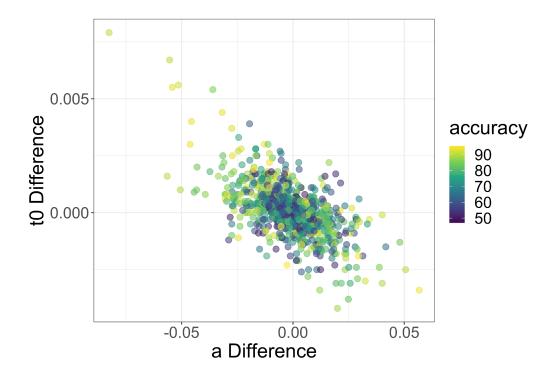


Figure C2. Scatterplot of the relationship between a-Difference and t0-Difference scores from the new Simulation of a model with enforced lower accuracy, colour-coded by mean accuracy for each participant.

Quantile Split Re-Analysis of Simulations 1 and 4

In a second step to investigate the impact of high accuracy, we re-analysed the data from Simulation 1 (DDM) and Simulation 4 (LBA) by splitting the 1,000 simulated participants from each simulation into four quantiles based on the mean accuracy per simulated participant (calculated as accuracy averaged across "easy" and "hard" conditions per simulated participant). The correlation between a-difference (caution-difference in the case of LBA) and $t\theta$ -difference was then computed separately for the different quartiles (see Figures C3 and C4 for plots of these correlations). We observed that the correlation between a-difference and $t\theta$ -difference occurred across all accuracy levels. In Simulation 1, the correlation amounted to r = -.85 in the quartile with highest accuracy, and r = -.69, r = -.69, r = -.66 in the other quartiles. In Simulation 4, the correlation was r = -.94 in the quartile with highest accuracy, and r = -.84, r = -.72, and r = -.78 in the other quartiles. Hence, in

both simulations, the spurious correlation between the difference scores in non-decision time and response caution seemed to be more pronounced in the 25% of simulated subjects with highest overall accuracy. Importantly, though, the spurious correlation was observed across all accuracy ranges, even in the 25% artificial subjects with lowest accuracy, in both simulations. This suggests that high accuracy may inflate the spurious correlation, but it is not the only reason for the spurious correlation to occur.

The more pronounced correlation in the quartile with highest accuracy might be driven by the larger range of a-difference (caution-difference) scores in the 25% artificial participants with highest accuracy levels. One possible interpretation of this data pattern is that having very few error trials leads to less precise estimation of the boundary separation parameter, which in turn leads to a larger range of a-difference (caution-difference) scores, and therefore more pronounced correlations between a-difference and t0-difference scores.

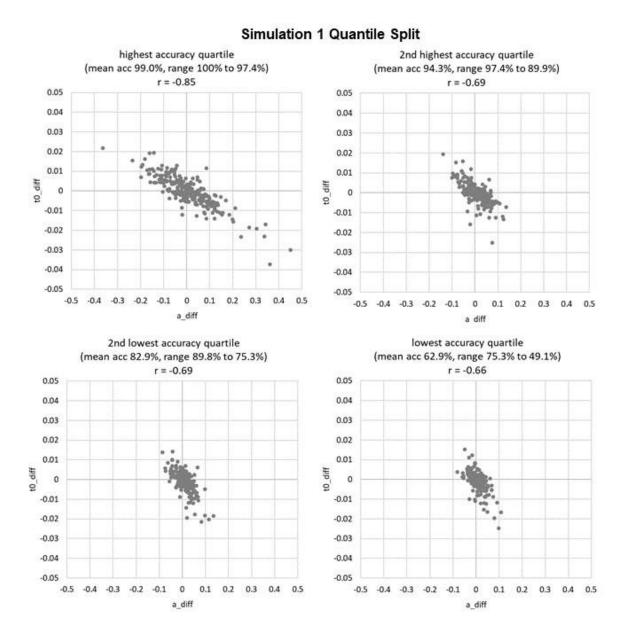


Figure C3. Quantile Split of Simulation 1 (DDM). Scatterplots of the relationship between *a*-difference (a_diff) and *t0*-difference (t0_diff) scores in the different accuracy quartiles (N=250 simulated participants per quartile). Points represent individual simulated participant difference scores in diffusion model parameters.

Simulation 4 Quantile Split

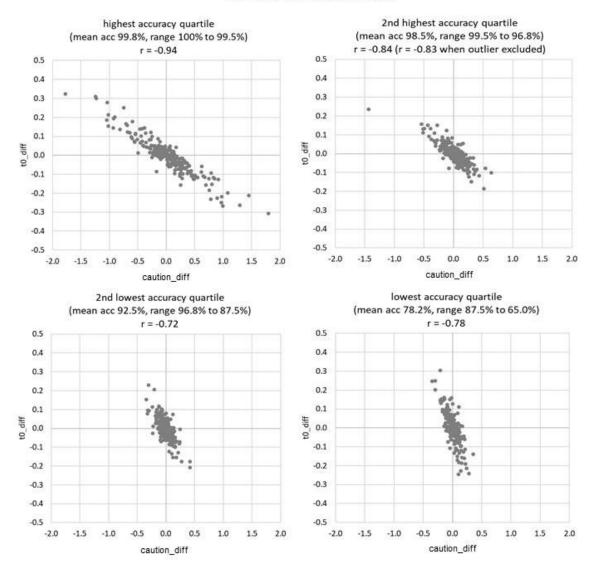


Figure C4. Quantile Split of Simulation 4 (LBA). Scatterplots of the relationship between *caution*-difference (caution_diff) and *t0*-difference (t0_diff) scores in the different accuracy quartiles (N=250 simulated participants per quartile). Points represent individual simulated participant difference scores in LBA model parameters. Note that the scales for the difference scores are different between Figures C3 and C4 due to the different parameterizations of the Drift-Diffusion Model (DDM) and the Linear Ballistic Accumulator Model (LBA) and/or different precision in parameter recovery in the two models.

To summarise, both the additional simulation with enforced lower accuracy, and the post-hoc analyses dividing the simulated participants by their accuracy level, suggest that high accuracy may inflate the spurious correlation between $t\theta$ -difference and a-difference scores, but it is not the only reason for the spurious correlation to occur.

Appendix D—Bayesian Hierarchical Diffusion Modelling

We utilised the hBayesDM package (Ahn et al., 2017) in R to fit a Bayesian hierarchical diffusion model to the data from Experiment 1 of Dutilh et al. (2019). The model was fit to the "easy" and the "hard" condition separately using 2,000 samples (with 1,000 treated as warm-up samples, later discarded) from the posterior distribution across 4 chains. The default priors in the hBayesDM package were used, and initial parameter values for the sampling were determined randomly. The results of the fitting procedure are shown in Table B1. As can be seen, the large negative correlation between a-difference and $t\theta$ -difference was also present in this fitting procedure (r = -.821).

Table D1. Product-moment correlation coefficients between the fitted parameters from Bayesian hierarchical diffusion modelling of data from Experiment 1 of Dutilh et al. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.792	_							
v (easy)	0.064	0.273	_						
v (hard)	-0.069	0.205	0.850	_					
t0 (easy)	-0.157	0.216	0.597	0.604	_				
t0 (hard)	-0.152	-0.012	0.533	0.597	0.878	_			
a diff	-0.220	0.421	0.343	0.431	0.578	0.206	_		
v diff	-0.237	-0.173	-0.461	0.076	-0.114	-0.003	0.077	_	
t0 diff	0.042	-0.474	-0.247	-0.139	-0.436	0.044	-0.821	0.233	_

Appendix E—Model Competition for Simulation 5

We repeated the model competition analysis for the data generated in Simulation 5 with a "true" negative correlation between a-difference and t0-difference of r = -.70, but with no population-level difference between any of the main parameters between conditions. The details of the models' specification that entered the competition are in Table E1, together with the fit statistics. As can be seen, the model where v, a, and t0 are not free to vary across conditions is correctly selected as the winner (as this is the model that generated the data).

Table E1. Results of the model competition approach to analysing data generated from Simulation 1. Each row depicts a different model based on whether drift rate (v), boundary separation (a), and non-decision time (t0) is free to vary across conditions or not (if yes, denoted by a tick, and by a cross if not). LL is the log-likelihood of the fit. AIC and BIC refer to the total Akaike's and Bayesian Information Criteria, respectively, summed across all simulated participants. W_{AIC} and W_{BIC} represent Akaike weights for each model based on the AIC and BIC values, respectively. Bold & underlined model represents the winner of the model competition.

Model	Vary v?	Vary a?	Vary t0?	LL	AIC	BIC	W _{AIC}	W_{BIC}
Model 1	<u>X</u>	<u>X</u>	<u>x</u>	<u>-572,161</u>	1,150,321	1,167,124	<u>1</u>	<u>1</u>
Model 2	✓	X	X	-576,991	1,161,981	1,184,385	0	0
Model 3	X	✓	X	-620,123	1,248,246	1,240,650	0	0
Model 4	X	X	✓	-707,278	1,422,557	1,444,960	0	0
Model 5	X	✓	✓	-716,287	1,442,574	1,470,579	0	0
Model 6	✓	X	✓	-708,398	1,426,797	1,454,801	0	0
Model 7	✓	✓	X	-621,822	1,253,644	1,281,649	0	0
Model 8	✓	✓	✓	-716,815	1,445,629	1,479,235	0	0

Appendix F — Latent Change Score Modelling

We explored whether the spurious correlation between a-difference and $t\theta$ -difference also occurred when using latent change score modelling (Kievit et al., 2018; McArdle 2009; see Schubert et al., 2015 and 2022 for applications of this approach). To examine this, we ran a version of Simulation 1 reported in the main paper where there is no true difference between any of the diffusion model parameters between easy and hard conditions. Data were again simulated from 1,000 artificial participants in two experimental conditions using the same parameters as in Simulation 1. Differing from Simulation 1, we simulated 2,000 trials per condition per participant to reduce simulation noise even more (it was 1,000 trials per condition per participant in Simulation 1). The data for each condition for each participant were then separated into two halves (odd trials in one half, even trials in the other half). The diffusion model was then fit to each half separately. Within each half, v, a, and t0 were allowed to vary freely across the easy and the hard conditions (i.e., the model fitting procedure within each half was identical to that in Simulation 1). Because odd trials and even trials were fitted separately, this procedure yielded (potentially) different parameter estimates for odd and even trials. The correlation matrices for odd and even trials are shown in Tables F1 and F2, respectively.

Table F1. Product-moment correlation coefficients between the fitted parameters from the fast-dm-30 fitting routine for odd trials. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.990	_							
v (easy)	0.045	0.045	_						
v (hard)	0.038	0.047	0.994	_					
t0 (easy)	-0.047	-0.042	0.000	0.003	_				
t0 (hard)	-0.043	-0.046	0.003	0.003	0.997	_			
a diff	-0.040	0.100	0.005	0.063	0.034	-0.020	_		
v diff	-0.060	0.012	-0.040	0.073	0.020	0.002	0.512	_	
t0 diff	0.055	-0.049	0.036	0.007	0.012	0.084	-0.741	-0.251	_

Table F2. Product-moment correlation coefficients between the fitted parameters from the fast-dm-30 fitting routine for even trials. Diff = difference scores on parameters (hard minus easy).

	a (easy)	a (hard)	v (easy)	v (hard)	t0 (easy)	t0 (hard)	a diff	v diff	t0 diff
a (easy)	_								
a (hard)	0.990	_							
v (easy)	0.046	0.037	_						
v (hard)	0.044	0.042	0.994	_					
t0 (easy)	-0.044	-0.043	-0.001	0.003	_				
t0 (hard)	-0.043	-0.050	0.002	0.004	0.997	_			
a diff	-0.017	0.123	-0.063	-0.011	0.003	-0.051	_		
v diff	-0.015	0.052	0.006	0.114	0.033	0.017	0.476	_	
t0 diff	0.007	-0.098	0.042	0.018	0.001	0.074	-0.751	-0.216	_

Latent Model Description

We initially fitted the latent change score model as depicted in Figure F1. In this model, the best-fitting diffusion parameters are used as indicator variables to estimate latent variables for each of the three main diffusion model parameters in each condition. For

example, the latent parameter reflecting boundary separation in the easy condition (i.e., a_easy) is estimated from the best-fitting diffusion model parameters for the boundary separation parameter in the easy condition for odd trials and for even trials (i.e., a_easy_odd & a_easy_even). Latent change scores for each diffusion model parameter—which reflect the difference in latent estimates of diffusion model parameters across easy and hard conditions—were estimated by regressing latent parameter estimates from the hard condition on the parameter estimates from the easy condition. The question of interest is then whether we observe a correlation between the latent difference score for boundary separation (shown as Δa) and non-decision time ($\Delta t0$).

It is possible that in the case of a spurious correlation, one would observe a large correlation between the two latent change scores, with at the same time very small variances, which could be an instance of a "Heywood case" (i.e., implausible or highly unlikely parameter estimates in factor analytic models; Heywood & Filon, 1931; see also Cooperman & Waller, 2021). If this were observed, the presumably spurious correlation should not be interpreted, and should not be used for further correlational analyses.

To fit the model we used the package *lavaan* in R (Rosseel, 2012). DDM parameters were standardised before fitting the structural equation model (SEM), and SEM optimisation was achieved via maximum likelihood.

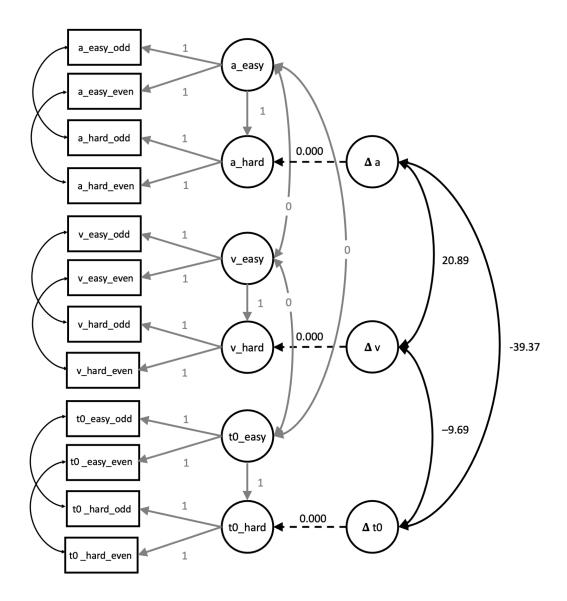


Figure F1. Path diagram for latent change score model 1. Rectangles represent indicator variables, and circles represent latent variables. Paths with thin lines to the left of the indicator variables reflect the residual covariances in the model. Grey path lines (and their numerical weights) indicate fixed paths; dashed lines indicate non-significant relationships.

The model demonstrated evidence of a Heywood case: The variances for the latent change scores were small and non-significant, yet the beta parameters reflecting the relationship between them were large. Note that the spurious negative relationship between a-difference and $t\theta$ -difference was present (b = -39.37), as was the smaller positive relationship between a-difference and v-difference sometimes reported in the main body of

the paper (b = 20.89). However, the latent change score model in Figure 1 did not provide a good fit to the data (see Table F3), but this lack of fit—and especially the significant result of the chi-square test—could be driven by the large sample size in the current simulation leading to small deviations of fit becoming highly significant due to extremely high power.

Table F3. Latent change score model fit indices. Np = number of parameters in each model. χ^2 = chi-square test (with * indicating significant tests). MSEA = Root mean square error of approximation. CFI = comparative fit index. AIC = Akaike's Information Criterion. W_{AIC} = Akaike weights for each model based on the AIC values. Bold & underlined model represents the winner of the model competition.

Model	Np	χ^2	RMSEA	CFI	AIC	$\mathbf{W}_{ ext{AIC}}$
Model 1	27	2393.51*	0.192	0.95	-10,119	0.000
Model 2	32	47.33	0.000	1.00	-12,455	0.119
Model 3	<u>30</u>	<u>47.38</u>	<u>0.000</u>	<u>1.00</u>	<u>-12,459</u>	0.881

We then explored a second model (see Figure F2) where condition-specific correlations could occur between all diffusion model parameters in the indicator variables. Note that in Model 1 correlations were only allowed between matching DDM parameters across conditions (e.g., a_easy_odd was only allowed to correlate with a_hard_odd). These correlations between the fitted DDM parameters are very high (about r = .99, see Tables F1 and F2), because the data for the easy and hard conditions were generated using identical parameter values (see main text for details of Simulation 1). In contrast, the correlations between fitted DDM parameters within a condition (e.g., between a_easy_odd, v_easy_odd, and t0_easy_odd) were all very small (ranging from about r = .05 to r = -.05, see Tables F1 and F2), and were set to zero in Model 1. In Model 2, we set a different correlational structure between the indicator variables. In Model 2, DDM parameters could correlate with all other parameters in the same condition (e.g., now a easy odd could correlate with

v_easy_odd and t0_easy_odd). The matching DDM parameters across conditions (e.g., between a_easy_odd and a_hard_odd) were no longer allowed to correlate in this model.⁸

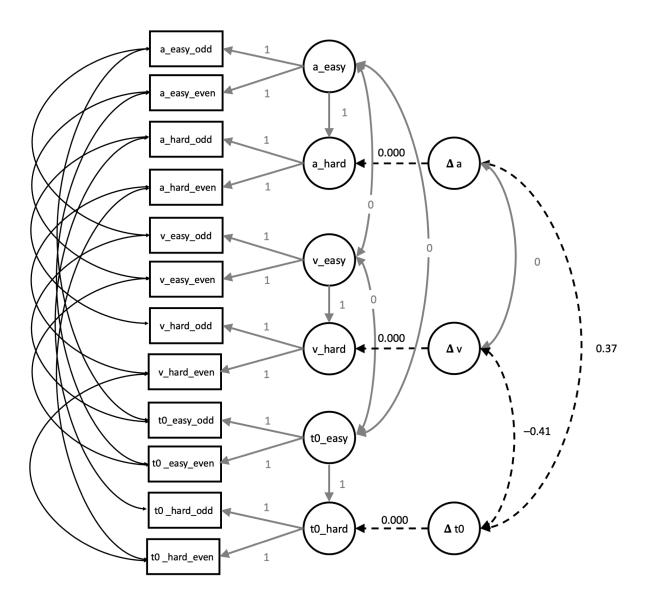


Figure F2. Path diagram for latent change score model 2. Rectangles represent indicator variables, and circles represent latent variables. Paths with thin lines to the left of the indicator variables reflect the residual covariances in the model. Grey path lines (and their numerical weights) indicate fixed paths; dashed lines indicate non-significant relationships.

⁸ Whether the matching DDM parameters across conditions were allowed to correlate or not led to very similar model output in Models 2 and 3.

Another change we made was to fix the correlation between the latent change scores a-difference and v-difference to zero 9 . Model 2 showed a considerably better fit than Model 1 on all metrics (see Table F3). Critically, the variances of all latent change scores were still very close to zero and non-significant (as in Model 1), but now there were no significant relationships between a-difference and t0-difference, or between v-difference and t0-difference. This latter result was investigated by a third model (Model 3, see Figure F3) which fixed the relationships between all latent change scores to zero. As shown in Table F1, Model 3 was the best fit among all considered.

As described above, Models 2 and 3 differed from Model 1 with respect to the correlational structure between the indicator variables. In Models 2 and 3 (but not in Model 1), the DDM parameters within a condition (e.g., between a_easy_odd, v_easy_odd, and t0_easy_odd) were allowed to correlate. Interestingly, in Models 2 and 3, the estimated covariances between the DDM parameters within a condition were all significant, albeit they were very small in size.

This observation prompted us to inspect the within-condition correlations of parameters in our simulations more closely. We focused on all simulations in which we observed the spurious correlation between difference scores. On a descriptive level, we observed a consistent pattern in the fitted DDM parameters within a condition: The correlation between a and t0 is always slightly negative (around r = -0.05); the correlation between a and v is always slightly positive (around r = 0.05); the correlation between v and t0 is still smaller (around r = 0.005 or smaller). This pattern occurs in the simulation reported in Tables F1 and F2 in this Appendix, as well as in the simulations reported in Tables 4, 5, 7, 8, and 10 in the main text, and Tables B13 and B14 in Appendix B.

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⁹ Note that we did try to fit a version of Model 2 where this correlation remained a free parameter, but the model fitting routine produced a warning that the covariance matrix of the latent variables was not positive definite. Ignoring this warning showed the relationship between a-difference and v-difference was non-significant.

That is, in all the simulations where we find the pronounced negative correlation between boundary_difference and t0_difference (and in most cases, a moderate positive correlation between boundary_difference and v_difference), we find that within conditions, the correlation between a and t0 is always slightly negative (around r = -0.05), and the correlation between a and v is always slightly positive (around r = 0.05). In contrast, in the simulations where we do not observe the spurious correlations between difference scores, and in the empirical data, the pattern is less consistent (the empirical data are presumably noisier due to smaller sample size). It thus seems possible that these small but systematic interdependencies between the DDM parameters within a condition are somehow inflated when calculating difference scores.

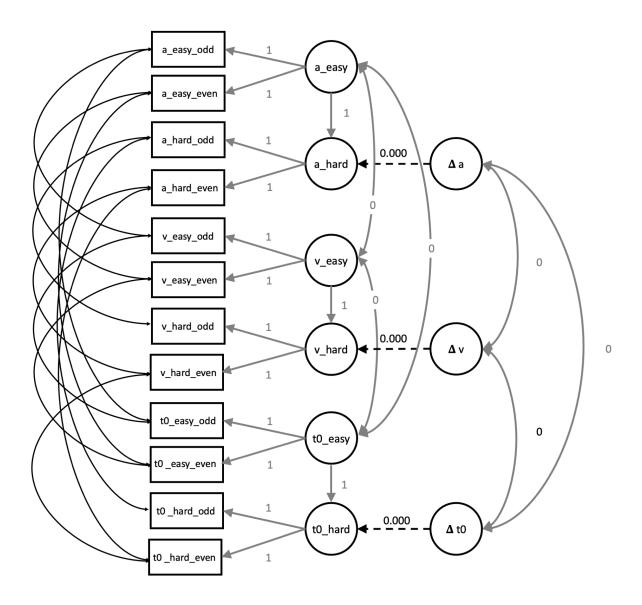


Figure F3. Path diagram for latent change score model 3. Rectangles represent indicator variables, and circles represent latent variables. Paths with thin lines to the left of the indicator variables reflect the residual covariances in the model. Grey path lines (and their numerical weights) indicate fixed paths; dashed lines indicate non-significant relationships.